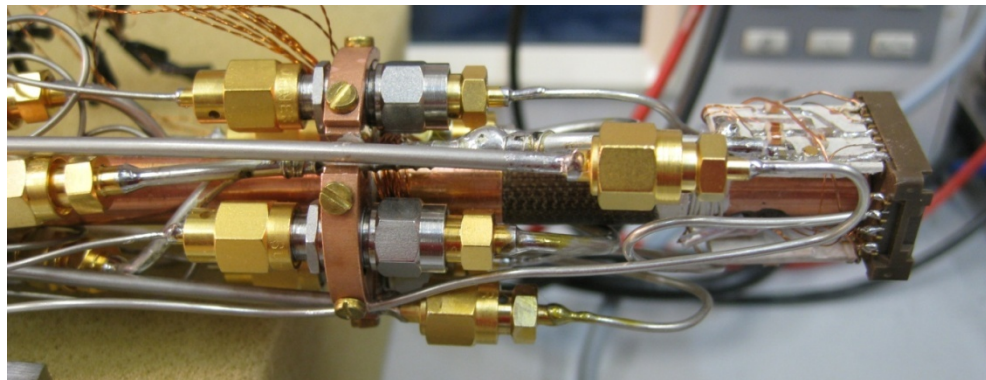


# Radio-Frequency Quantum Point Contact Charge Detection



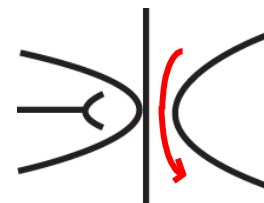
Thomas Müller  
Nanophysics Group, ETH Zürich

In collaboration with

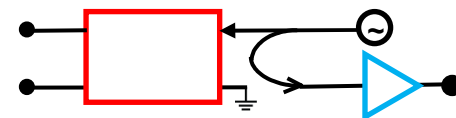
J. Güttinger, B. Küng, T. Choi, S. Hellmüller, D. Bischoff, P. Studerus, C. Barengo, K. Ensslin, T. Ihn  
GaAs/AlGaAs heterostructures grown by M. Reinwald and W. Wegscheider; S. Schön

# Contents

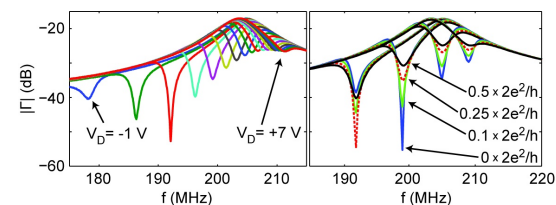
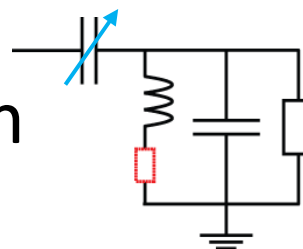
I. QPC charge detection



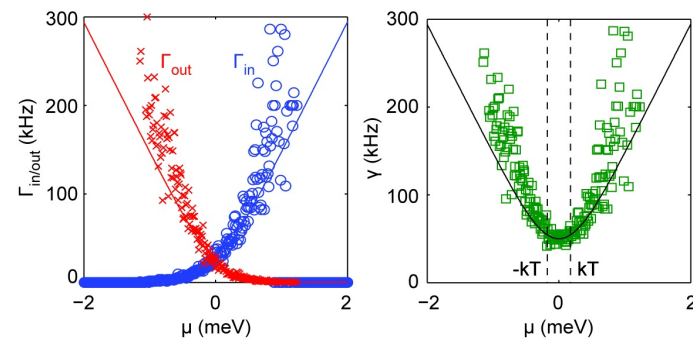
II. Radio-frequency reflectometry



III. Experimental realisation



IV. Multi-level tunneling into a graphene quantum dot connected to a single lead

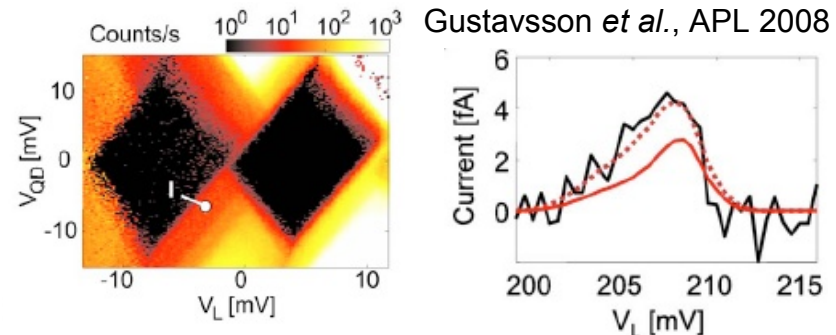
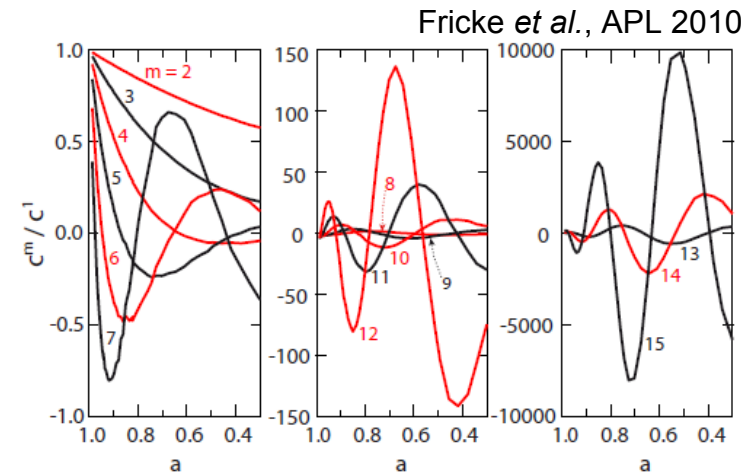
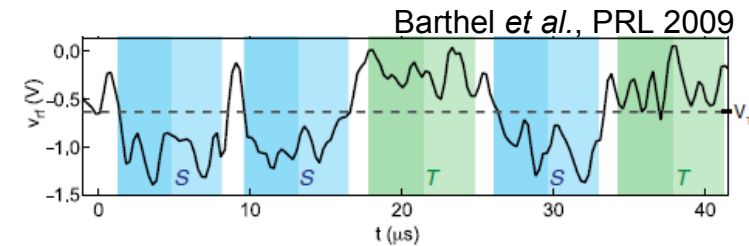


# I. Why More Time Resolution?

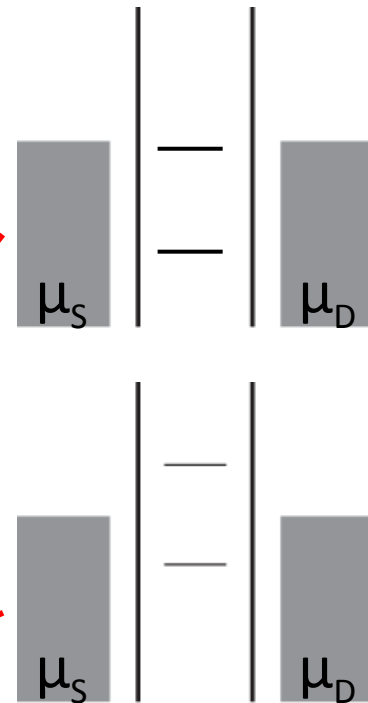
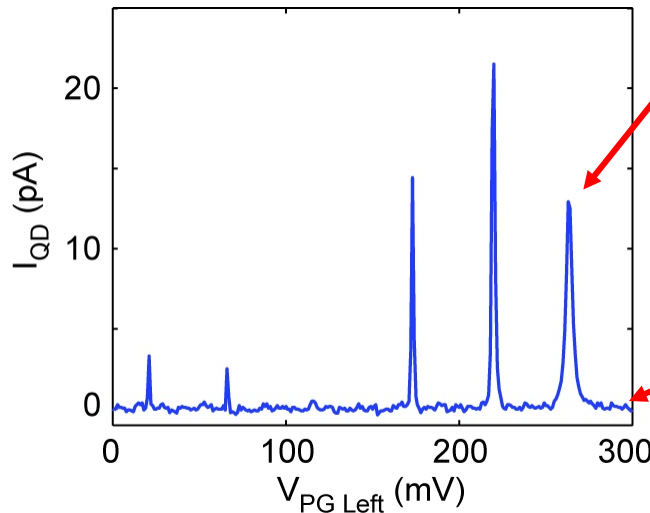
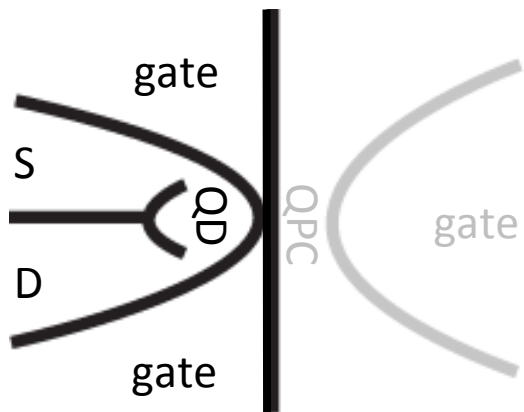
Single-shot detection

Measurement time

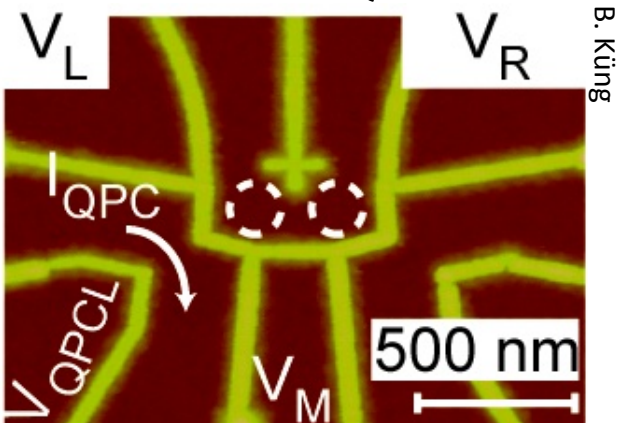
Less restricted by low tunnel rates



# I. Quantum Dots

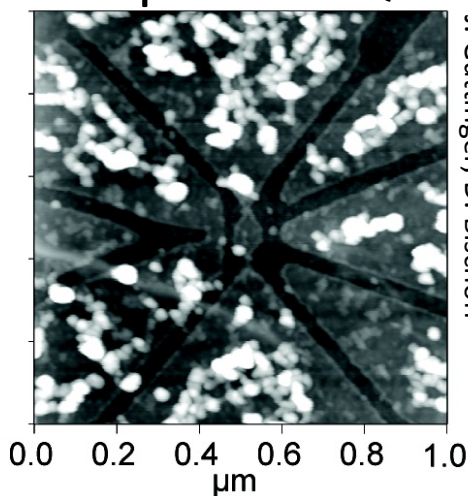


GaAs DQD



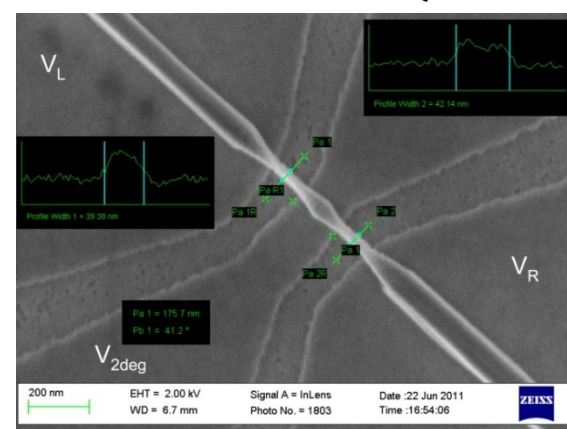
B. Küng

Graphene SQD



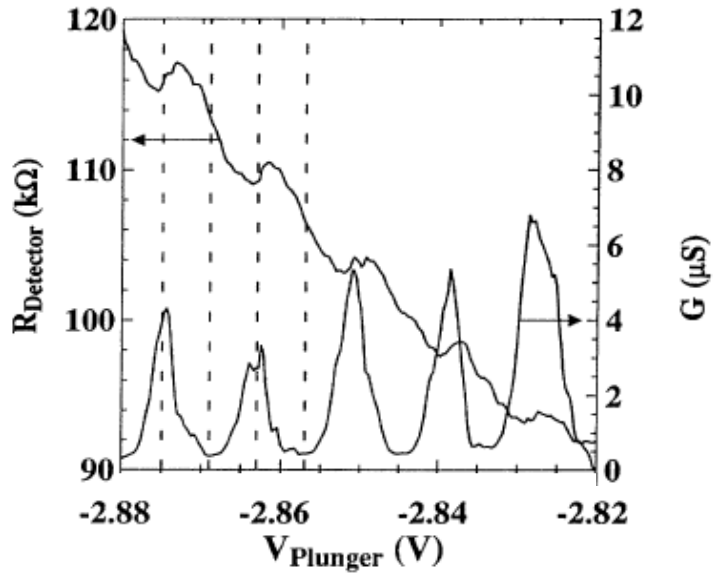
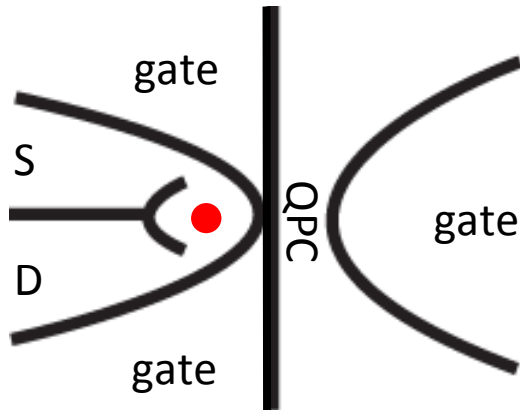
J. Güttinger, D. Bischoff

InAs NW SQD

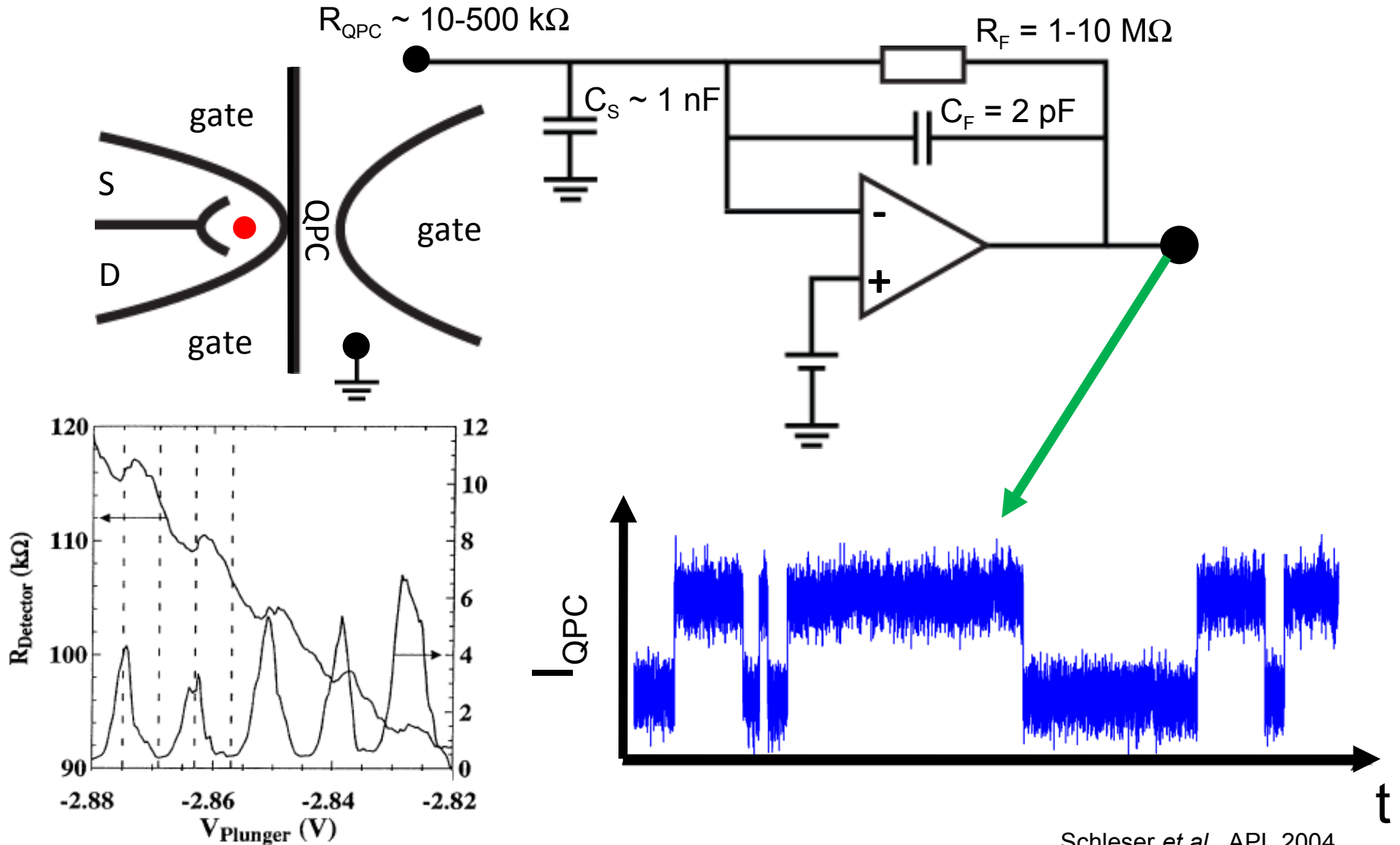


T. Choi

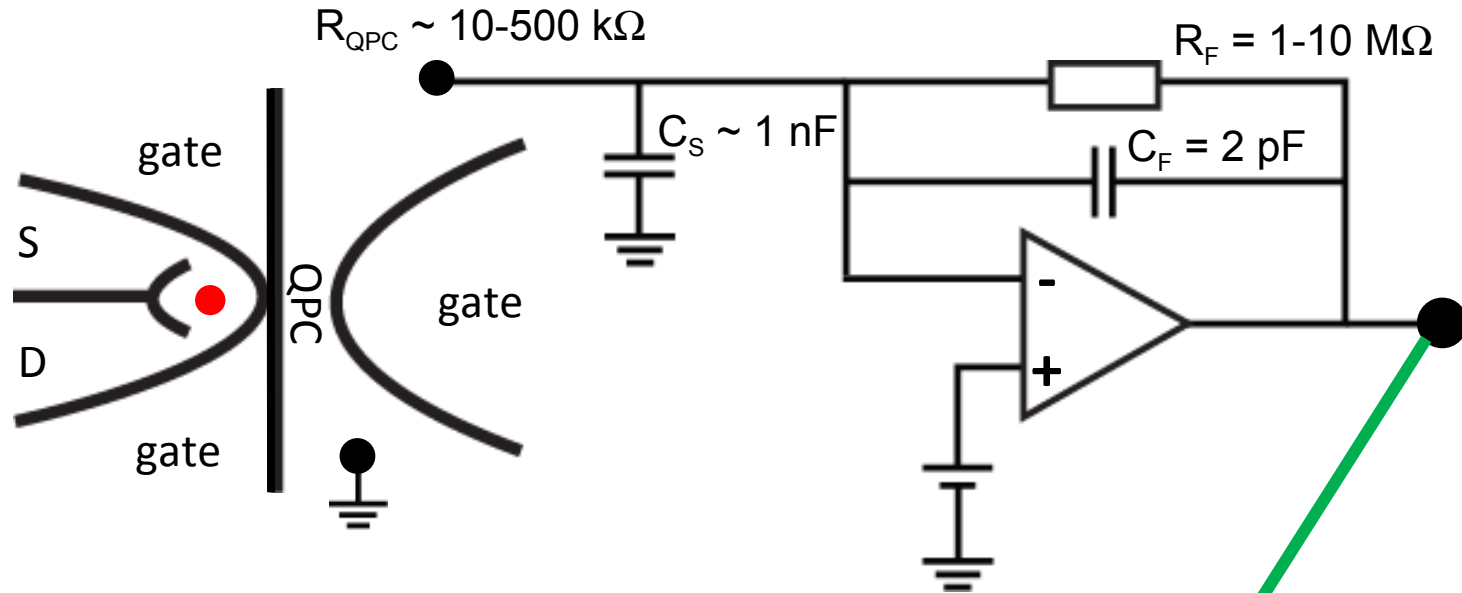
# I. QPC Charge Detection



# I. Time-Resolved Charge Detection

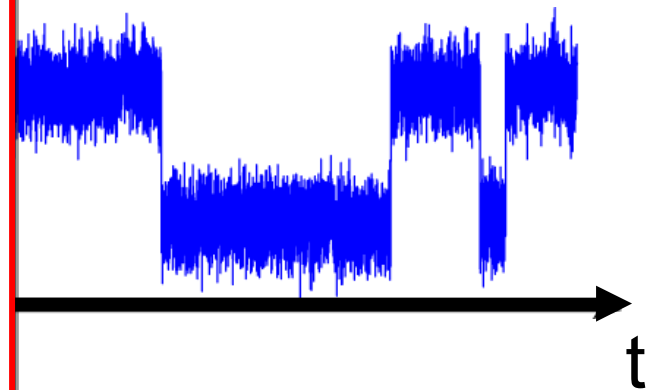


# I. Time-Resolved Charge Detection

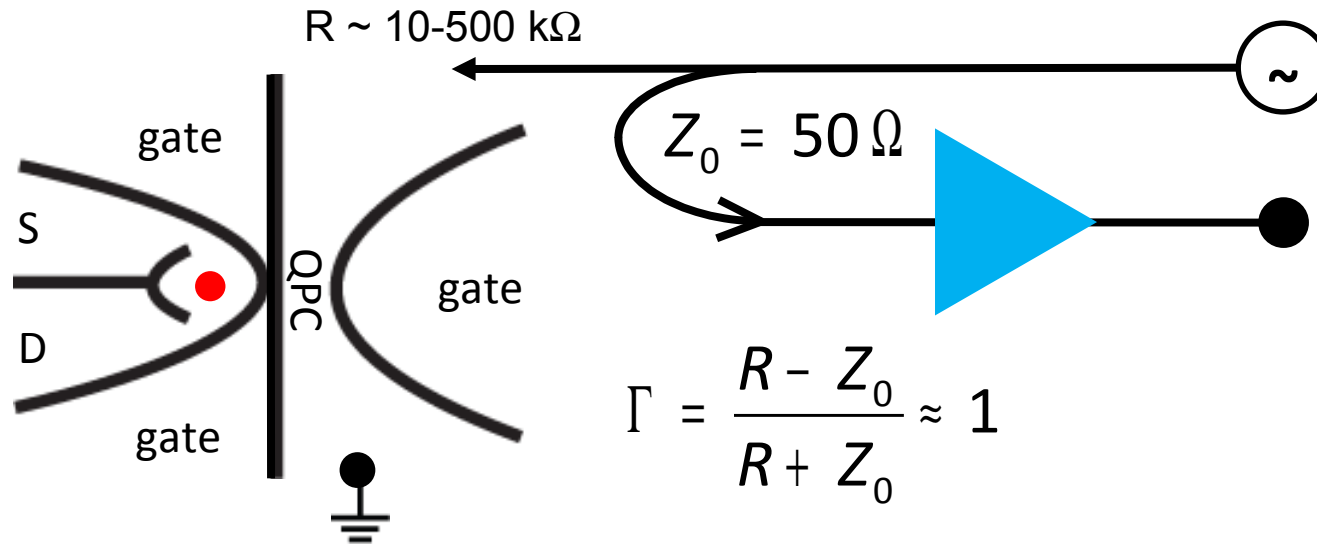


Capacitive noise gain  
„Slow“ electronics  
 $1/f$  noise

limit bandwidth to  $\sim 100 \text{ kHz}$

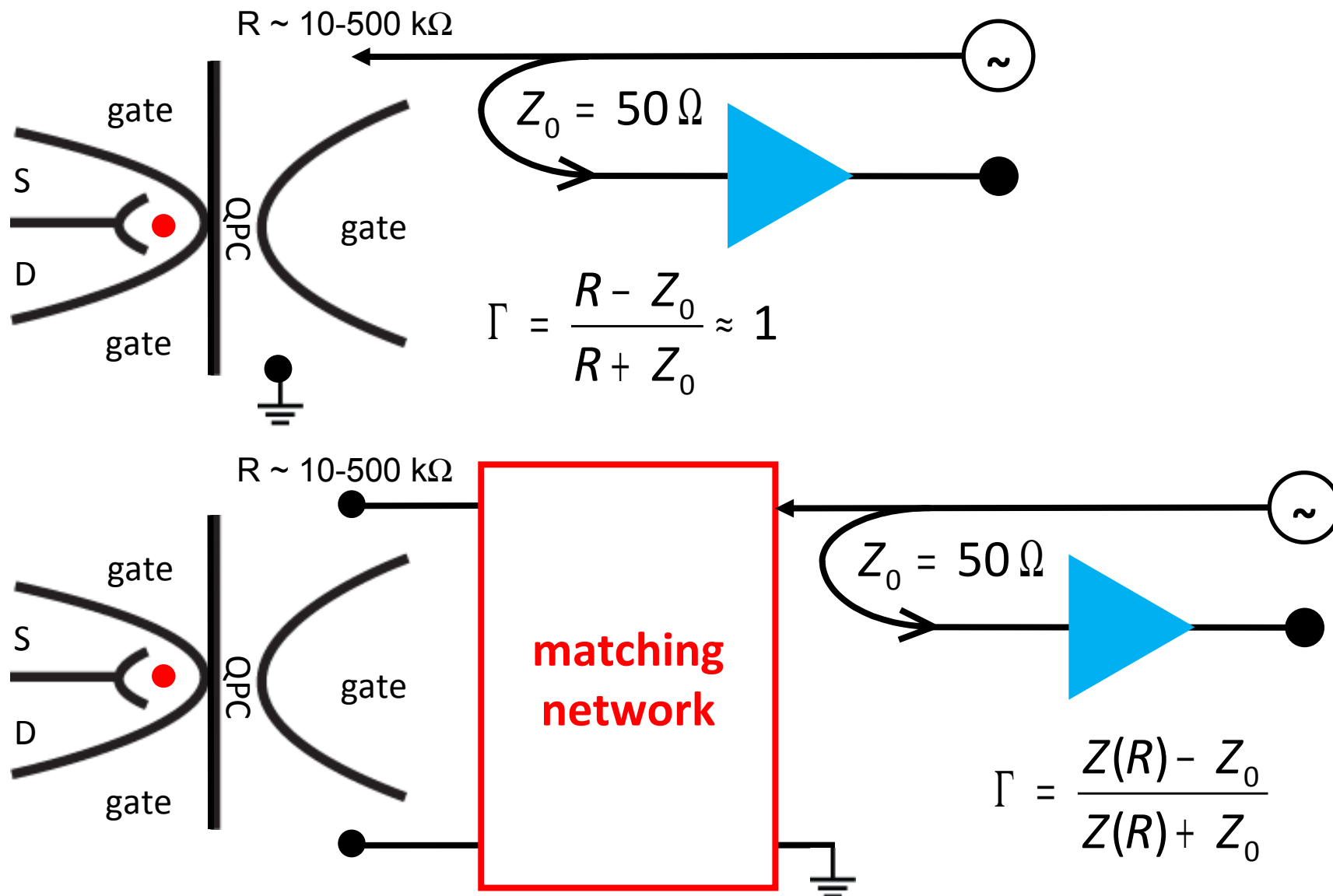


## II. Reflection Coefficient $\Gamma$



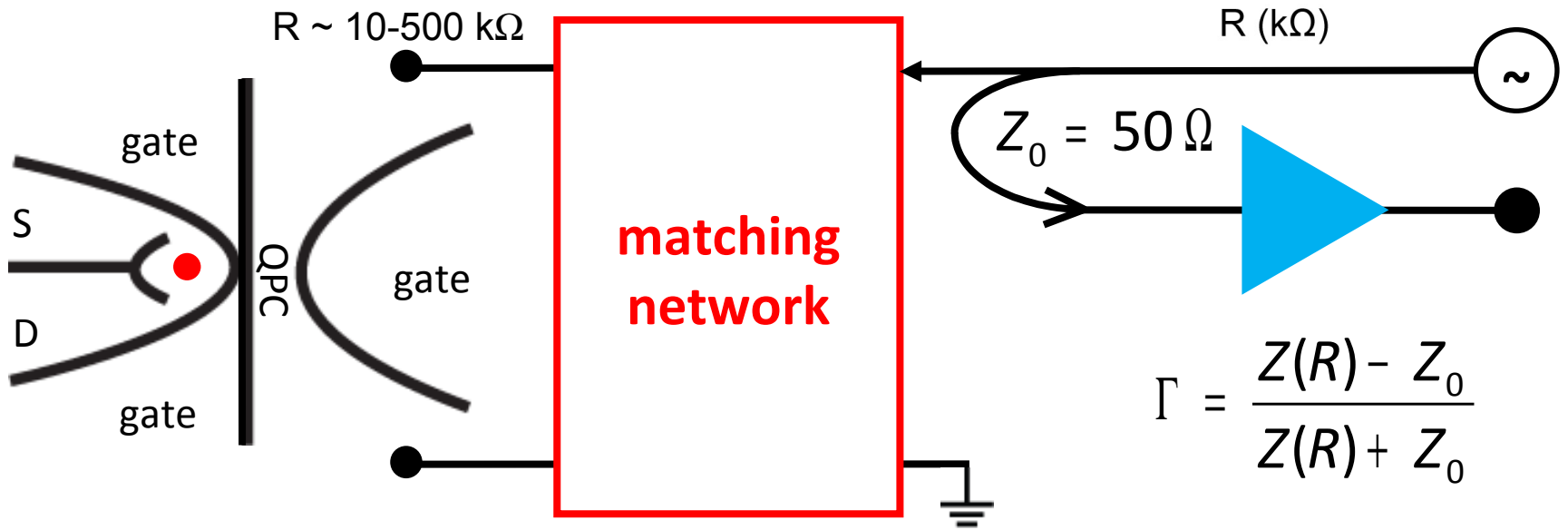
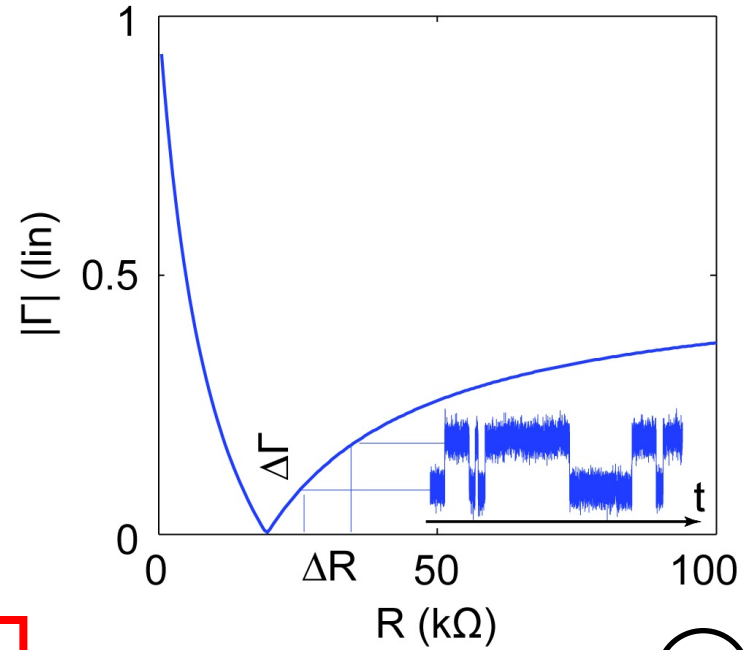


## II. Reflection Coefficient $\Gamma$



# II. Reflection Coefficient $\Gamma$

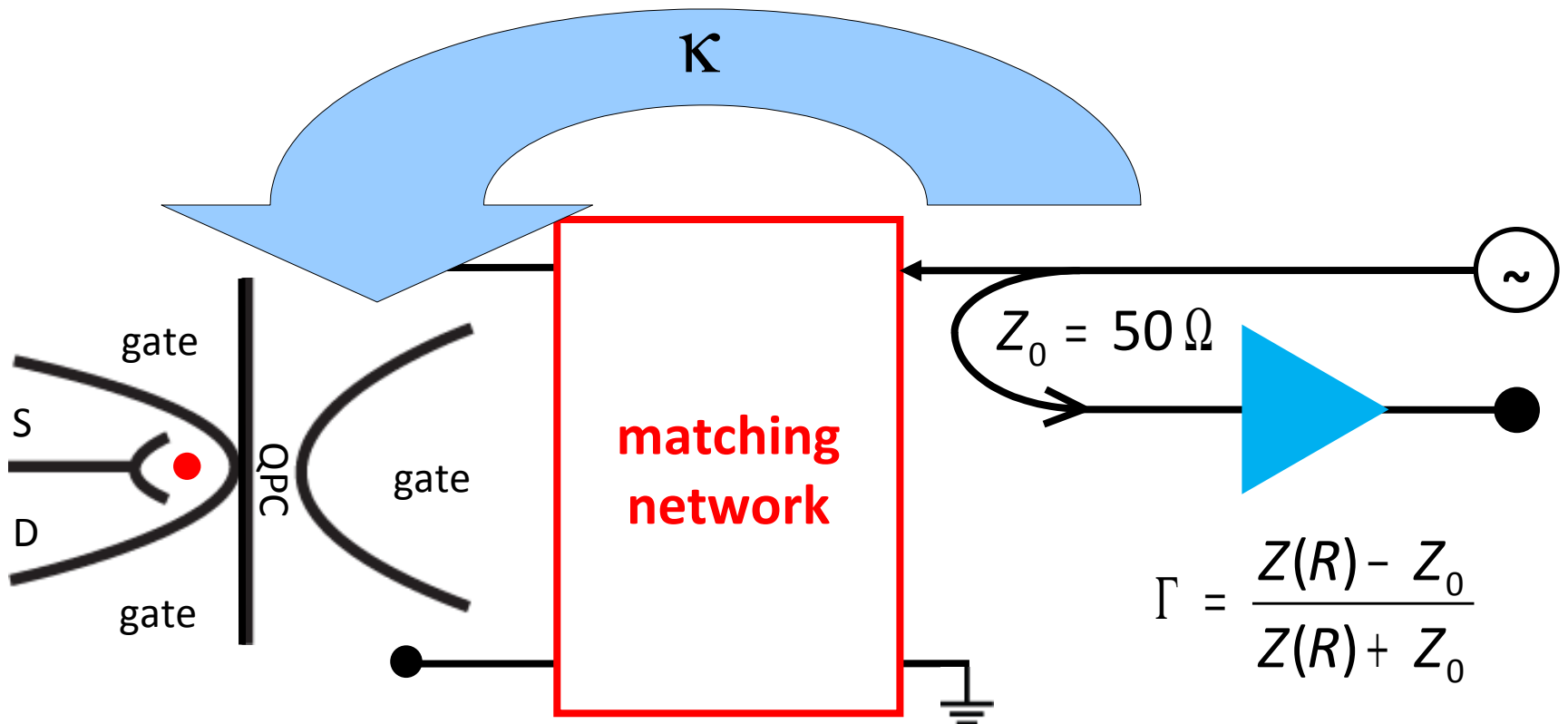
Optimise  $\Delta\Gamma(\Delta R)$



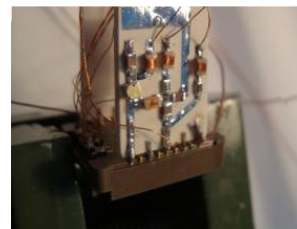
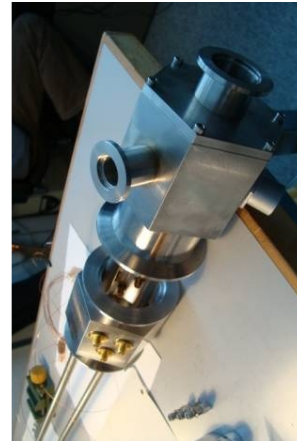
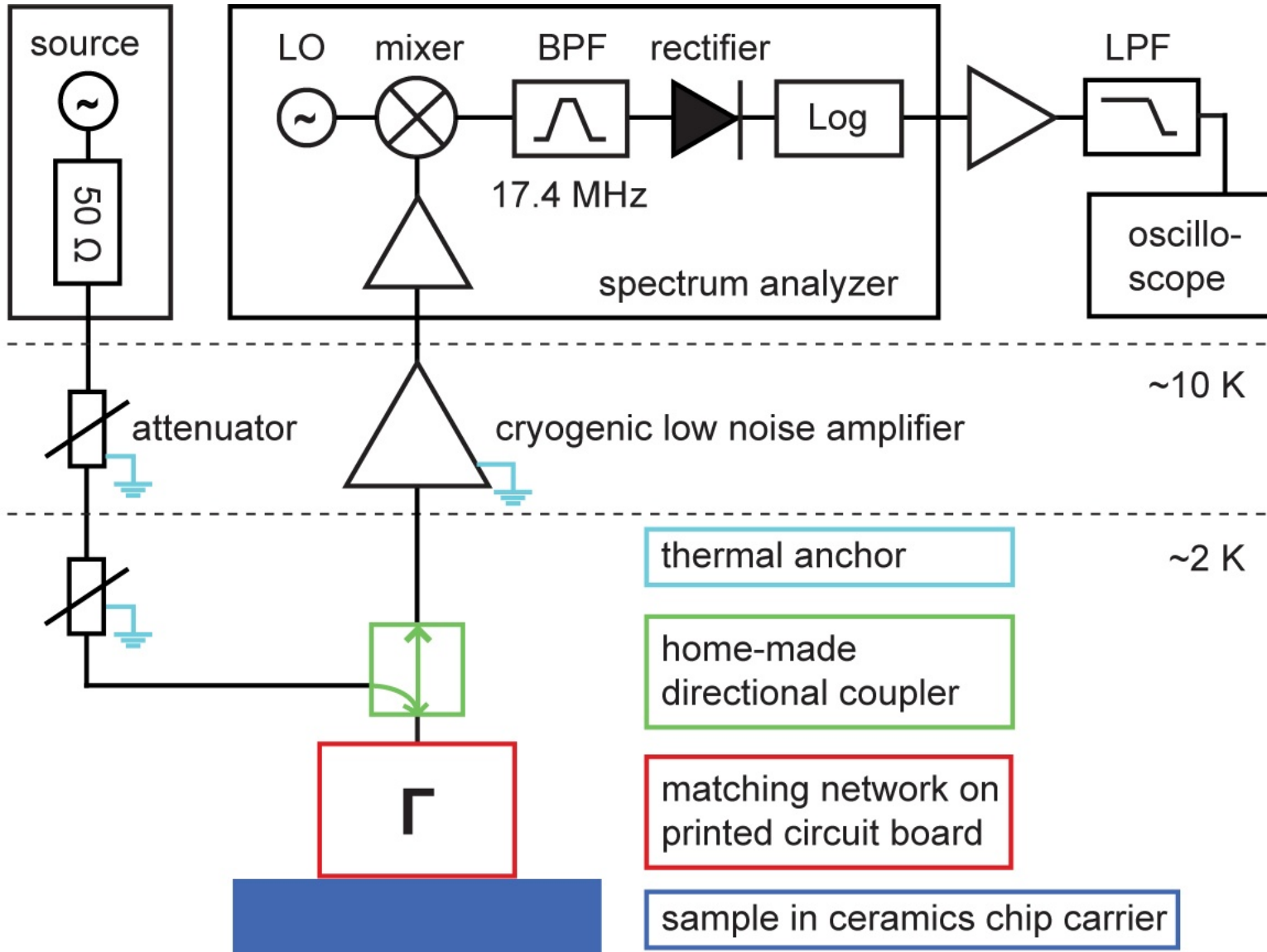
## II. Signal-to-Noise Ratio

Optimise  $\Delta\Gamma(\Delta R)$

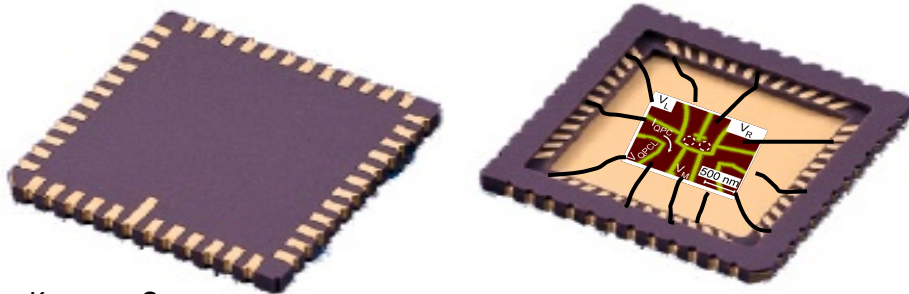
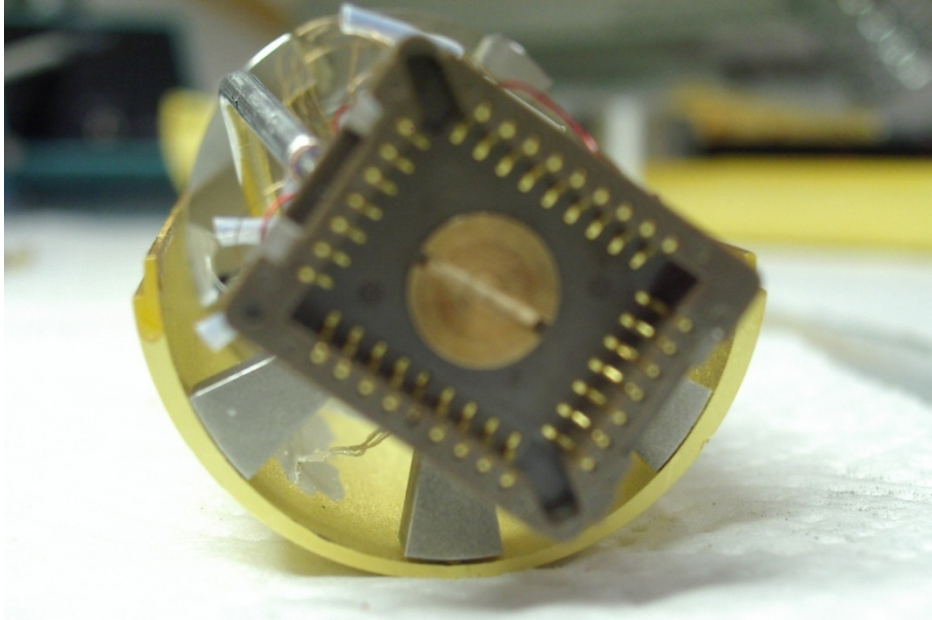
$$\Delta\Gamma = \kappa \Delta R / 2R$$



# II. Schematic Measurement Setup



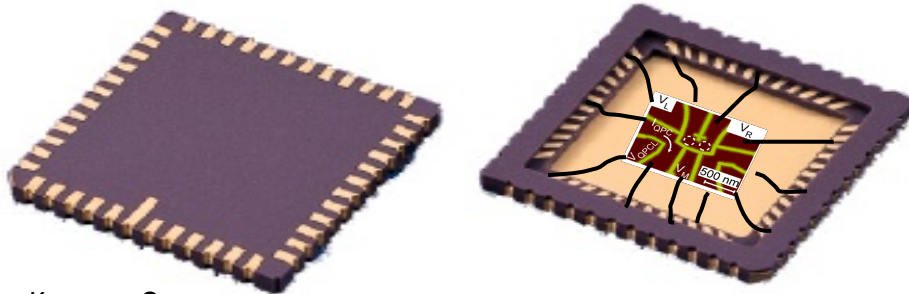
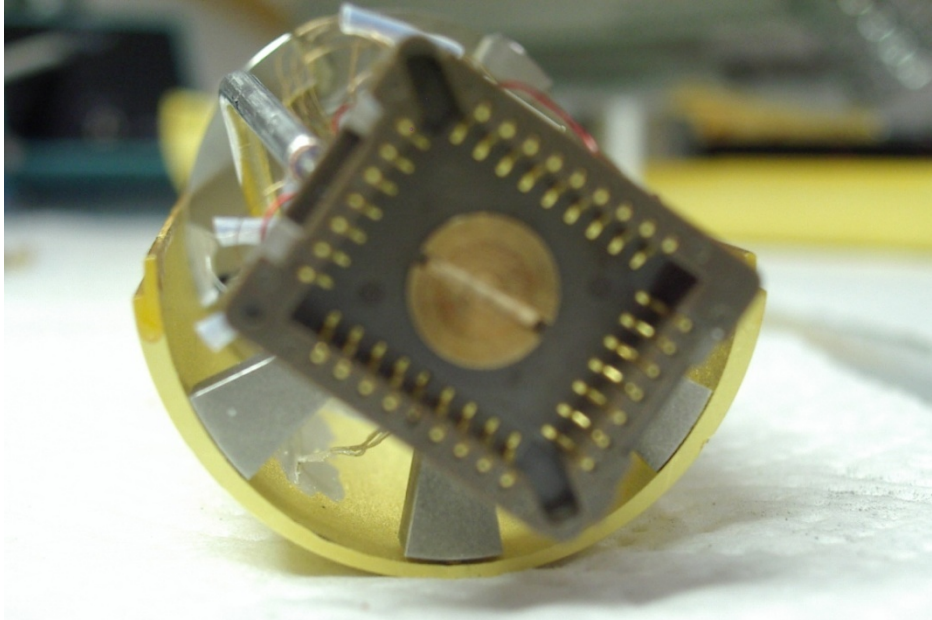
## II. Chip Socket and Carrier



Kyocera Corp.



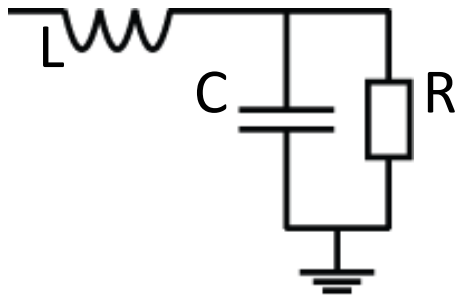
## II. Chip Socket and Carrier



Kyocera Corp.

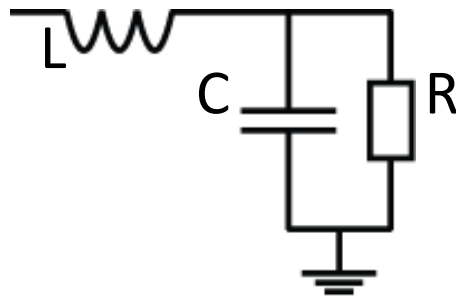
high versatility, but large stray capacitance ( $> 2 \text{ pF}$ )

# III. „Standard“ Matching Circuit



$$Z(\omega) = i\omega L + \frac{1}{1/R + i\omega C}$$

# III. „Standard“ Matching Circuit



$$Z(\omega) = i\omega L + \frac{1}{1/R + i\omega C}$$

$$\text{Matching condition: } \Gamma = \frac{Z - Z_0}{Z + Z_0} \approx 0$$

$$\text{Re}(Z) = 50 \Omega$$

$$\text{Im}(Z) = 0 \Omega$$

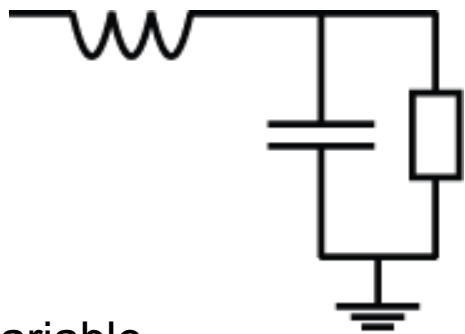
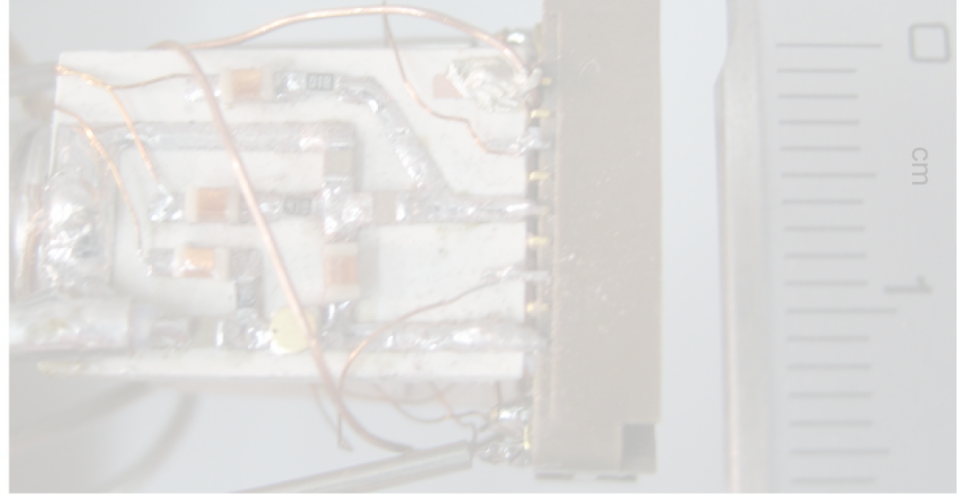
$$\text{For } \omega = 2\pi \cdot 200 \text{ MHz and } R = 30 \text{ k}\Omega$$

$$C \approx 0.65 \text{ pF}$$

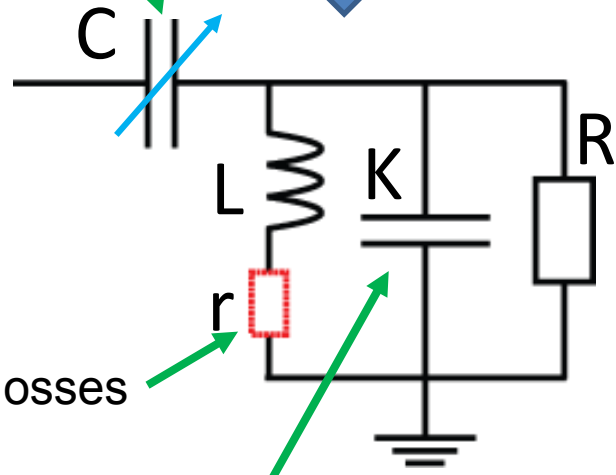
$$L \approx 1 \mu \text{ H}$$



# III. Our Circuit Design

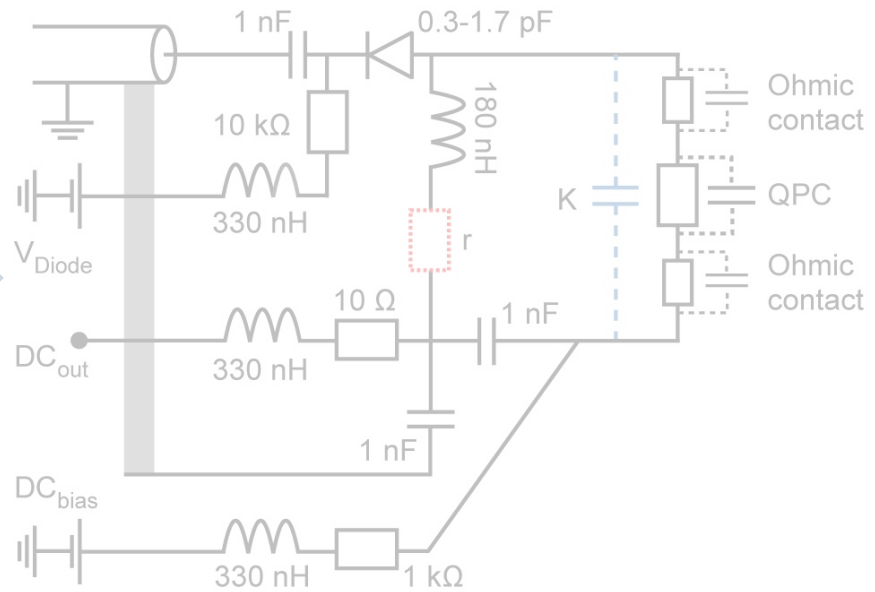
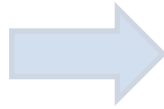


variable capacitance

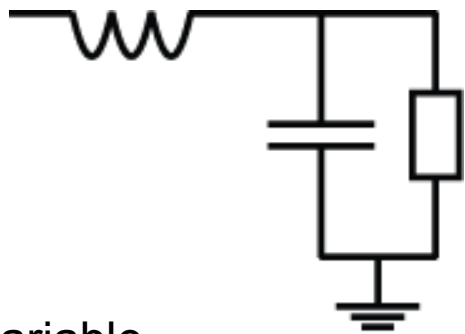
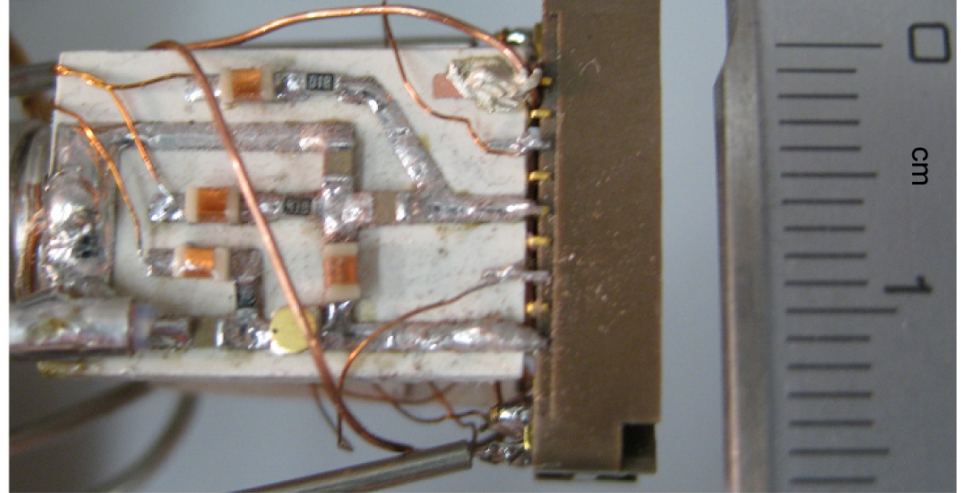


losses

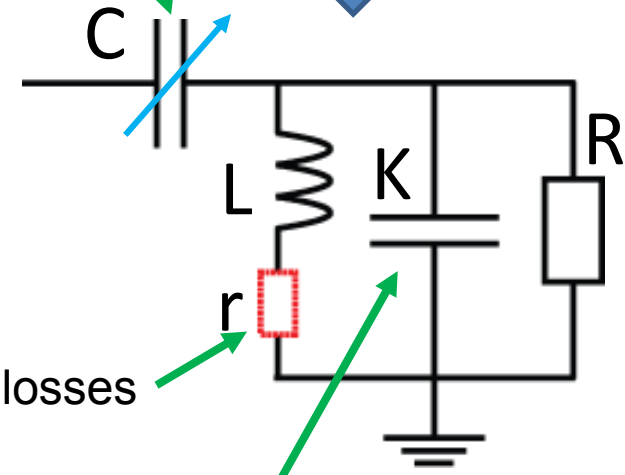
stray capacitance



# III. Our Circuit Design

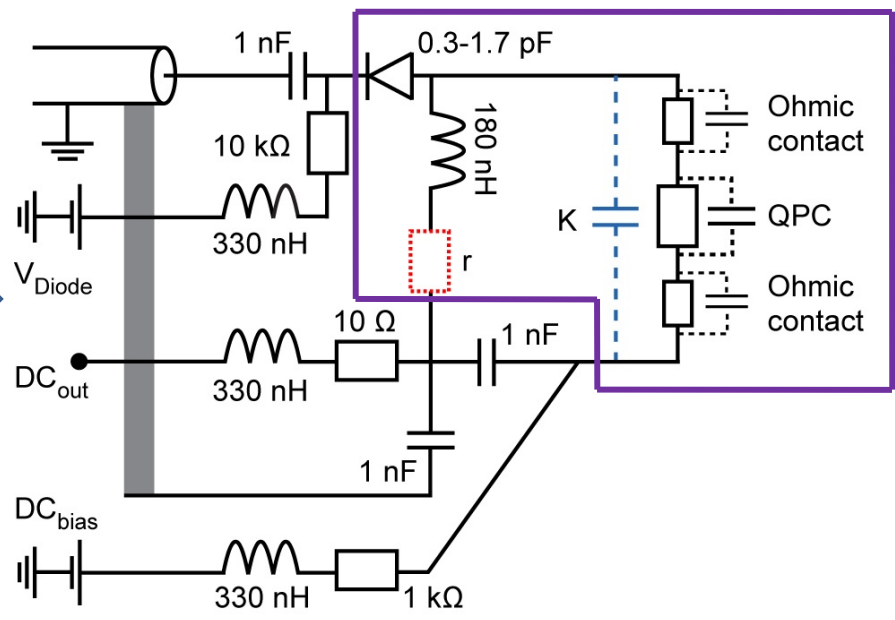
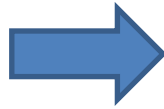


variable capacitance

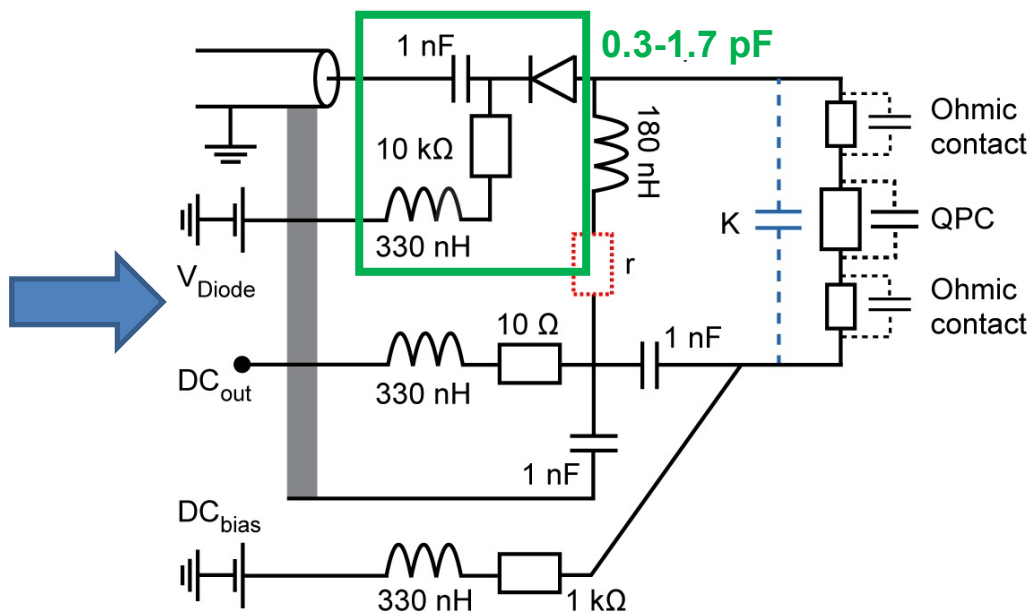
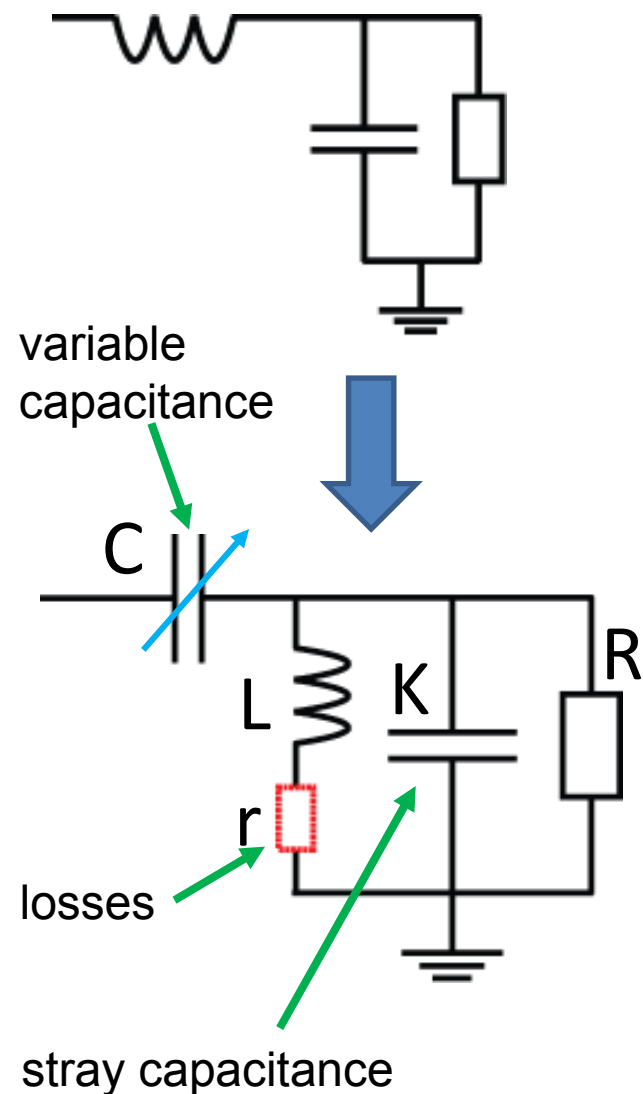
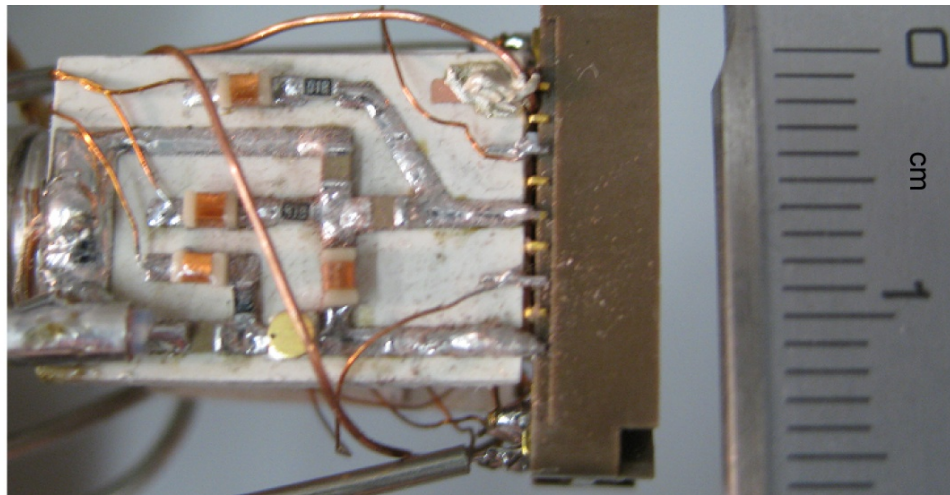


losses

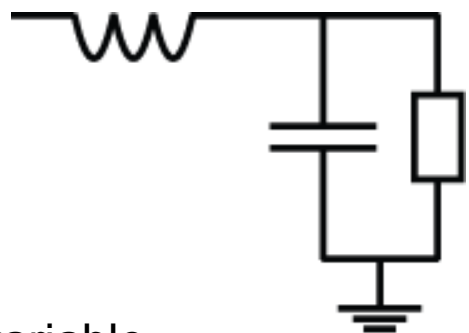
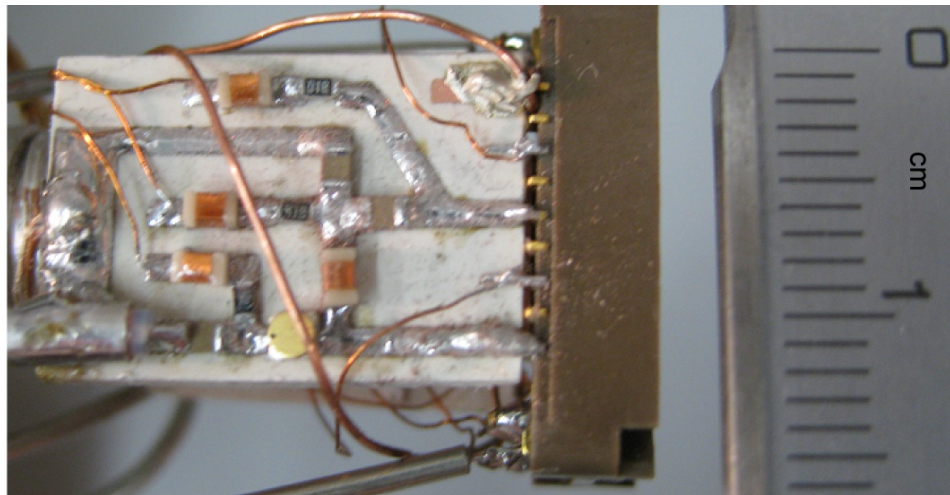
stray capacitance



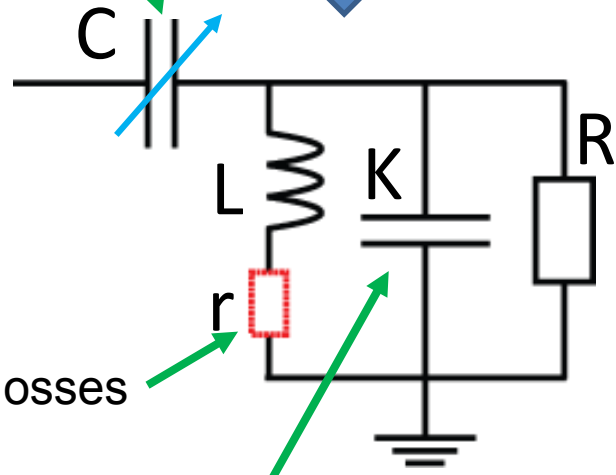
# III. Our Circuit Design



# III. Our Circuit Design

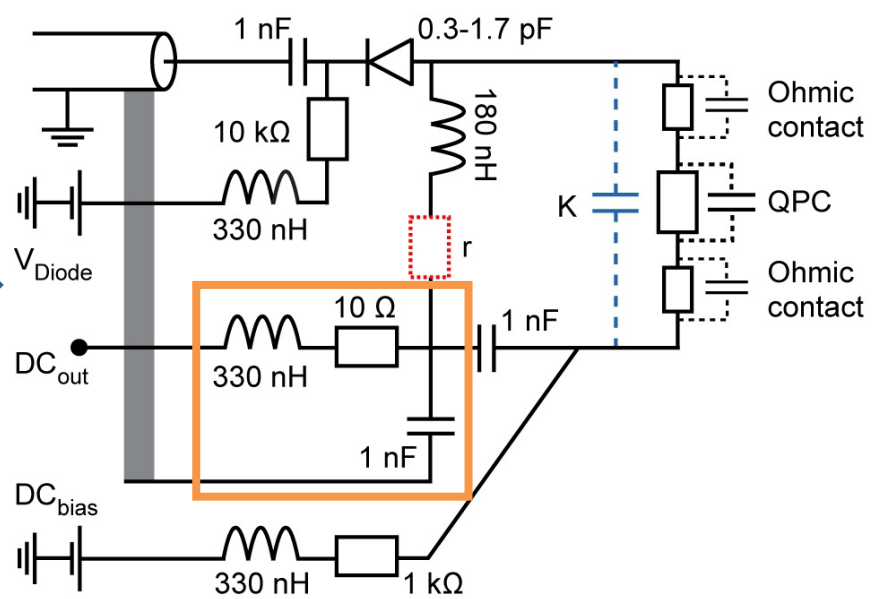


variable capacitance

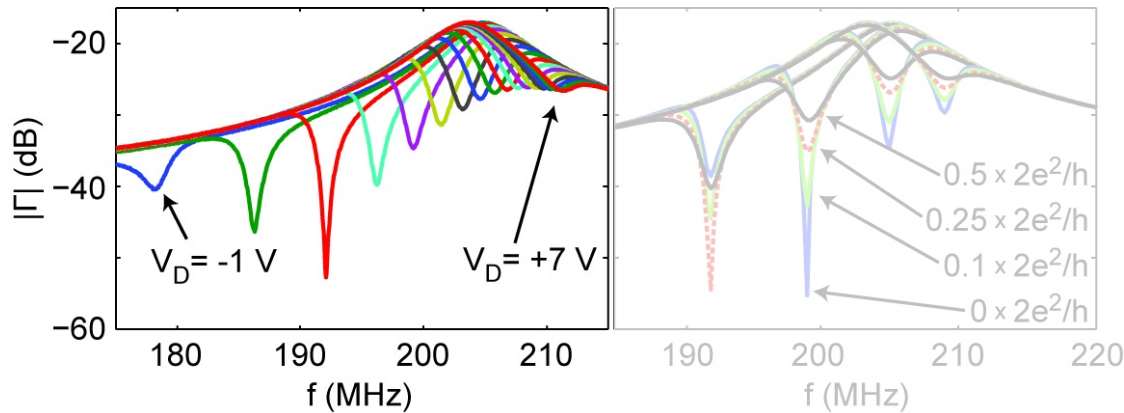


losses

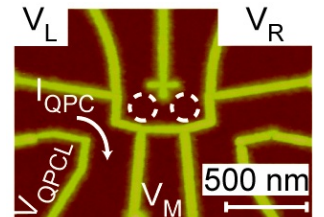
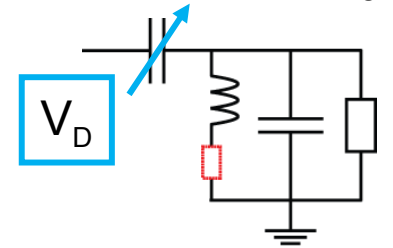
stray capacitance



# III. Experimental Realisation

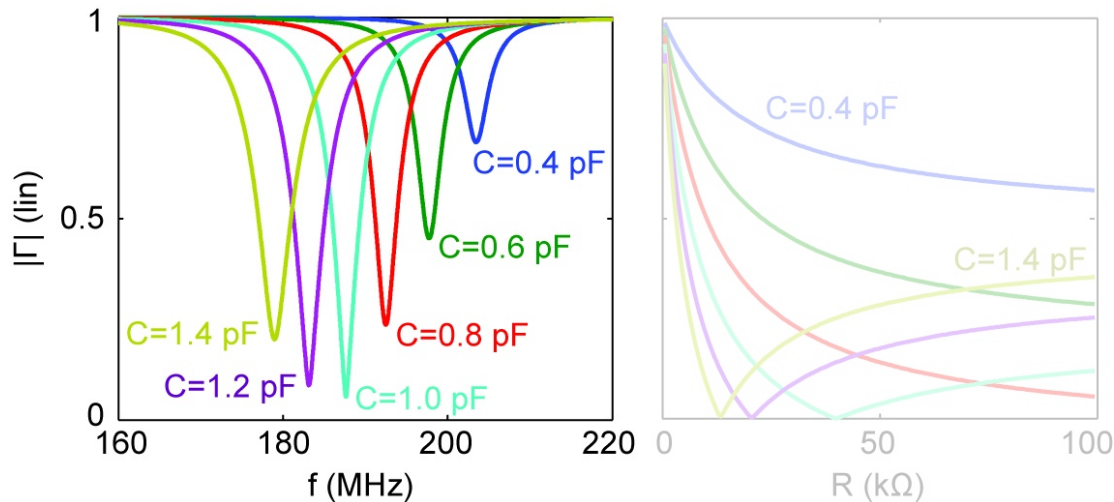


$$\Gamma = \frac{Z - Z_0}{Z + Z_0}$$



Sample processing:  
B. Küng

Calculation:



$$K = 3 \text{ pF}$$

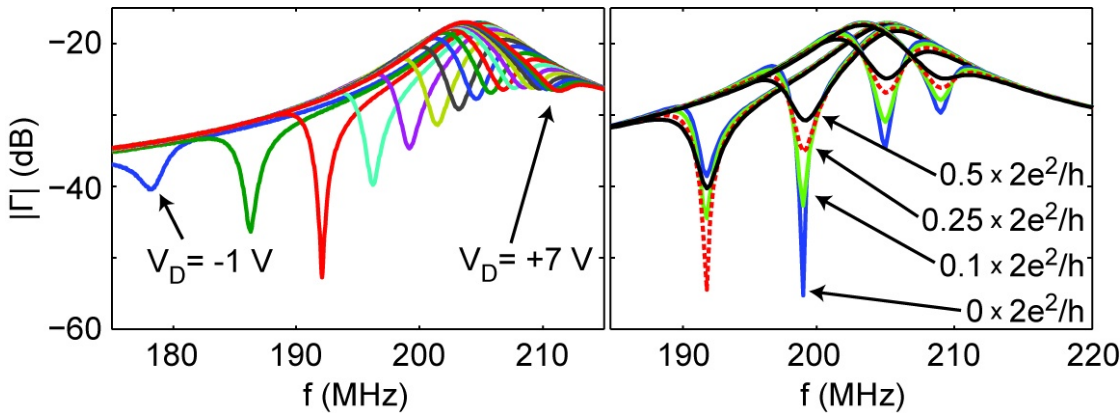
$$L = 180 \text{ nH}$$

$$r = 2 \text{ } \Omega$$

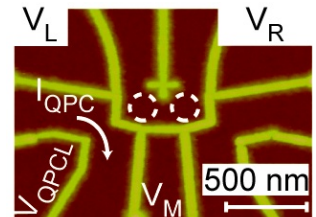
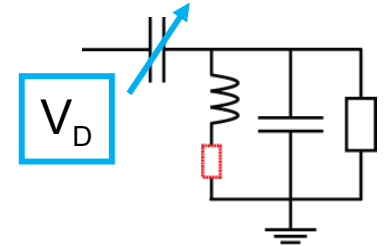
$$R = 30 \text{ k}\Omega$$

$$f_{res} \approx \frac{1}{2\pi\sqrt{L(C+K)}}$$

# III. Experimental Realisation

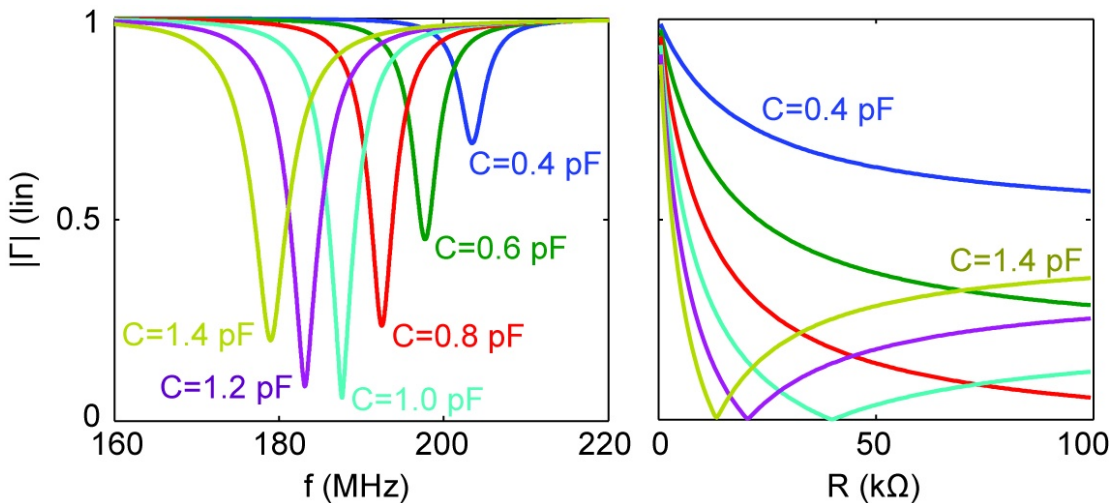


$$\Gamma = \frac{Z - Z_0}{Z + Z_0}$$



Sample processing:  
B. Küng

Calculation:



$$K = 3 \text{ pF}$$

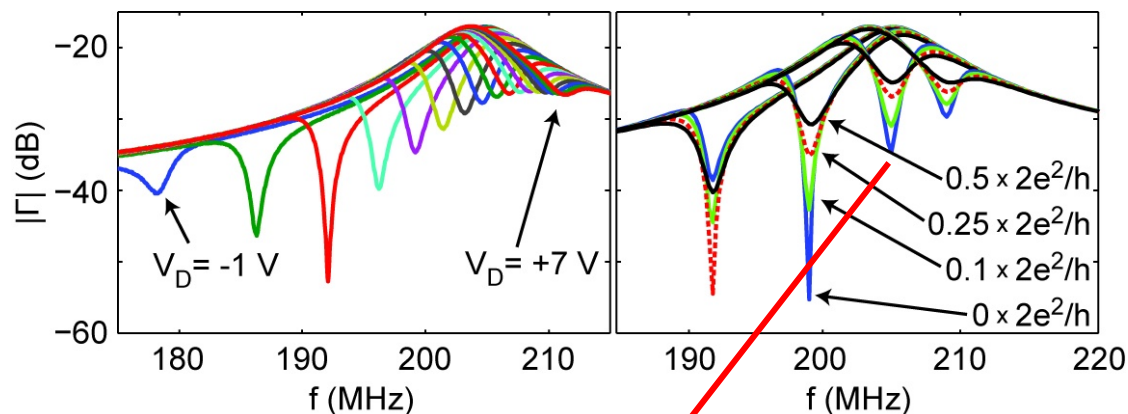
$$L = 180 \text{ nH}$$

$$r = 2 \text{ } \Omega$$

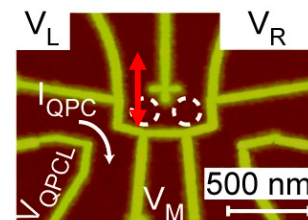
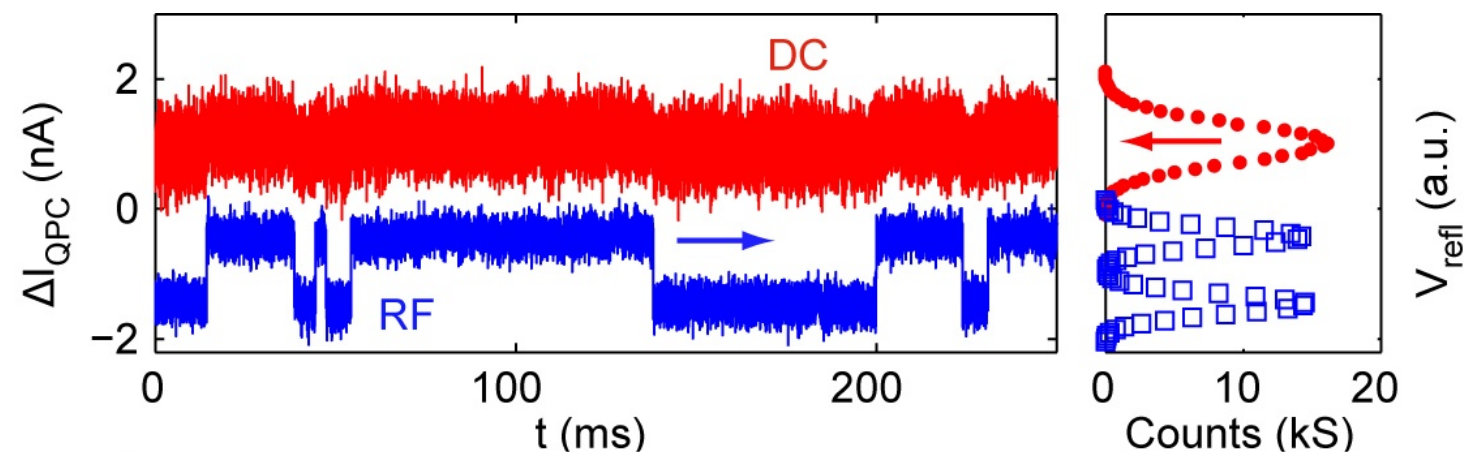
$$R = 30 \text{ k}\Omega$$

$$f_{res} \approx \frac{1}{2\pi\sqrt{L(C+K)}}$$

# III. Experimental Realisation



$$\Gamma = \frac{Z - Z_0}{Z + Z_0}$$

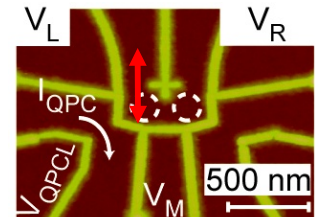
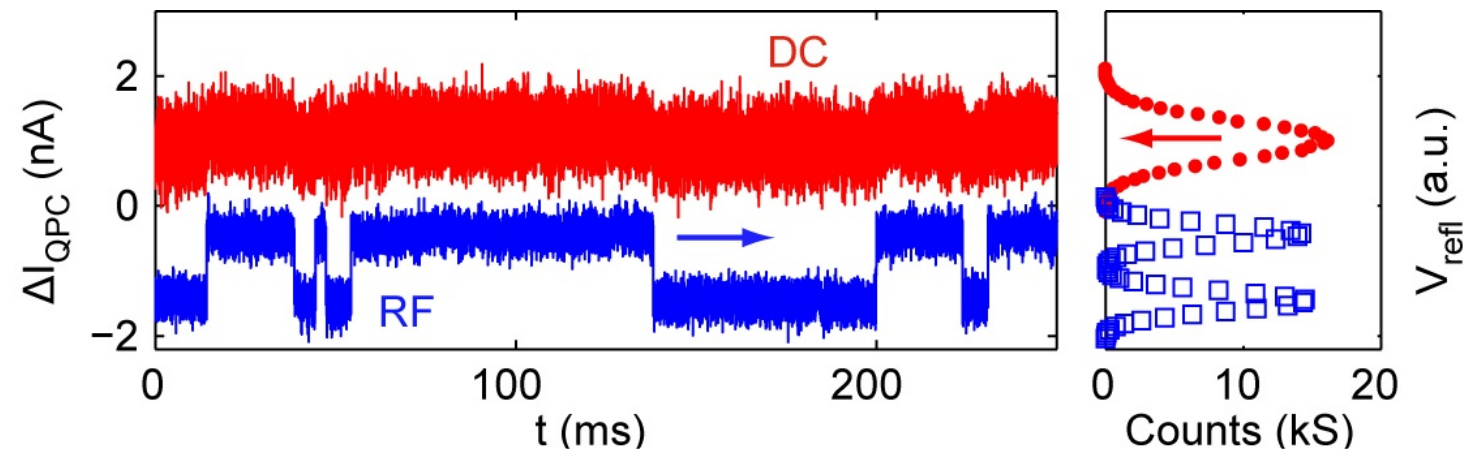
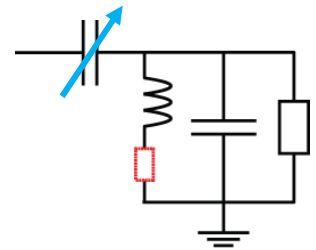


Sample processing:  
B. Küng

$T = 2$  K  
 $50$  kHz BW  
 $\Delta G = 0.01 \ 2e^2/h \rightarrow \Delta I = 300$  pA

# III. Experimental Realisation

- ✓ *In situ*-tunable rf reflectometry setup
- ✓ Performs significantly better than dc

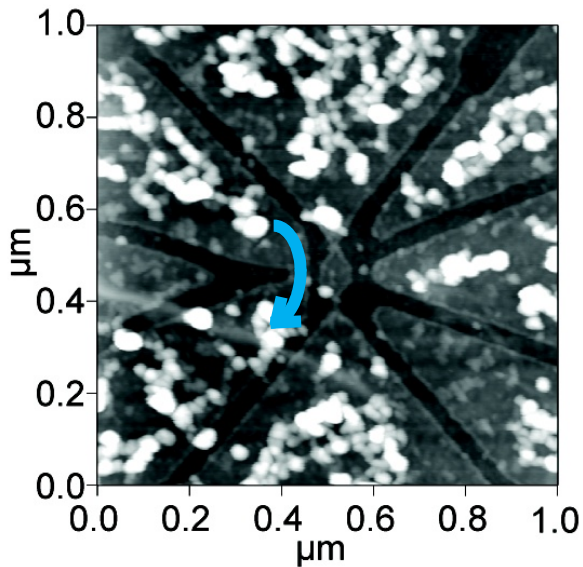


Sample processing:  
B. Küng

$T = 2 \text{ K}$   
 $50 \text{ kHz BW}$   
 $\Delta G = 0.01 \frac{2e^2}{h} \rightarrow \Delta I = 300 \text{ pA}$



# IV. Graphene QD and Charge Detector



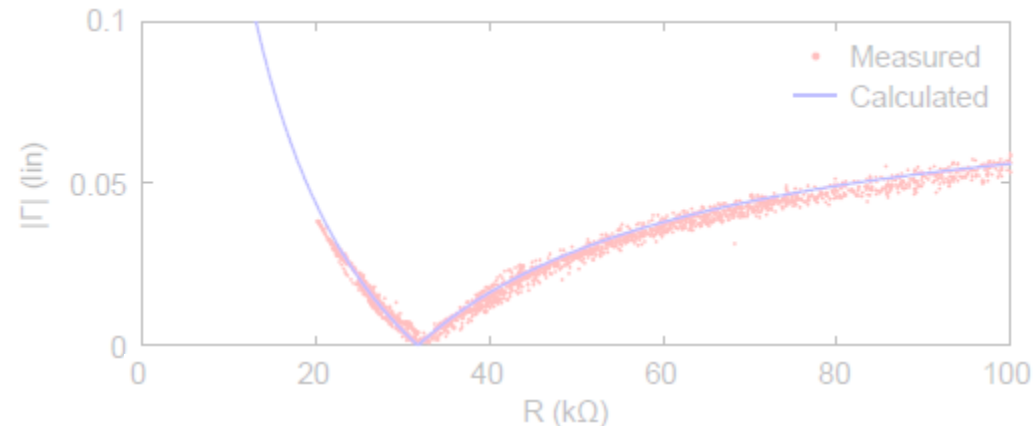
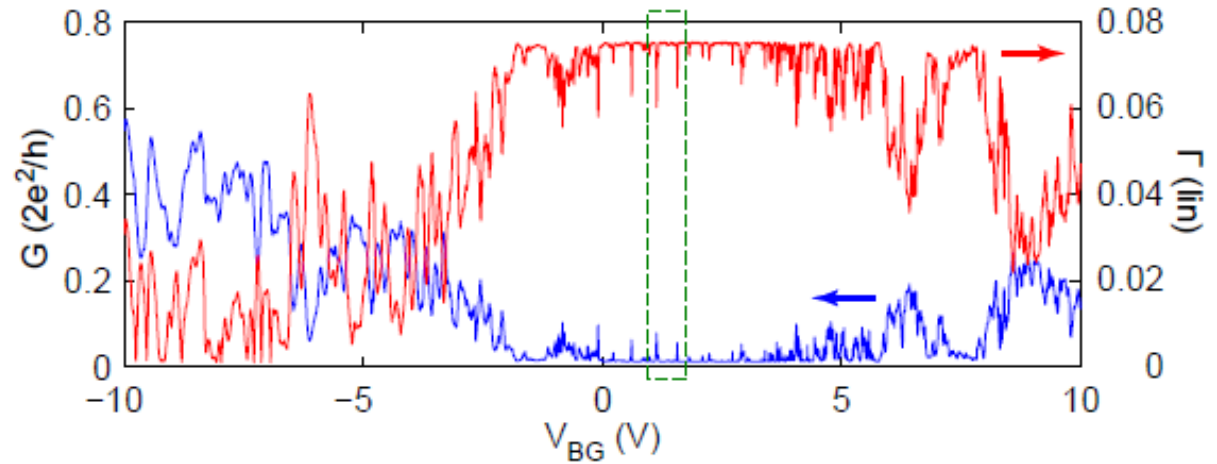
$$d_{\text{dot}} = 80 \text{ nm}$$

$$w_{\text{barrier}} \sim 25 \text{ nm}$$

$$w_{\text{constriction}} = 45 \text{ nm}$$

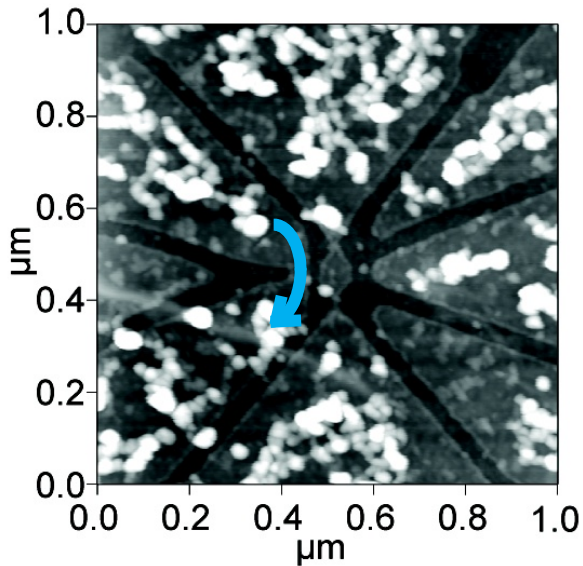
$$d_{\text{dot-constriction}} = 15 \text{ nm}$$

$$C_{\text{bondpad}} \sim 0.5 \text{ pF}$$



$$C = 1.2 \text{ pF}, K = 3.3 \text{ pF}, L = 100 \text{ nH}, \text{ and } r = 3.6 \text{ } \Omega, f = 232 \text{ MHz}$$

# IV. Graphene QD and Charge Detector



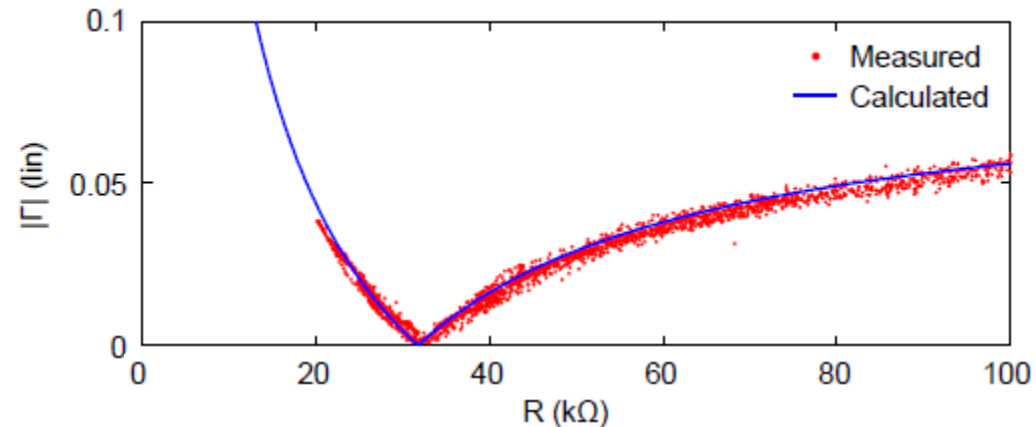
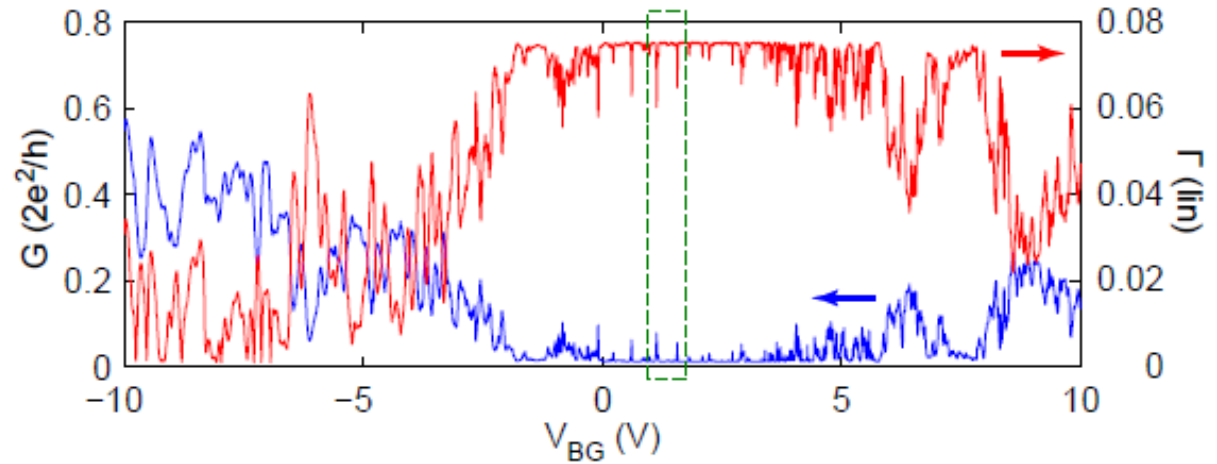
$$d_{\text{dot}} = 80 \text{ nm}$$

$$w_{\text{barrier}} \sim 25 \text{ nm}$$

$$w_{\text{constriction}} = 45 \text{ nm}$$

$$d_{\text{dot-constriction}} = 15 \text{ nm}$$

$$C_{\text{bondpad}} \sim 0.5 \text{ pF}$$

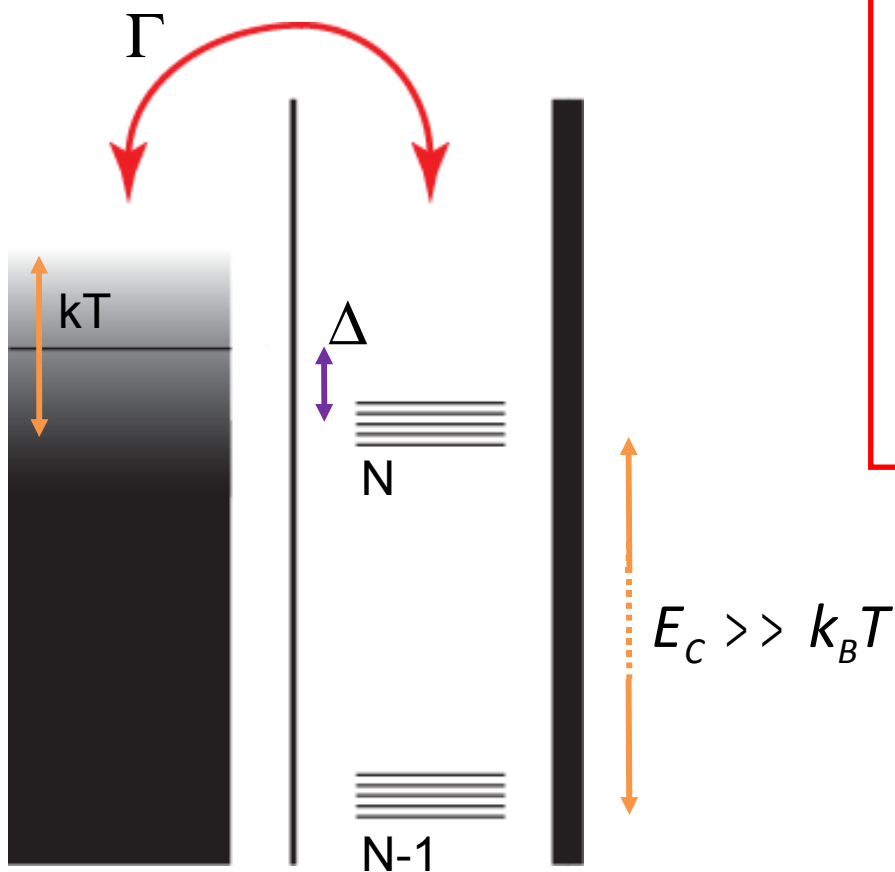


$$C = 1.2 \text{ pF}, K = 3.3 \text{ pF}, L = 100 \text{ nH}, \text{ and } r = 3.6 \text{ } \Omega, f = 232 \text{ MHz}$$

# IV. Multi-Level Tunneling to a Single Lead

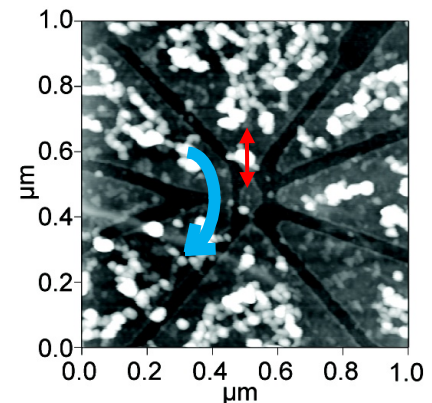
$$\Gamma_{in} = \sum_p \Gamma_p \left[ 1 - F_{eq}(E_p | N-1) \right] \cdot f(E_p + U(N) - U(N-1) - E_F)$$

Beenakker, PRB 1991

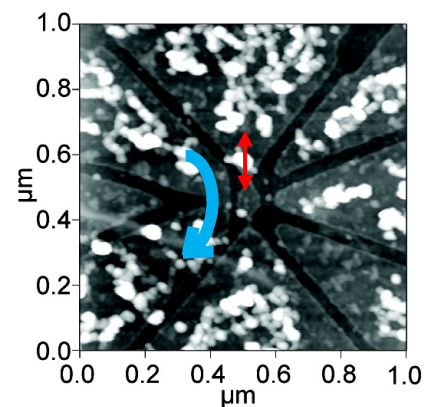
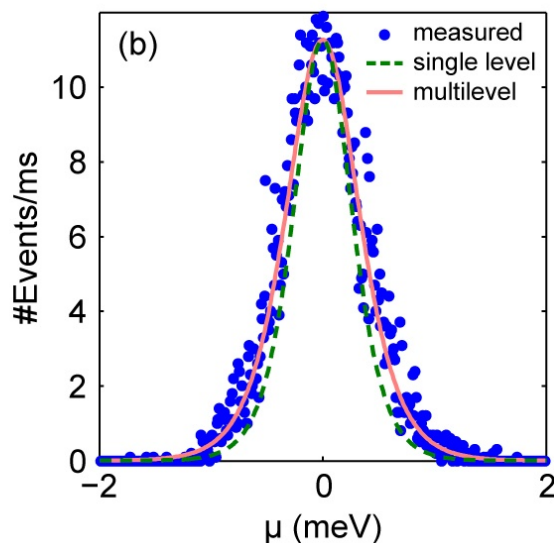
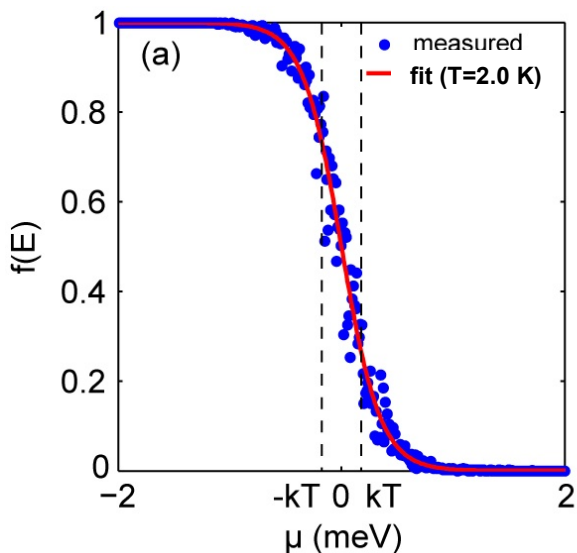


$$\Gamma_{in} \approx \rho \cdot \Gamma \cdot \frac{-\Delta}{1 - \exp(\Delta / k_B T)}$$

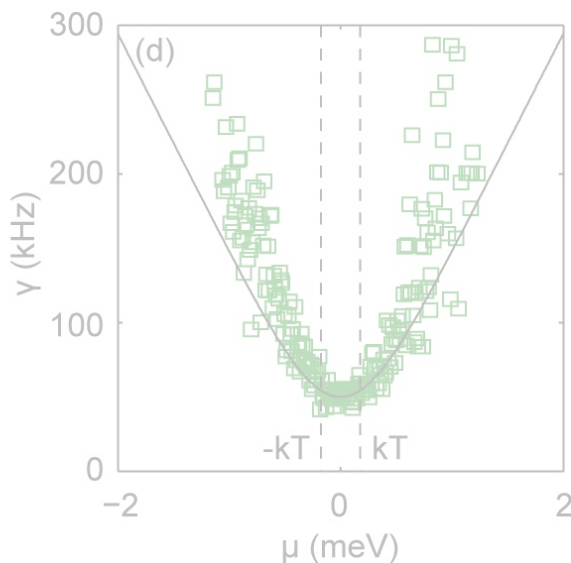
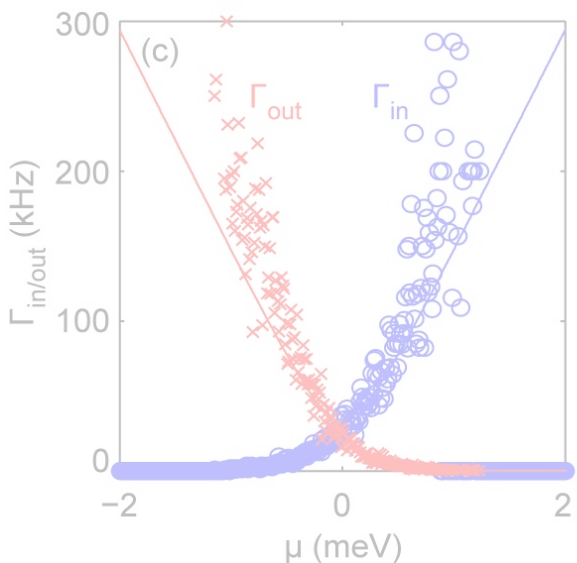
$$\Gamma_{out} \approx \rho \cdot \Gamma \cdot \frac{\Delta}{1 - \exp(-\Delta / k_B T)}$$



# IV. Measurement of Temperature



$T = 2$  K  
200 kHz BW



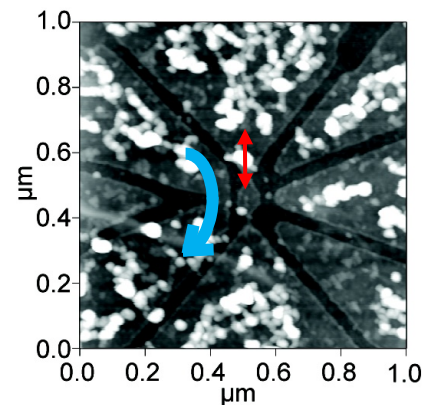
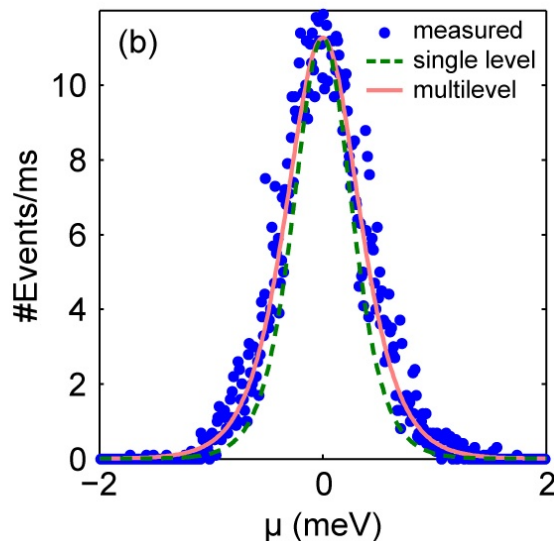
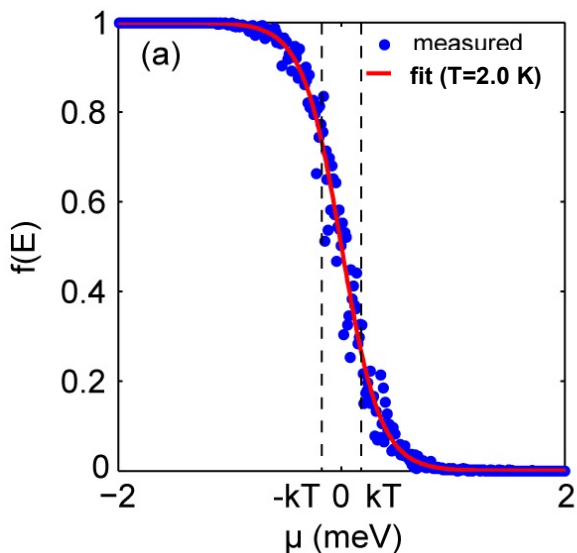
$$\Gamma_{in} \approx \rho \cdot \Gamma \cdot \frac{-\Delta}{1 - \exp(\Delta / k_B T)}$$

$$\Gamma_{out} \approx \rho \cdot \Gamma \cdot \frac{\Delta}{1 - \exp(-\Delta / k_B T)}$$

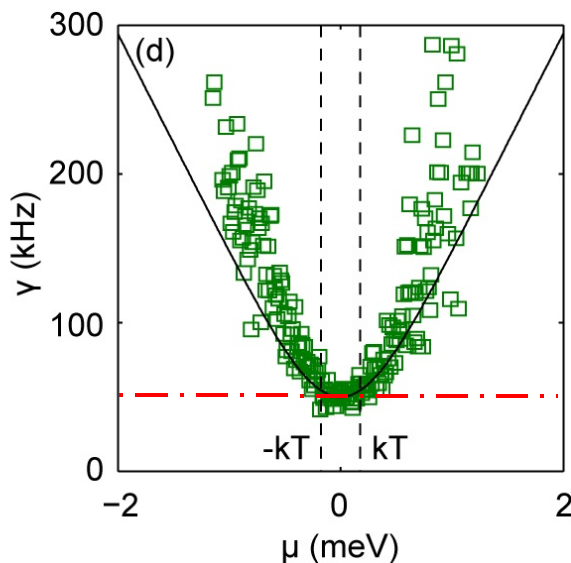
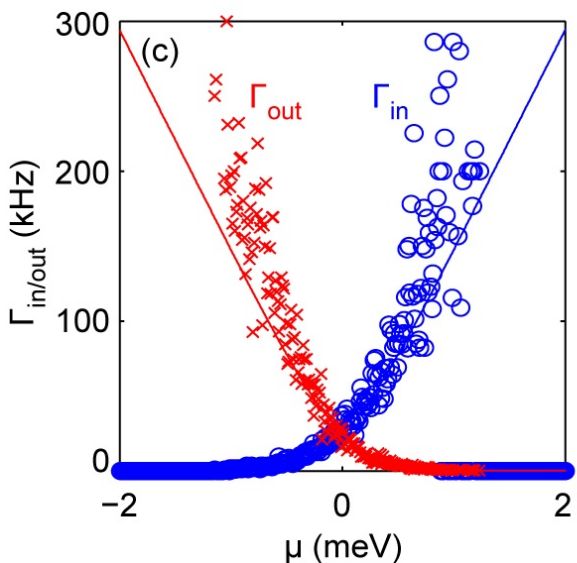
$$\Delta = -\mu$$

$$\gamma = \Gamma_{in} + \Gamma_{out}$$

# IV. Measurement of Tunnel Rates



$T = 2$  K  
200 kHz BW



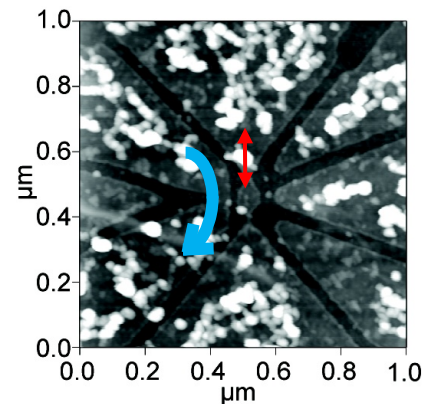
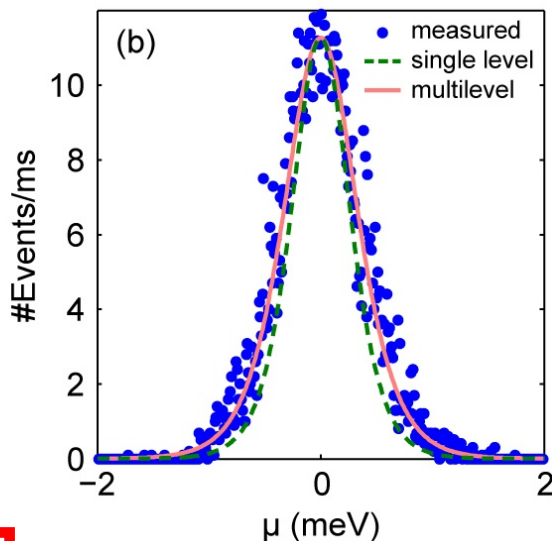
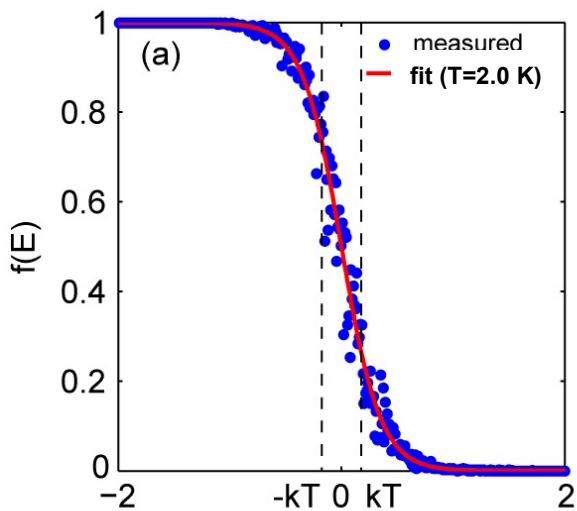
$$\Gamma_{in} \approx \rho \cdot \Gamma \cdot \frac{-\Delta}{1 - \exp(\Delta / k_B T)}$$

$$\Gamma_{out} \approx \rho \cdot \Gamma \cdot \frac{\Delta}{1 - \exp(-\Delta / k_B T)}$$

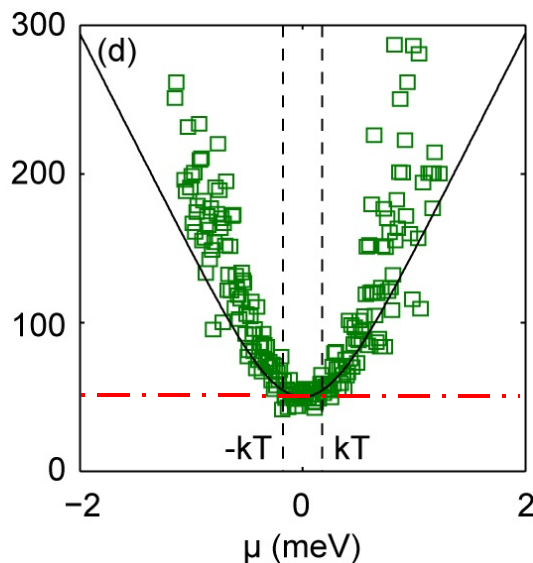
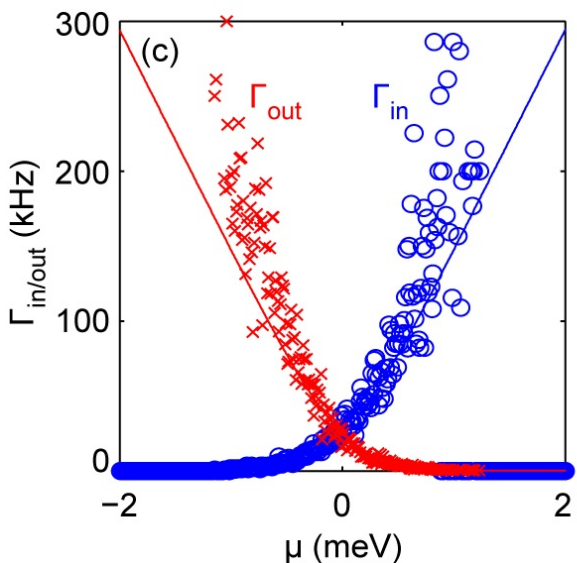
$$\Delta = -\mu$$

$$\gamma = \Gamma_{in} + \Gamma_{out}$$

# IV. Measurement of Tunnel Rates



$T = 2$  K  
200 kHz BW



$$\Gamma_{in} \approx \rho \cdot \Gamma \cdot \frac{-\Delta}{1 - \exp(\Delta / k_B T)}$$

$$\Gamma_{out} \approx \rho \cdot \Gamma \cdot \frac{\Delta}{1 - \exp(-\Delta / k_B T)}$$

$$\Delta = -\mu$$

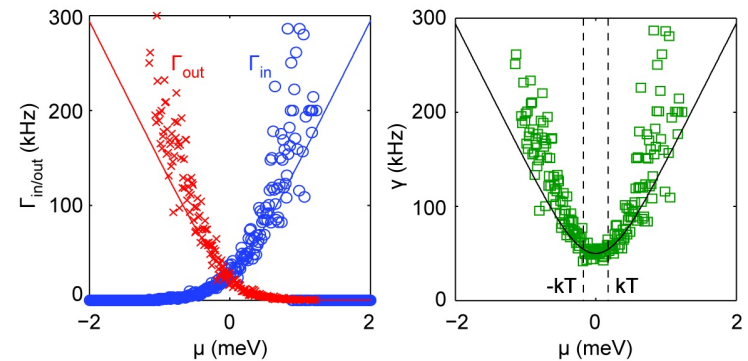
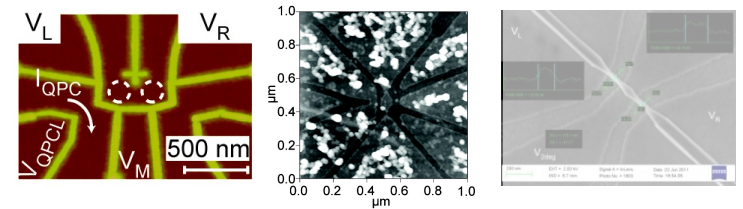
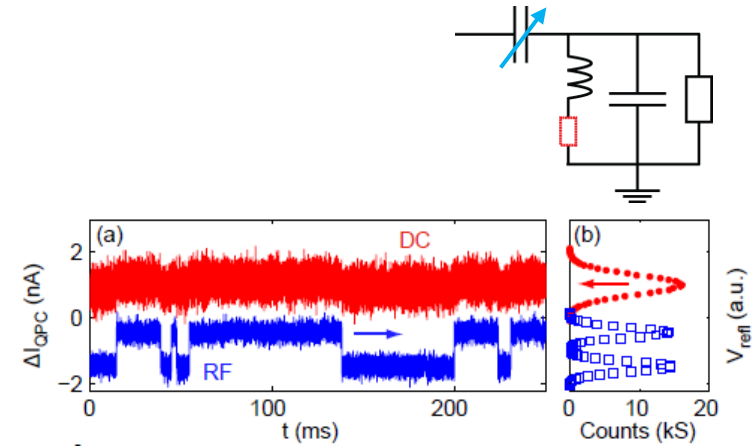
$$\gamma = \Gamma_{in} + \Gamma_{out}$$

# V. Conclusion

High-performance *in situ*-tunable matching network

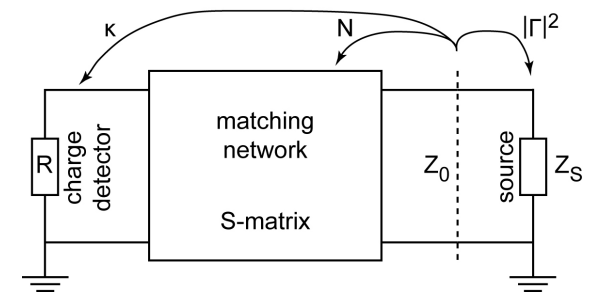
Measurements on different types of material systems

Determination of tunnel rates to a single lead in a multi-level regime

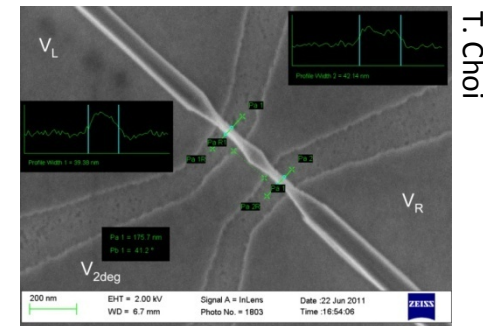
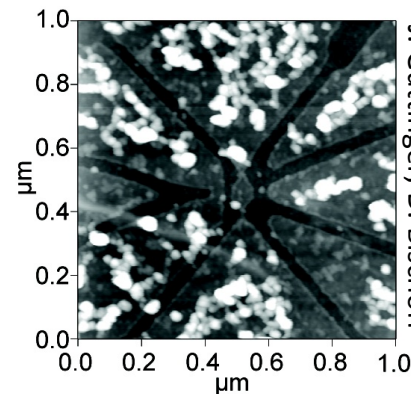
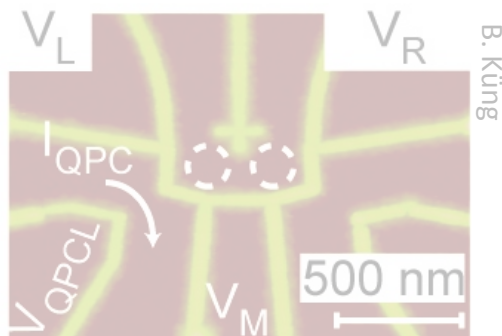


# VI. Outlook

Lower temperatures for better performance

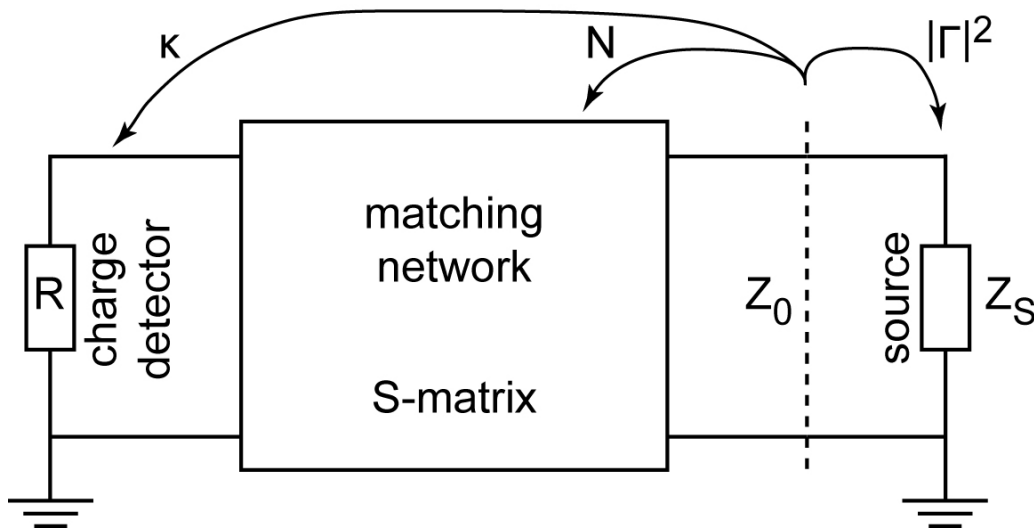


Study charge transport in „exotic“ material systems (graphene, InAs, p-GaAs)





# VII. Appendix: Power Transfer and Noise



$$T_{\Sigma} = T_N + K T_{QPC} + N T_{circ}$$

$$\approx 2 - 15K + \frac{1}{3} \cdot 2K + \frac{2}{3} \cdot 5K$$

$$\approx 6 - 20K$$

$$\Delta \Gamma = \frac{\Delta R}{R} \cdot K$$

$$\text{Signal} \propto (\Delta \Gamma \cdot V_{in})^2 \propto \frac{\Delta \Gamma^2}{K \cdot R} \propto \Delta G^2$$

# VII. Appendix – $\Delta G$

System	$\Delta G \left( \frac{2e^2}{h} \right)$
QD charge sensor on DQD	0.1 [3]
Top gate defined SQDs	0.006-0.002 [1, 13, 49, 65]
Top gate defined DQDs	0.01 [96], 0.0015 [65]
AFM defined SQDs	0.02-0.065 [29, 97]
AFM defined DQDs	0.01 [98]
Hybrid S and DDQDs	0.003 [99]
GaAs QPC underneath InAs nanowire SQD	0.065-0.12 [100, 101]
InAs nanowire DQD with self-aligned detector	0.05 [102]
Graphene SQD with nanoconstriction	0.08 [103]
Al SET on top of a top gate defined GaAs SQD	0.008 [24]
Lateral SET sensor of a SQD	0.003 [104]

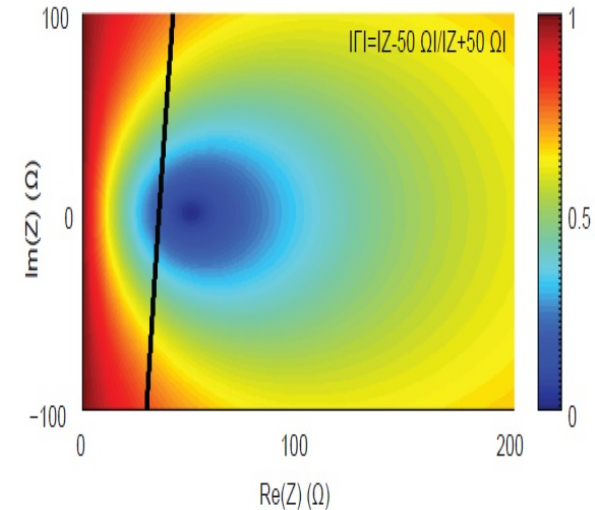
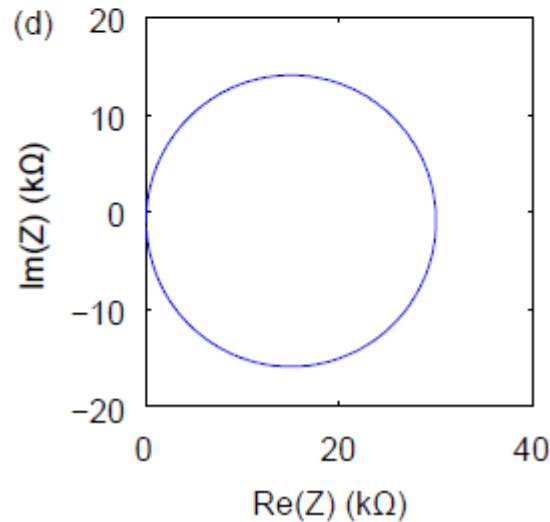
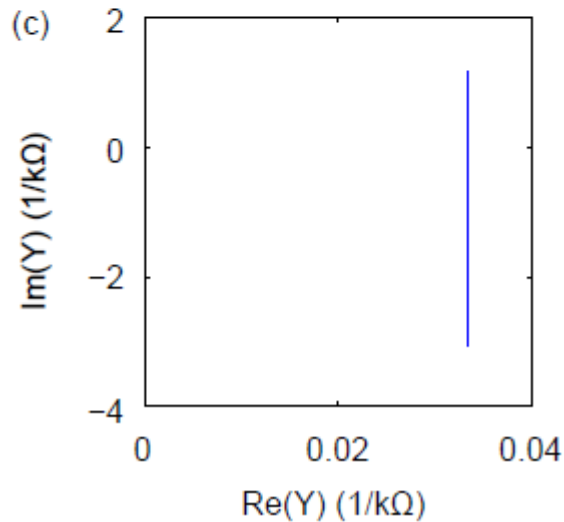
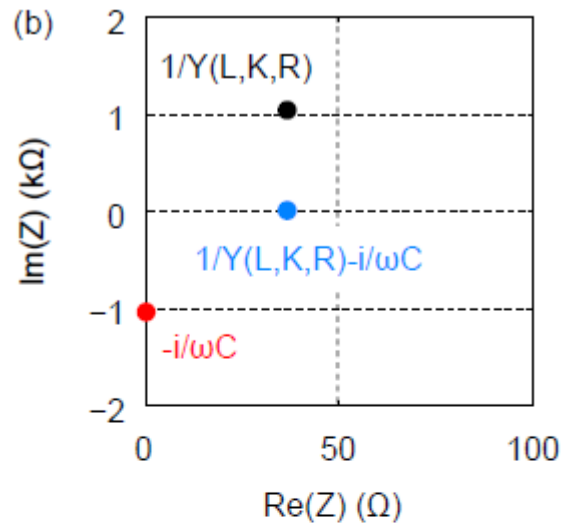
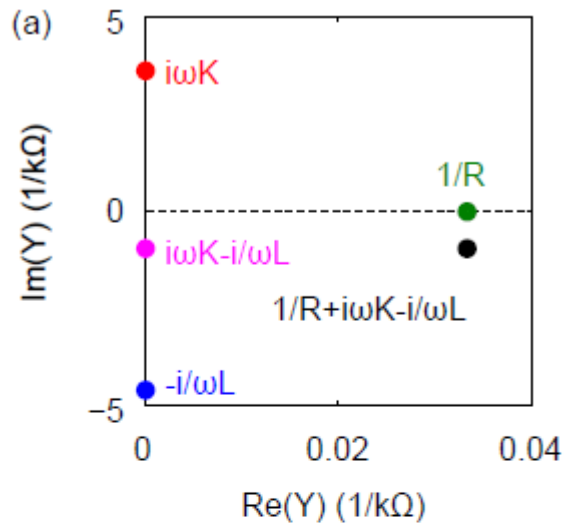
Table 2.1: Dot to charge sensor coupling for different systems as found in literature.

# VII. Appendix – rf Performance

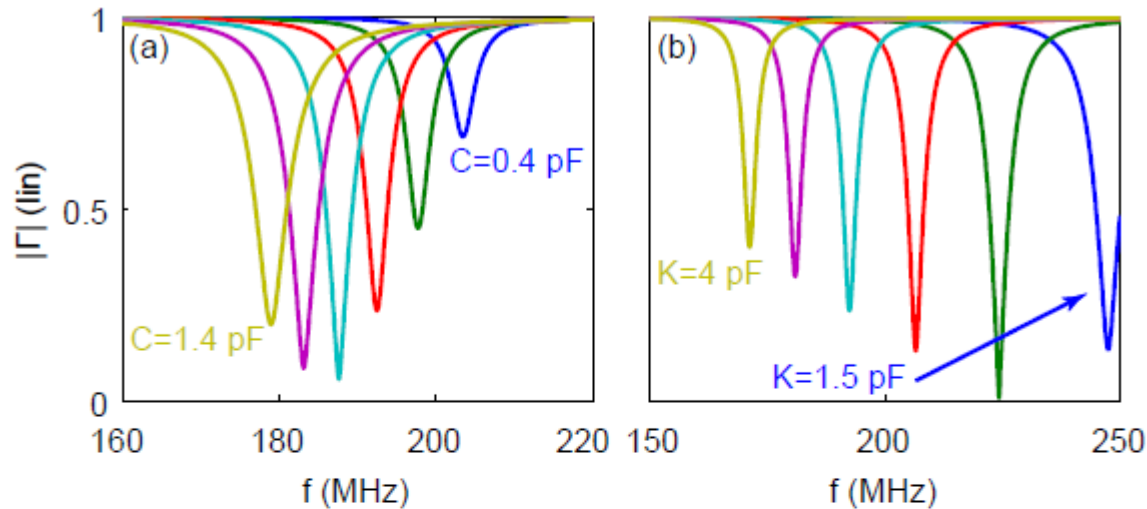
Experiment	$\delta q$ ( $e/\sqrt{\text{Hz}}$ )	$\Delta G$ ( $2e^2/h$ )	$\delta G$ ( $e^2/h\sqrt{\text{Hz}}$ )	$T_\Sigma$ (K)	BW (MHz)
Lu <i>et al.</i> [24]	$\sim 2.4 \times 10^{-4}$	0.008	$\sim 4 \times 10^{-6}$	?	?
Vink <i>et al.</i> [49]	$4.4 \times 10^{-4}$	0.006	$5.6 \times 10^{-6}$	4.3	1
Reilly <i>et al.</i> [65]	$1.6 \times 10^{-3}$	0.0015	$5 \times 10^{-6}$	$\sim 18$	8
Cassidy <i>et al.</i> [66]	$2 \times 10^{-4}$	0.025	$1 \times 10^{-5}$	$\sim 12$	21
Barthel <i>et al.</i> [3, 108], QPC	$6 - 7 \times 10^{-4}$	0.003	$4 \times 10^{-6}$	?	1.5
Barthel <i>et al.</i> [3], SQD	$2.3 \times 10^{-4}$	0.1	$4.6 \times 10^{-5}$	?	1.5
Mason <i>et al.</i> [109]	$1.5 \times 10^{-4}$	?	?	$\sim 10$	$\sim 10$
Müller <i>et al.</i> [98], GaAs	$6.3 \times 10^{-4}$	0.01	$1.3 \times 10^{-5}$	$\sim 18$	$\sim 3$
Müller <i>et al.</i> [103], Graphene	$3.2 \times 10^{-4}$	0.08	$5.1 \times 10^{-5}$	$\sim 10$	$> 3$
Müller <i>et al.</i> [101], InAs NW	$\sim 4 \times 10^{-4}$	0.12	$\sim 1 \times 10^{-4}$	6 – 7	$> 3$

Table 2.2: Charge and conductance sensitivities for fast charge-detection experiments on quantum dots. The system noise temperature  $T_\Sigma$  contains all noise contributions in the experiments. For its determination see text.

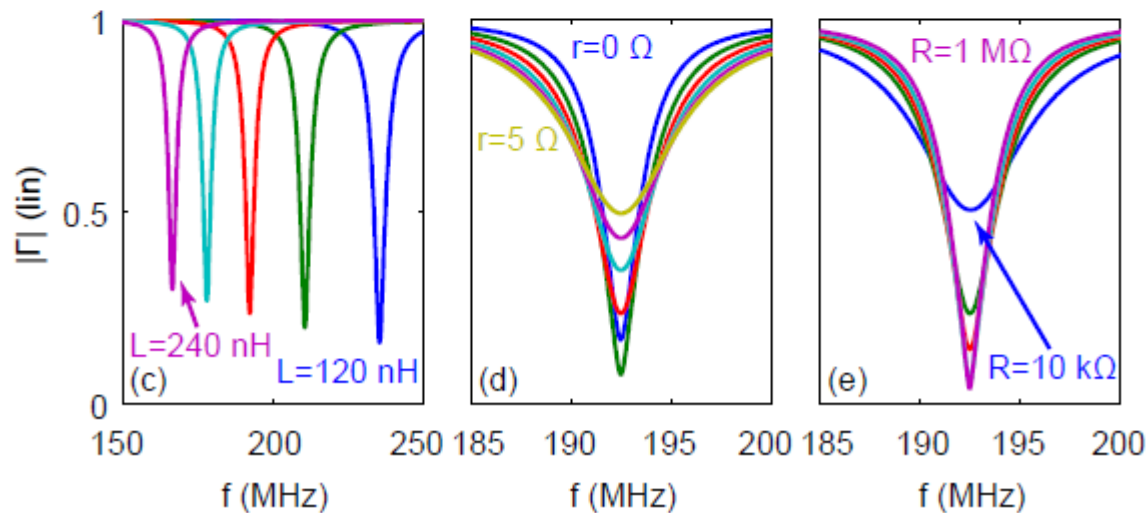
# VII. Appendix – Impedance Trafo



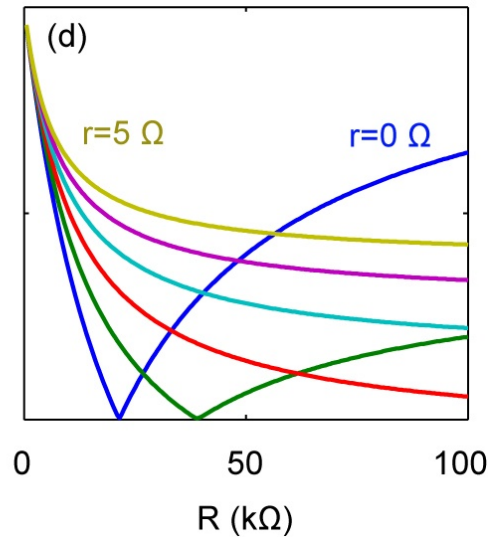
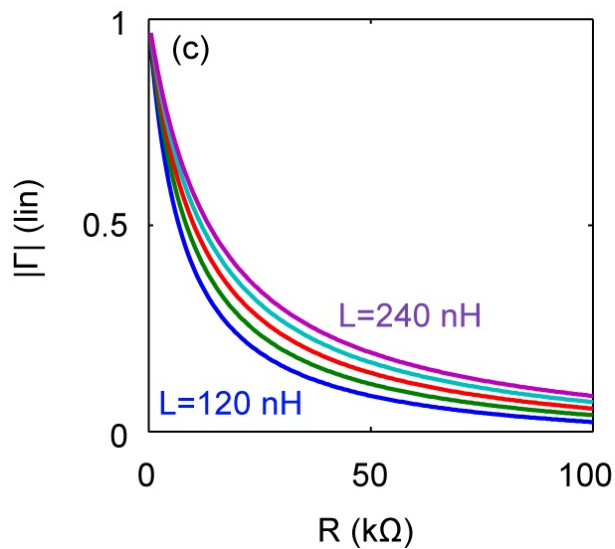
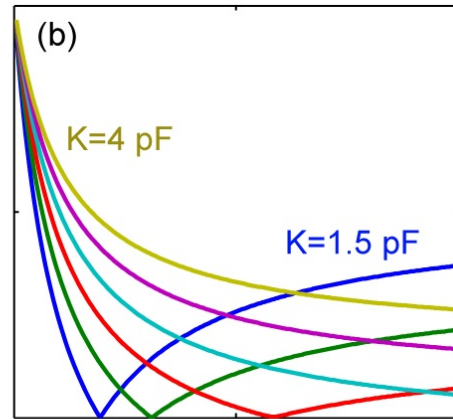
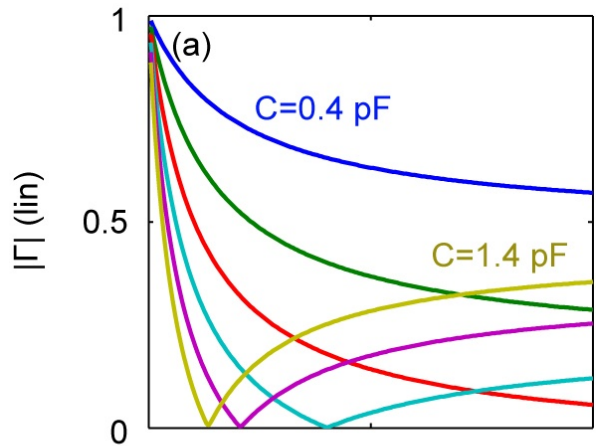
# VII. Appendix – Parameter Influence: f



$C = 0.8 \text{ pF}$   
 $K = 3 \text{ pF}$   
 $L = 180 \text{ nH}$   
 $r = 2 \text{ } \Omega$   
 $R = 30 \text{ k}\Omega$



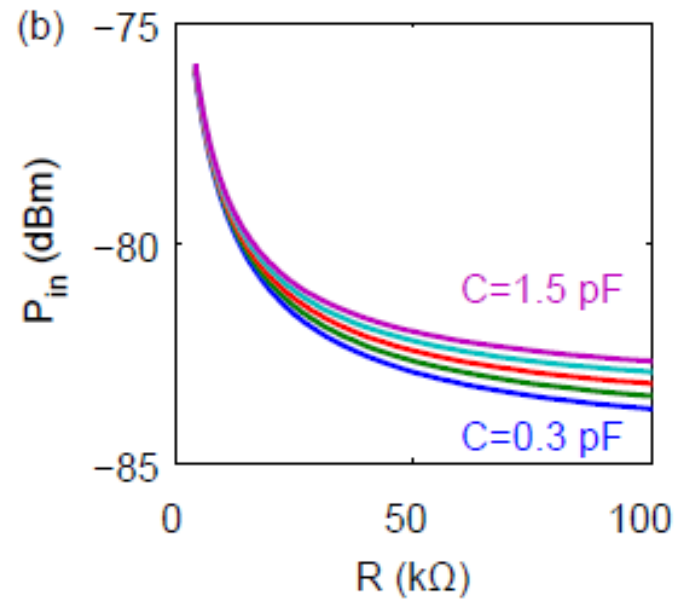
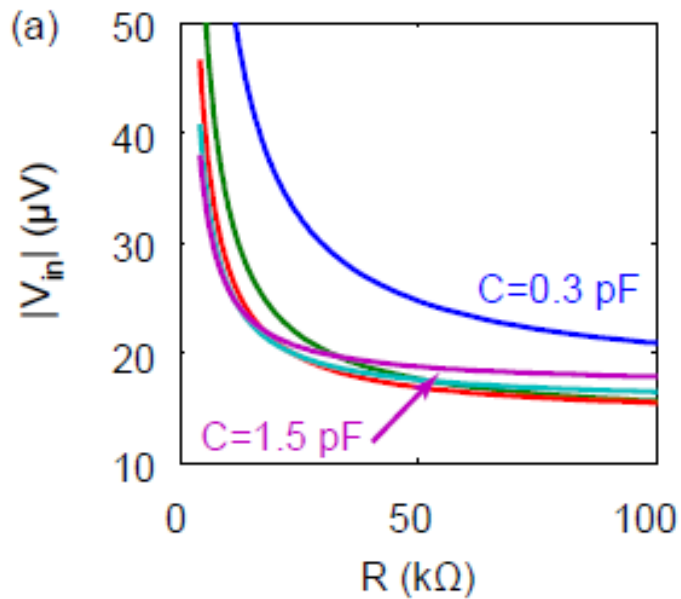
# VII. Appendix – Parameter Influence: R



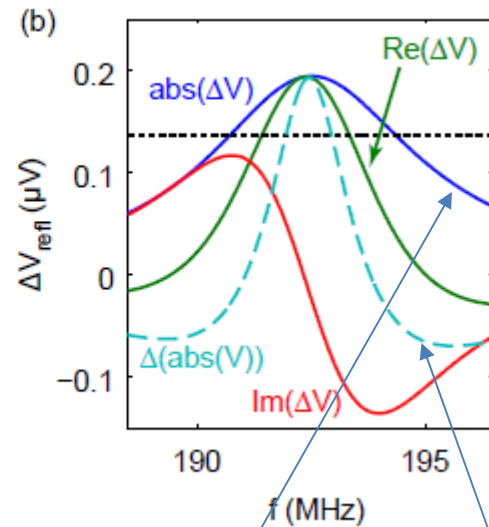
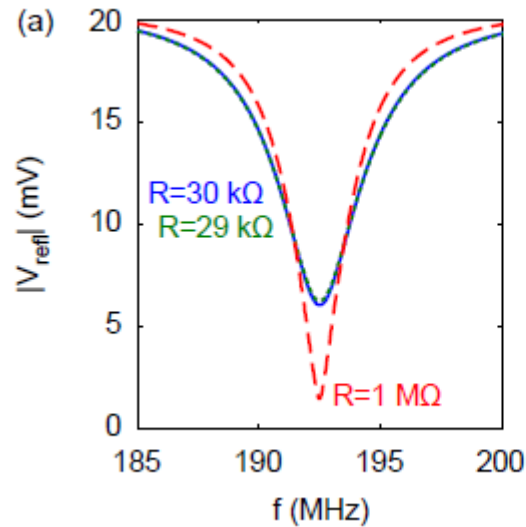
$C = 0.8$  pF  
 $K = 3$  pF  
 $L = 180$  nH  
 $r = 2$   $\Omega$

# VII. Appendix – Applicable Power

$K = 3 \text{ pF}$   
 $L = 180 \text{ nH}$   
 $r = 2 \text{ } \Omega$



# VII. Appendix: Frequency Response

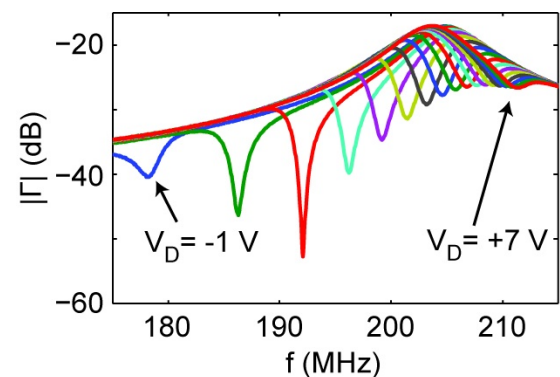
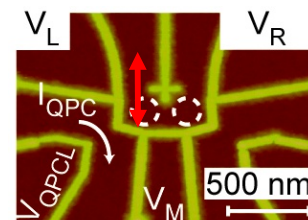
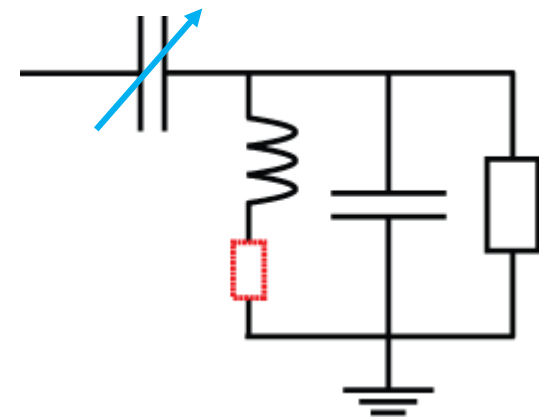
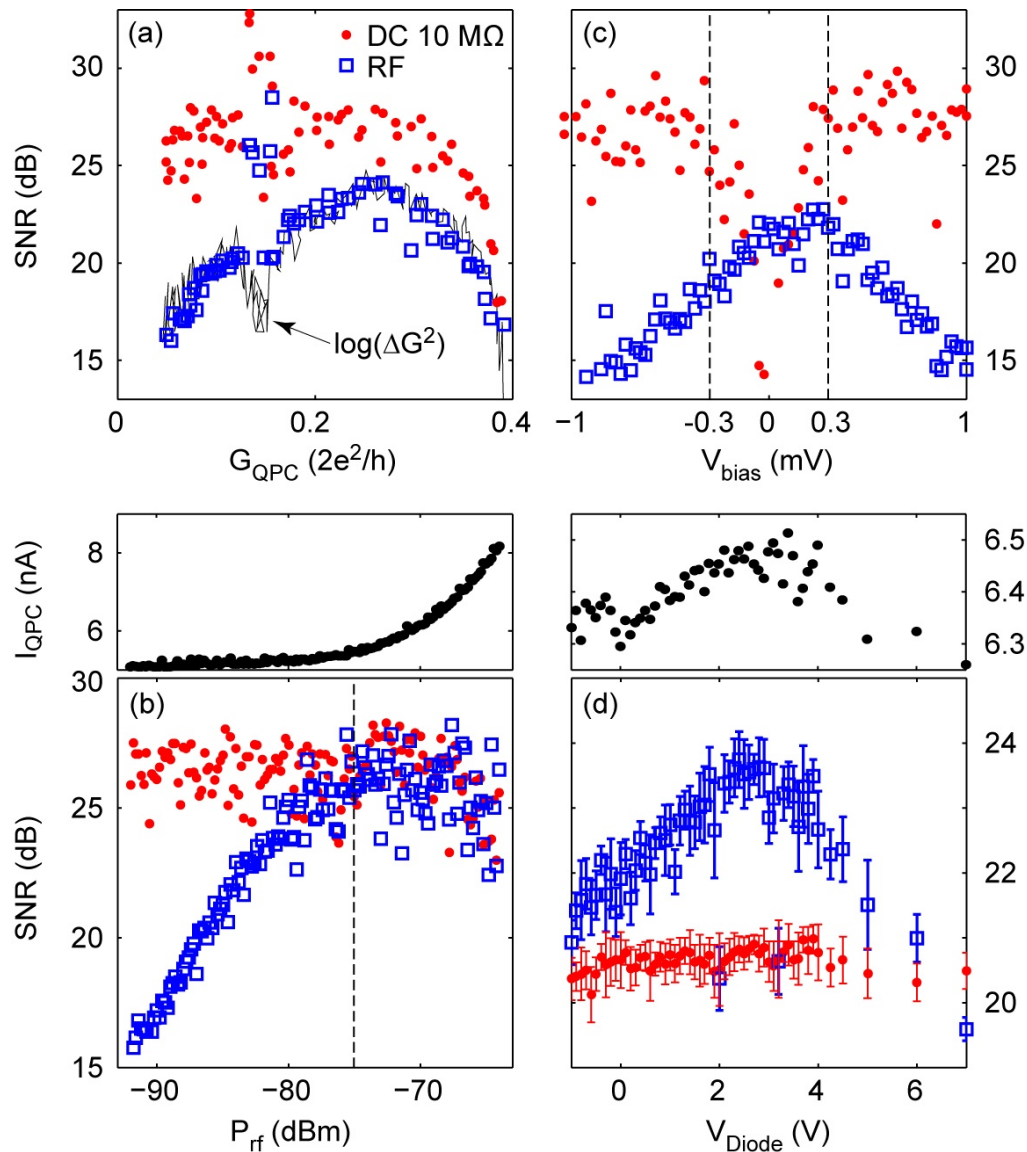


IQ-mixing

IF-mixing



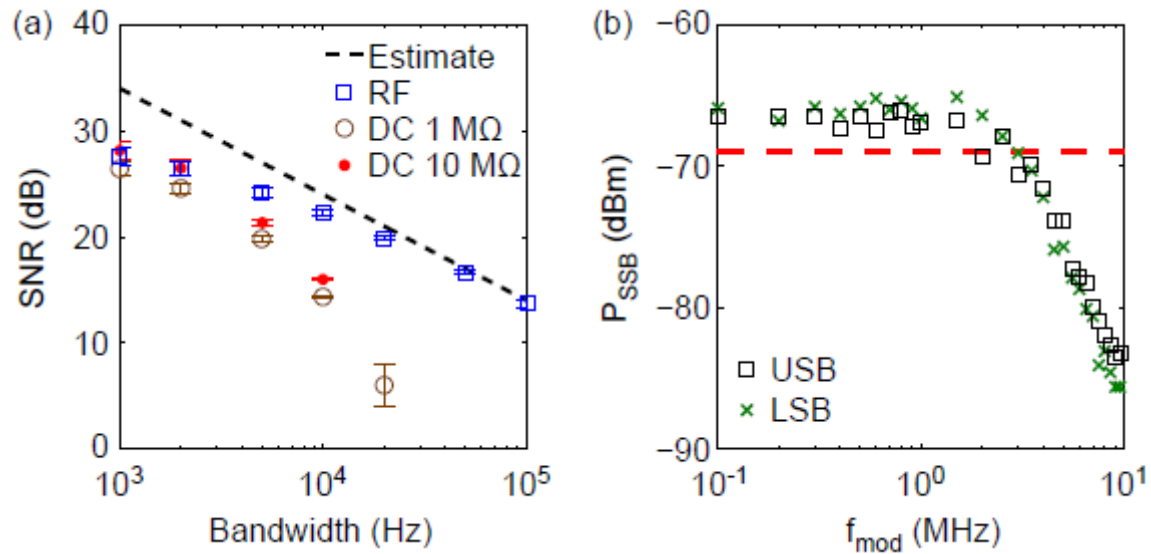
# VII. Optimization of the Tunable Circuit



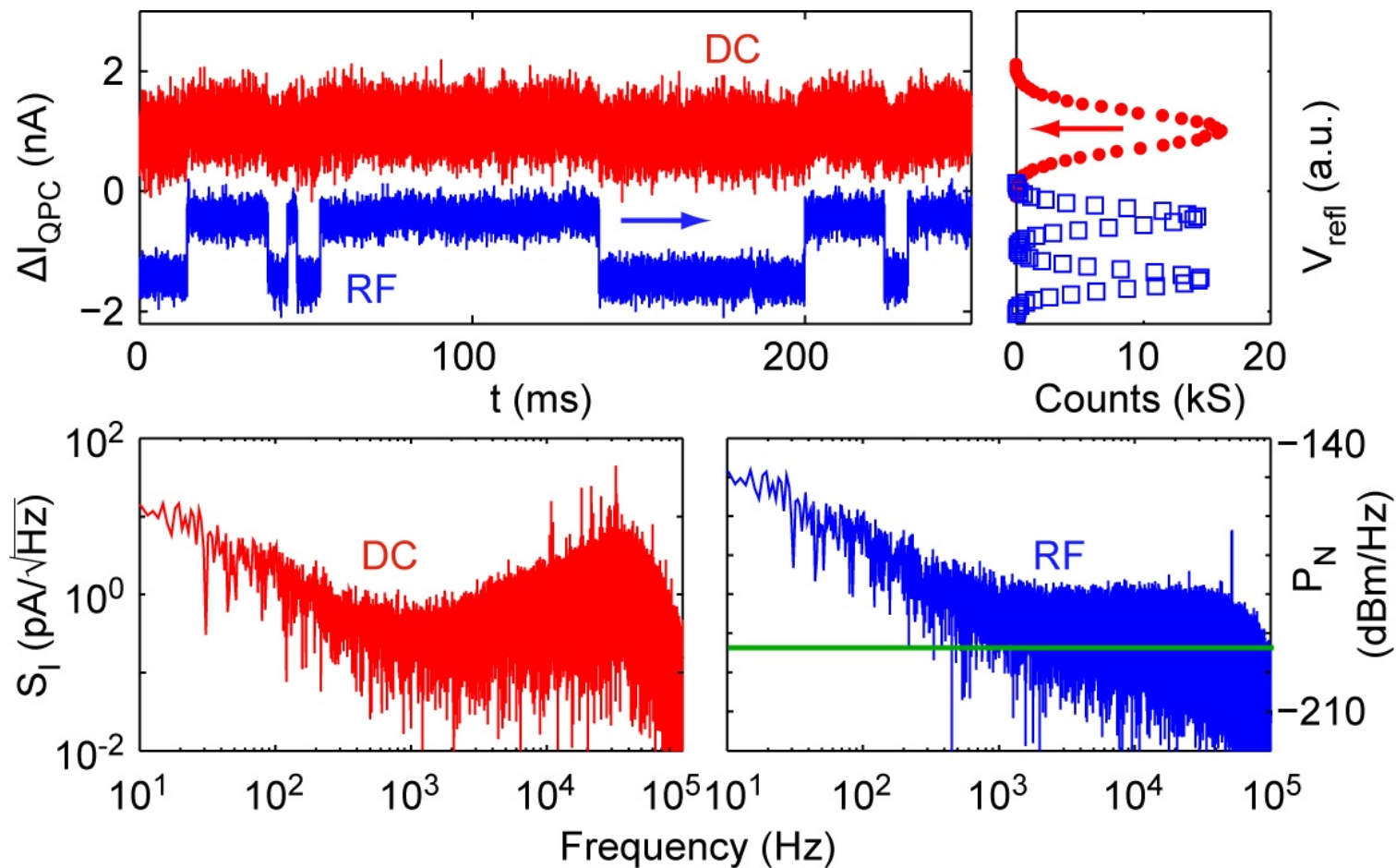
T = 2 K

1 kHz BW (a-c), 5 kHz BW (d)

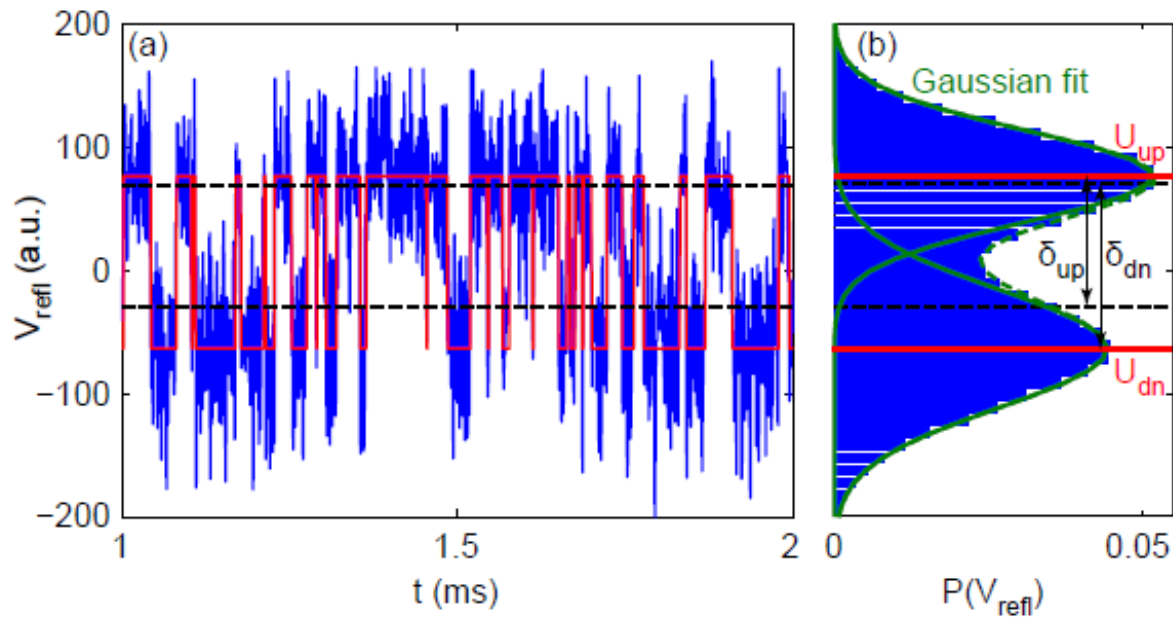
# VII. Appendix – Bandwidth



# VII. Appendix: PSD



# VII. Appendix: Counting Algorithm

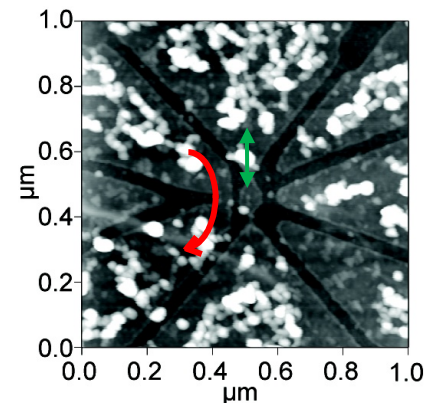


if point  $n-1$  is „up“, then

$$P_{\text{up}}(V_n) = \frac{G_{\text{up}}(V_n)}{A_{\text{up}}} \cdot \left( 1 - \frac{\Delta t}{\tau} \right)$$

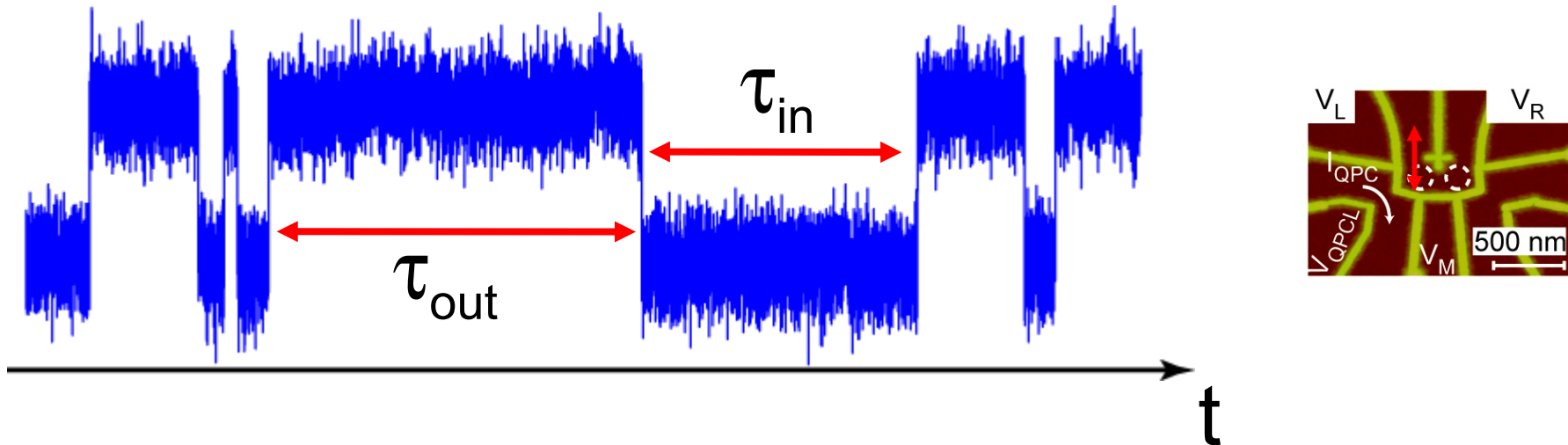
$$P_{\text{dn}}(V_n) = \frac{G_{\text{dn}}(V_n)}{A_{\text{dn}}} \cdot \frac{\Delta t}{\tau}$$

$T = 2 \text{ K}$   
 $800 \text{ kHz BW}$



Algorithm: Yuzhelevski *et al.*, RSI 2000

# Interlude: Extraction of Tunnel Rates



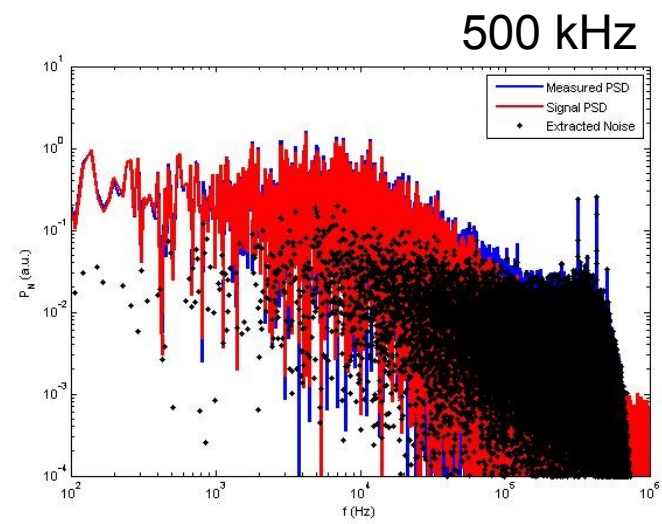
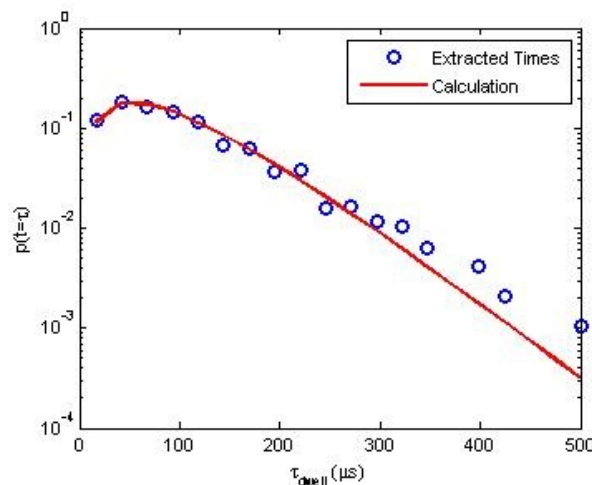
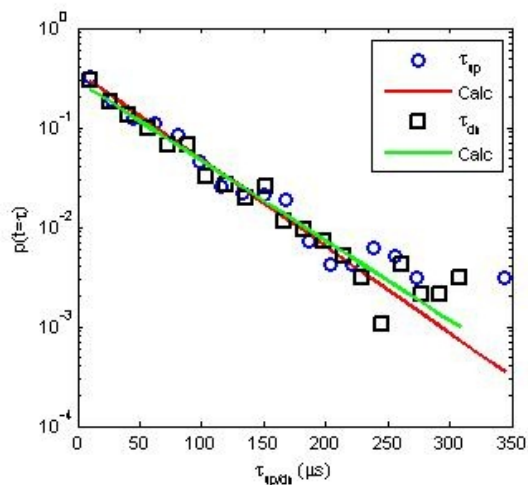
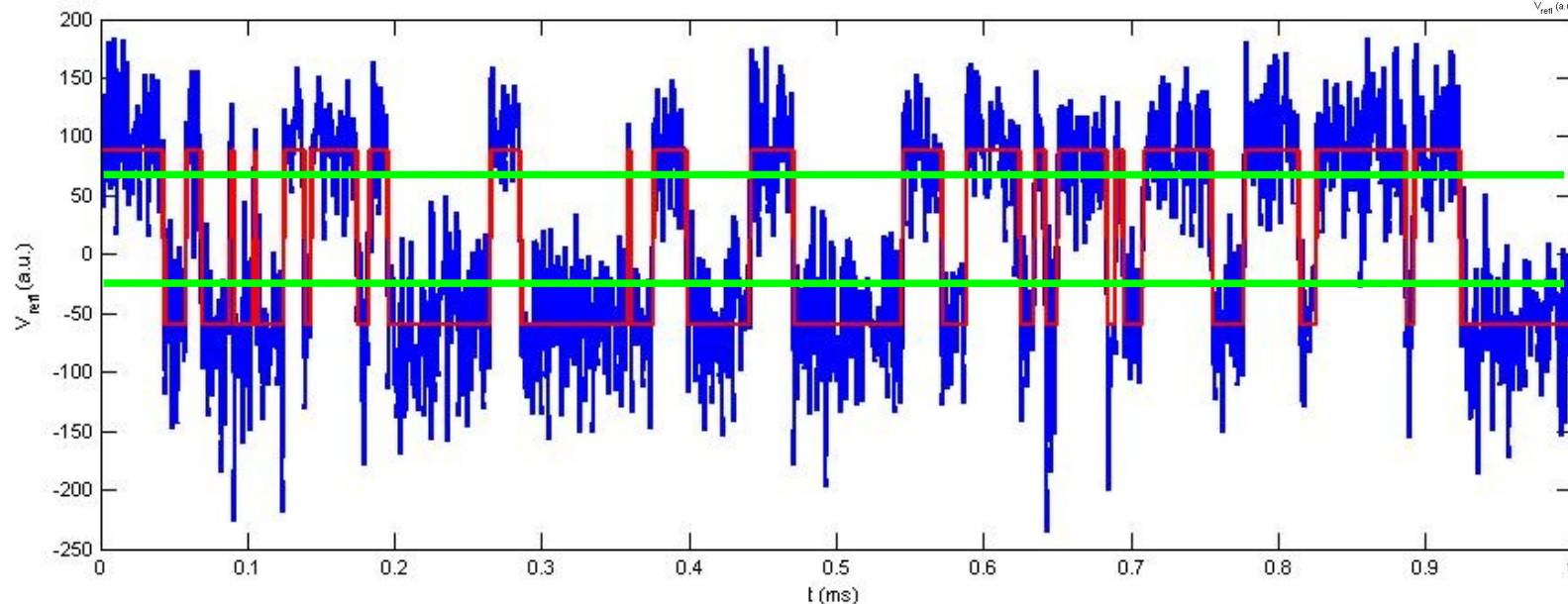
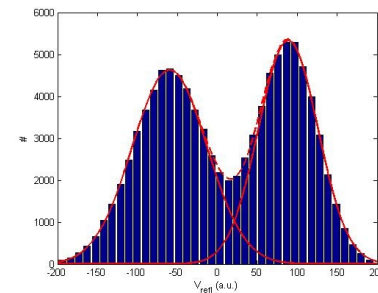
$$\Gamma_{in} = 1/\langle\tau_{out}\rangle$$

$$\Gamma_{out} = 1/\langle\tau_{in}\rangle$$

$$\gamma = \Gamma_{in} + \Gamma_{out} = 1/\langle\tau_{in}\rangle + 1/\langle\tau_{out}\rangle$$

$$\tau = 1/\Gamma_{in} + 1/\Gamma_{out} = \langle\tau_{in}\rangle + \langle\tau_{out}\rangle = 1/r_E$$

# VII. Appendix: Extraction of Parameters

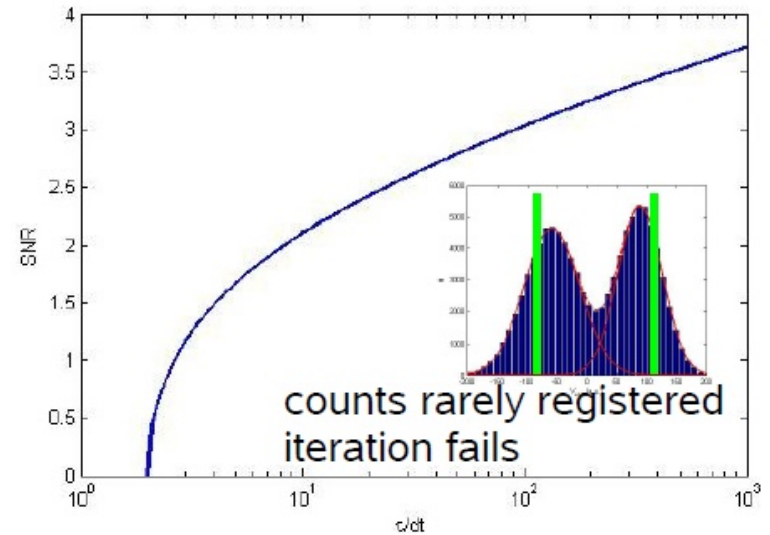


# VII. Appendix – Algorithm Limitations

## Signal to noise ratio

$$\frac{\Delta V}{\sigma} \geq \sqrt{2 \ln\left(\frac{\tau}{\Delta t} - 1\right)}.$$

thresholds have to be closer than the 2<sup>nd</sup> peak



## Measurement bandwidth

If bandwidth is too small, Gaussians are not properly fitted

