

# Electron transport simulations from first principles

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# Methods

- **Tunneling & ballistic transport:**
  - Tight-binding (hopping)
  - Kubo-Greenwood linear response  
Implemented into the fully relativistic SKKR code  
Suitable to study **magnetotransport, relativistic effects (SOC, AMR)**
  - Nonequilibrium Green's functions
- **Tunneling transport only:**  
STM simulations, different levels of theories:
  - 1D WKB (QM)
  - 3D WKB (atom superposition)
  - Tersoff-Hamann (LDOS)
  - Bardeen (perturbation theory, transfer Hamiltonian)
  - multiple scattering theory (Green's function methods)
- All above based on first principles **electronic structure** data  
**first principles = ab initio = parameter-free, no fitting**  
(Schrödinger equation or relativistic Dirac equation)

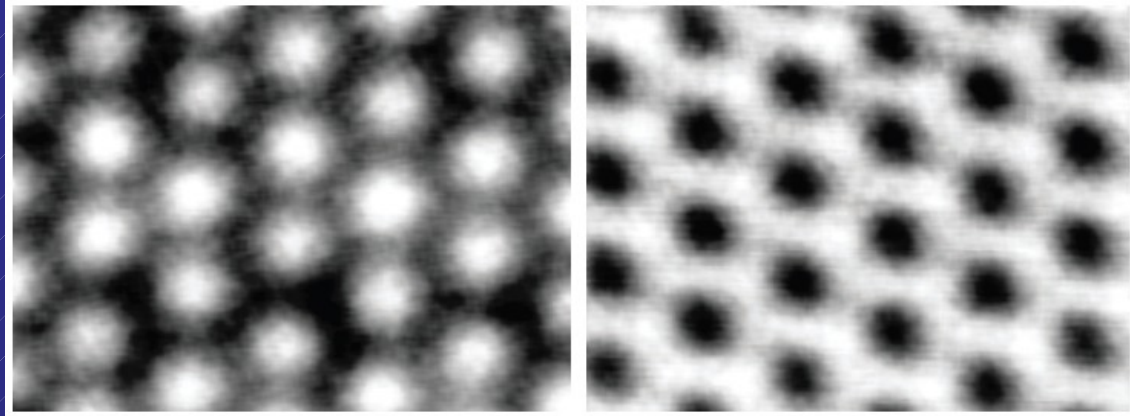
# STM simulations

- **New SP-STM/STS simulation package** developed based on electronic structure data (from first principles), extending the work of **Heinze, Appl. Phys. A 85, 407 (2006)**.
- Main features:
  1. Imaging noncollinear surface magnetic structures
  2. **Tip electronic structure** considered
  3. Bias voltage included
  4. Energy dependence of local spin quantization axes included
  5. **Easy combination with any electronic structure code**
- Studied examples:
  1. Tip-sensitivity of SP-STS: Fe(001)
  2. SP-STS: Cr ML on Ag(111)
  3. Bias-dependent magnetic contrast of SP-STM: Cr ML on Ag(111)
  4. Orbital dependent tunneling: contrast inversion on W(110)
- Conclusions

# Motivation

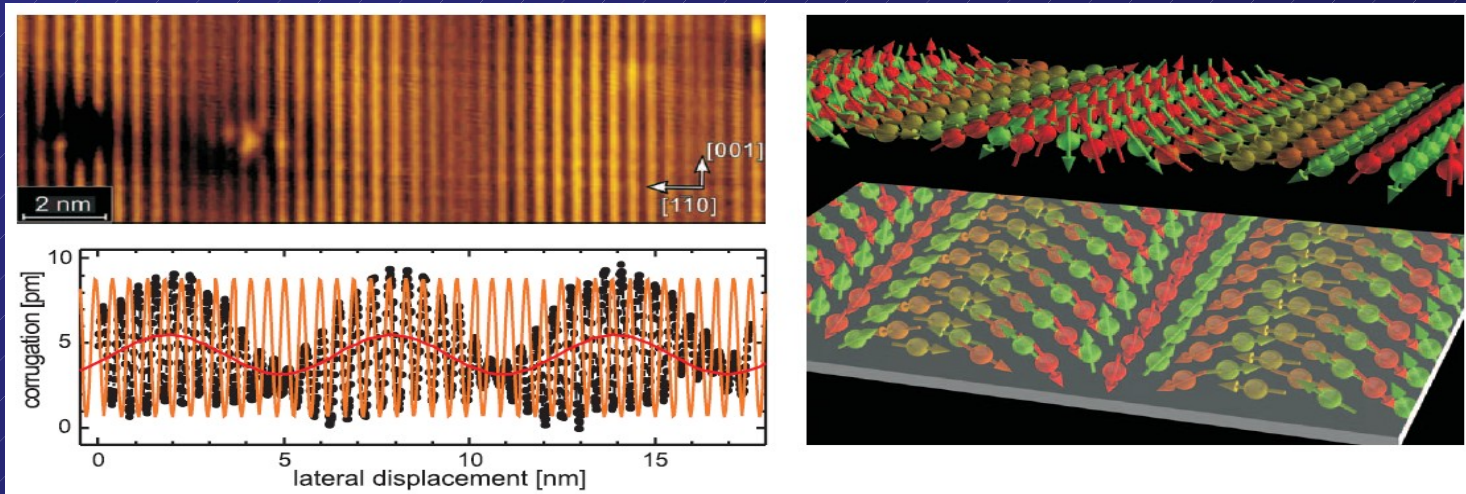
**Recent experimental advances in spin-polarized STM:**

Frustrated antiferromagnets: Mn/Ag(111), Gao and Wulfhekel, *J.Phys.Cond.Matt.* 22, 084021 (2010)



Another Review:  
Wiesendanger,  
*Rev. Mod. Phys.* 81,  
1495 (2009)

Spin spirals: Mn/W(110), Bode et al., *Nature* 447, 190 (2007)



# Recipe

Determine the **ground state magnetic structure** of the studied system (from first principles: Density Functional Theory; For larger systems: considering model Hamiltonians describing magnetic interactions or micromagnetic simulations)

Magnetic interactions from first principles: e.g.

**Antal et al., Phys. Rev. B 77, 174429 (2008)**

Multiscale approach: e.g.

**Udvardi et al., Physica B 403, 402 (2008)**

Self-consistent method based on band energy derivatives:

**Balogh et al., Phys. Rev. B 86, 024406 (2012)**

Calculate electronic structure and **simulate STM/STS**  
(**New SP-STM/STS simulation package**)

Compare the simulation results to experiments



# Theoretical description

Heinze model [Appl. Phys. A 85, 407 (2006)]:

$$LDOS(\underline{R}_{TIP}(x, y, z), E_F) = \sum_{\alpha} e^{-2\kappa|\underline{R}_{TIP} - \underline{R}_{\alpha}|} (1 + P_T(E_F) P_S^{\alpha}(E_F) \cos \varphi_{\alpha})$$

Assumption made:

Contribution to vacuum LDOS from spherical tail of atomic wave functions  
(**Independent orbital approximation**)

LDOS considered in our model at arbitrary energies:

$$LDOS(x, y, z, E, V) = \Delta E \sum_{\alpha} e^{-2\kappa(E, V)|\underline{R}_{TIP}(x, y, z) - \underline{R}_{\alpha}|} n_T(E) n_S^{\alpha}(E) [1 + P_T(E) P_S^{\alpha}(E) \cos \varphi_{\alpha}(E)]$$

Energy dependent vacuum decay:  $\kappa(E, V) = \frac{1}{\hbar} \sqrt{2m \left( \frac{\phi_S + \phi_T + eV}{2} + E_F^S - E \right)}$

Virtual diff. conductance:  $\frac{dI}{dU}(U, V) = \frac{e^2}{h} \Delta E \cdot LDOS(E_F^S + eU, V)$

**Total current:**  $I(V) = \int_0^V dU \frac{dI}{dU}(U, V)$  Palotás et al., PRB 84, 174428

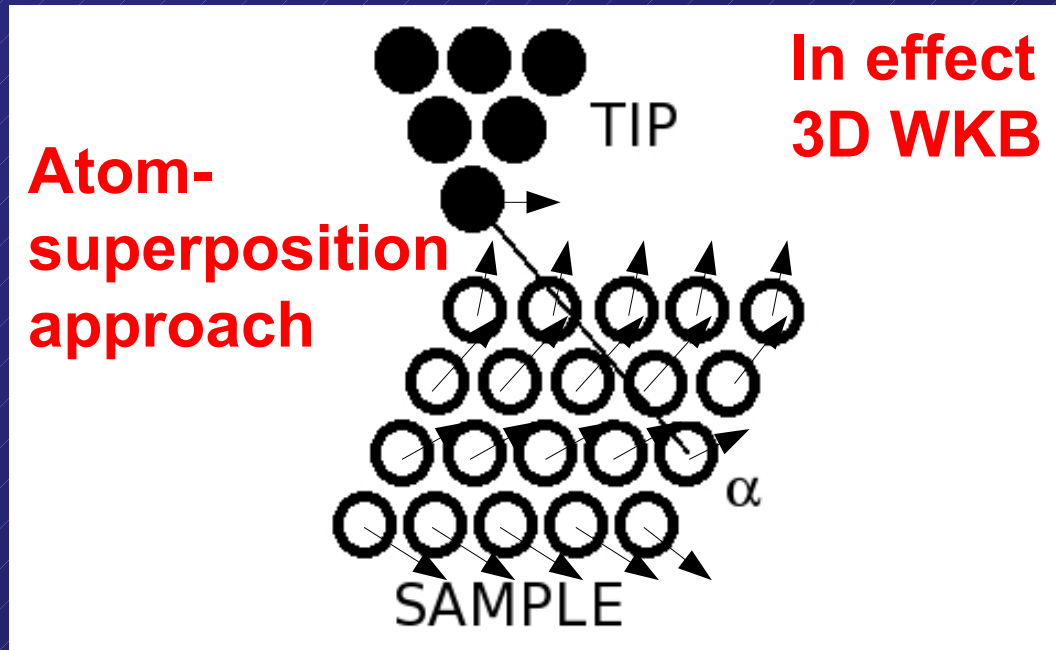
**Diff. conductance:**  $\frac{dI}{dV}(V') = \frac{dI}{dU}(V', V') + \int_0^{V'} dU \frac{\partial}{\partial V} \frac{dI}{dU}(U, V) \Big|_{V=V'}$

# Theoretical description

Modified electron local density of states at tip apex position  $\underline{R}_{TIP}$  at energy  $E$  in flavour of the **spin-pol. Tersoff-Hamann model**:

$$LDOS(x, y, z, E, V) = \Delta E \sum_{\alpha} e^{-2\kappa(E, V)|\underline{R}_{TIP}(x, y, z) - \underline{R}_{\alpha}|} n_T(E) n_S^{\alpha}(E) [1 + P_T(E) P_S^{\alpha}(E) \cos \varphi_{\alpha}(E)]$$

Topographic **TOPO**:  $n_T n_S$  and magnetic **MAGN**:  $m_T m_S \cos \varphi$  contributions  
Sum over  $\alpha$  has to be carried out over all atoms on the surface:



# Theoretical description

$$LDOS(x, y, z, E, V) = \Delta E \sum_{\alpha} e^{-2\kappa(E, V)|\underline{R}_{TIP}(x, y, z) - \underline{R}_{\alpha}|} n_T(E) n_S^{\alpha}(E) [1 + P_T(E) P_S^{\alpha}(E) \cos \varphi_{\alpha}(E)]$$

$\varphi_{\alpha}$ : angle between local spin quant. axes of tip apex and the  $\alpha$ th atom.

$P_T$  and  $P_S$  is the spin polarization of tip apex and sample atoms, respectively.

The atom-projected charge and magnetization DOS (PDOS):

$$n(E) = n_{\uparrow}(E) + n_{\downarrow}(E) \quad \text{Spin polarization (COLLINEAR calc.):}$$

$$m(E) = n_{\uparrow}(E) - n_{\downarrow}(E) \quad P_{T,S}(E) = \left( n_{T,S}^{\uparrow}(E) - n_{T,S}^{\downarrow}(E) \right) / \left( n_{T,S}^{\uparrow}(E) + n_{T,S}^{\downarrow}(E) \right)$$

**NONCOLLINEAR calc.** [Palotás et al., PRB 84, 174428 (2011)]:

$$n_{T,S}(E) = \sum_{\underline{k}} \sum_j \frac{1}{G\sqrt{\pi}} e^{-(E - \varepsilon_{T,S}^j(\underline{k}))^2 / G^2} \int_{\text{atomic volume}} d^3r \Psi_{T,S}^{jk\dagger}(\underline{r}) \Psi_{T,S}^{jk}(\underline{r})$$

$$\underline{m}_{T,S}(E) = \sum_{\underline{k}} \sum_j \frac{1}{G\sqrt{\pi}} e^{-(E - \varepsilon_{T,S}^j(\underline{k}))^2 / G^2} \int_{\text{atomic volume}} d^3r \Psi_{T,S}^{jk\dagger}(\underline{r}) \underline{\sigma} \Psi_{T,S}^{jk}(\underline{r})$$

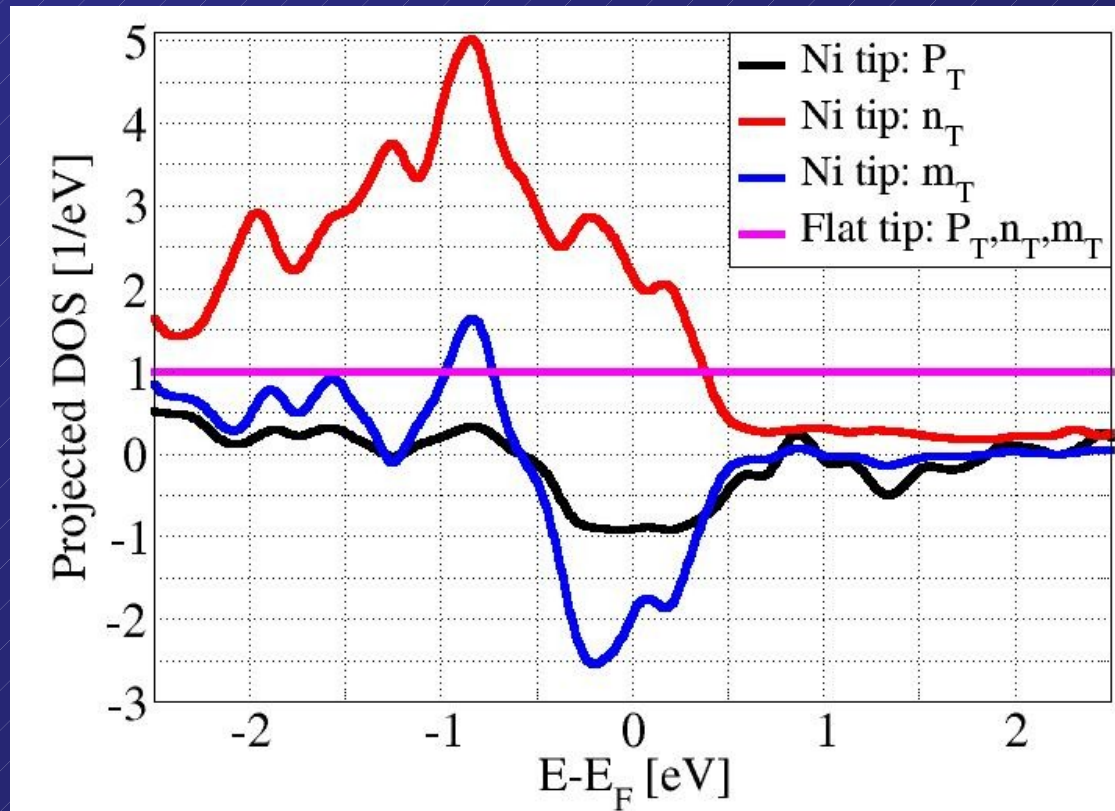
Spin polarization vector: 
$$\underline{P}_{T,S}(E) = \frac{\underline{m}_{T,S}(E)}{n_{T,S}(E)}$$



# Model tips

Three tip models considered:

1. **Ideal** maximally spin-polarized electronically **flat tip**
2. **Ni(110) tip** with single Ni atom apex, VASP+PAW, GGA-PW91  
Symm. 7 lay. Ni(110) slab+apex atom, 3x3 cell, 36 IBZ k-points  
 $P_T$  close to -1 in the energy range  $[-0.3\text{eV}, +0.3\text{eV}]$ ,  $\phi_T = 4.52\text{ eV}$
3. **Fe(001) tip with Cr apex**, data from Ferriani et al. PRB 82, 054411 (2010)



Projected DOS onto  
the tip apex atom:  
Charge ( $n$ ) and  
magnetization ( $m$ )  
DOS:

$$n(E) = n_{\uparrow}(E) + n_{\downarrow}(E)$$

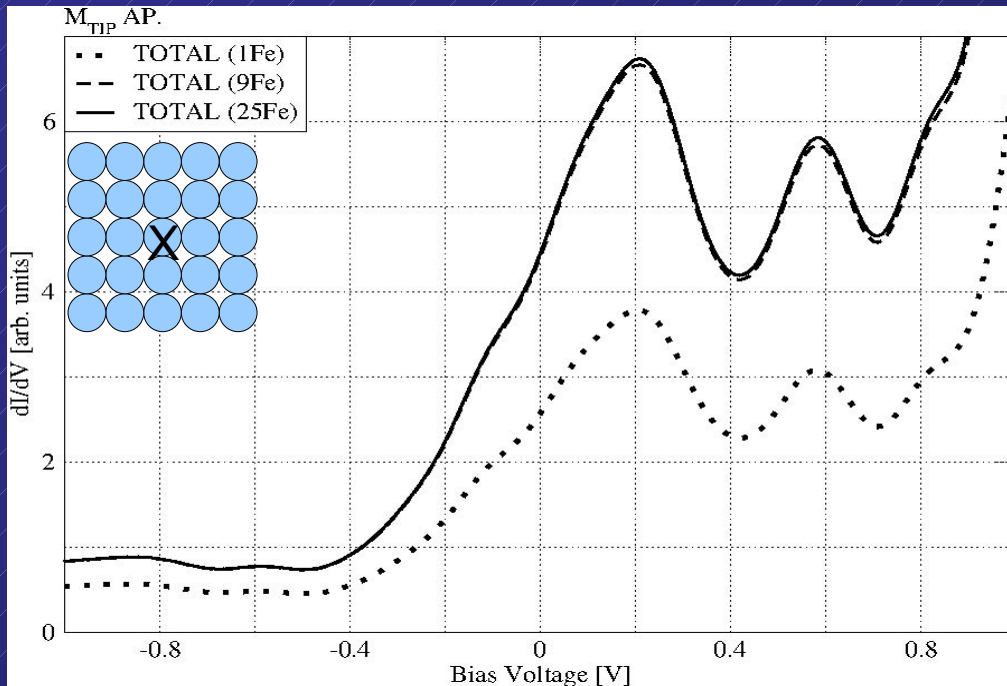
$$m(E) = n_{\uparrow}(E) - n_{\downarrow}(E)$$

Spin-polarization:  
 $P(E) = m(E)/n(E)$

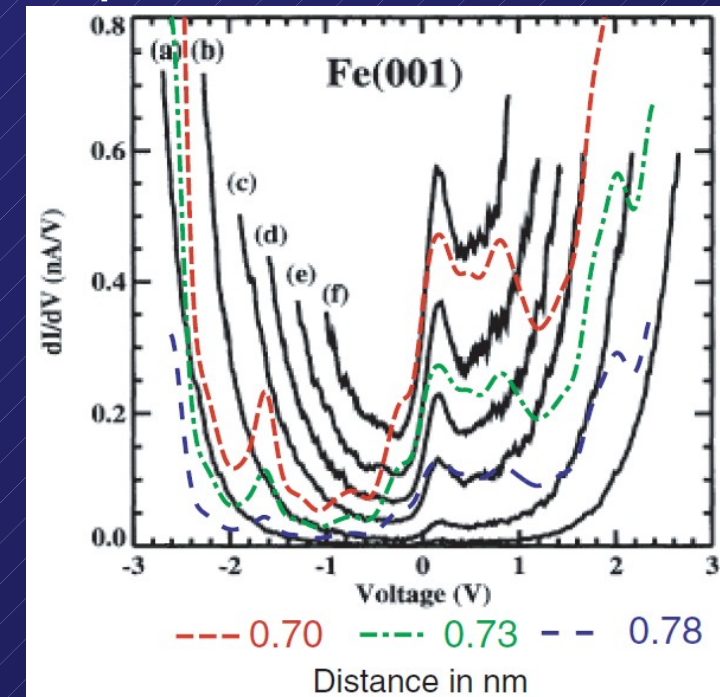
# Differential tunnelling spectrum of Fe(001)

Simulation details: VASP+PAW, GGA-PW91,  
Symmetric 13 layers Fe(001) slab, 1x1 cell, 72 k-points in IBZ

Ideal tip



Experiment and BSKAN:



Peak position at +0.20V agrees with exp. and more sophisticated calc.

Experiment: Stroscio et al. PRL 75, 2960 (1995).

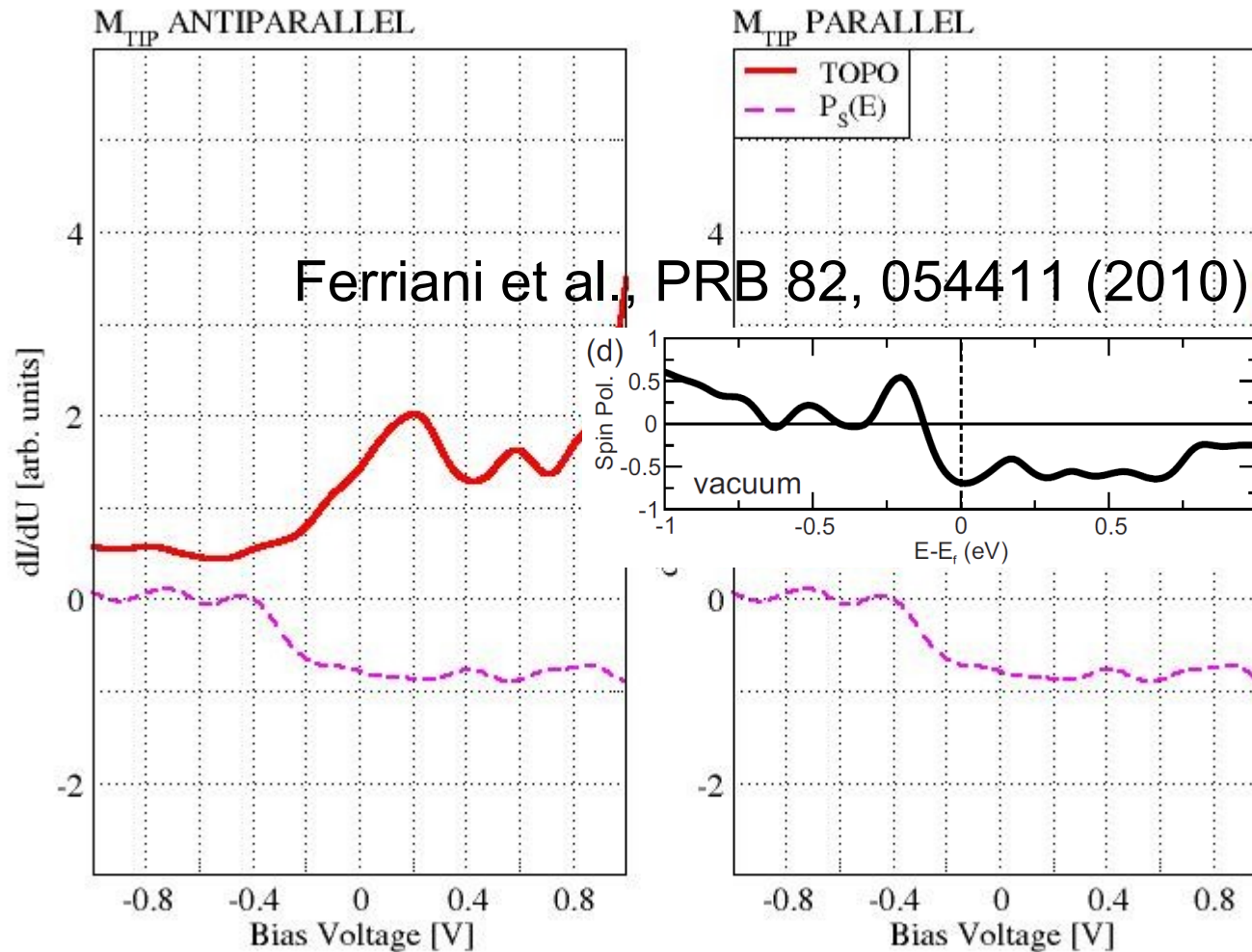
Theor. results from multiple scattering theory of tunnelling (BSKAN code):

Palotás and Hofer: J. Phys. Cond. Matt. 17, 2705 (2005).

# Differential tunnelling spectrum of Fe(001)

**Ideal tip:**  $dI/dU(U)$

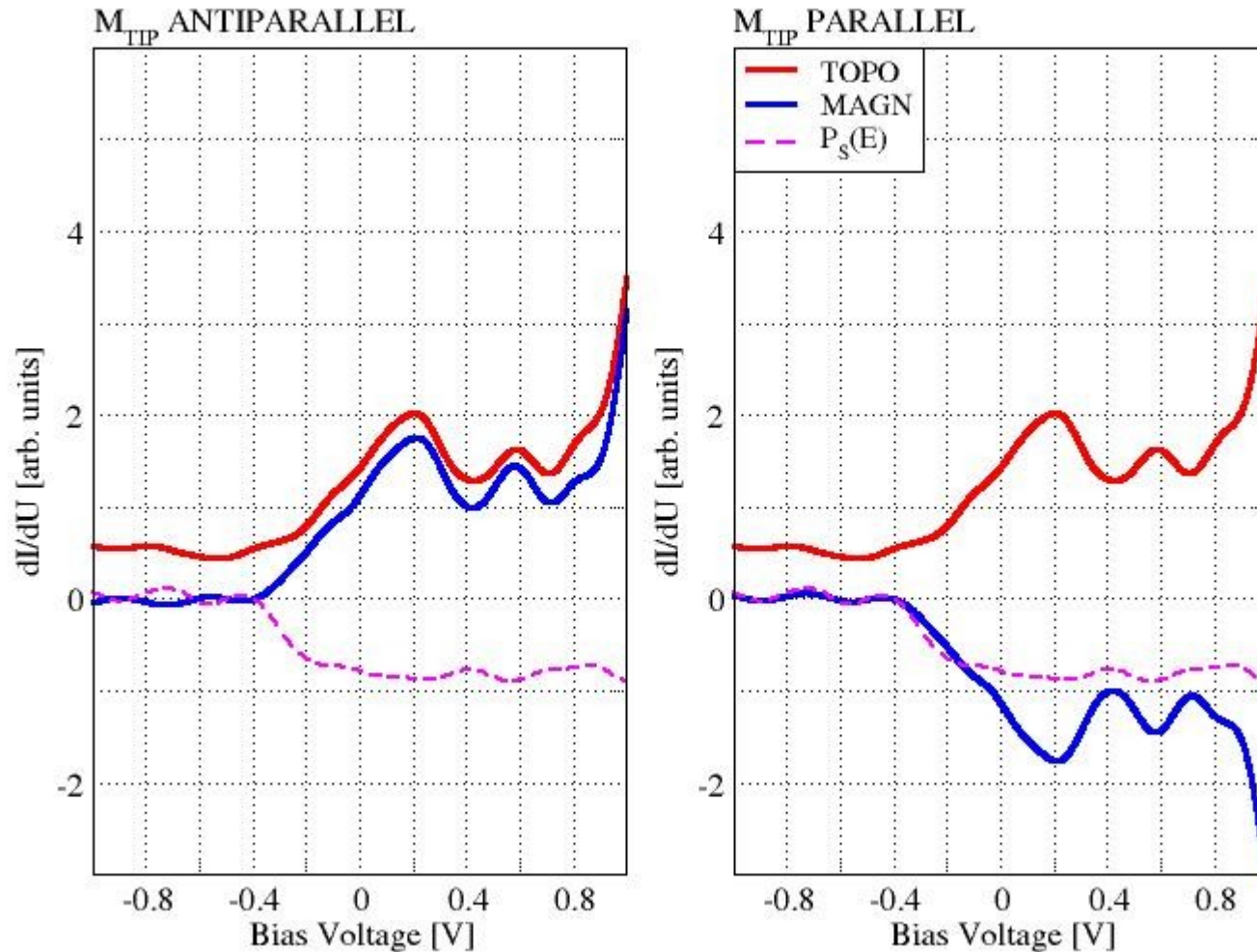
Palotás et al., PRB 83, 214410 (2011)



# Differential tunnelling spectrum of Fe(001)

**Ideal tip:**  $dI/dU(U)$

Palotás et al., PRB 83, 214410 (2011)

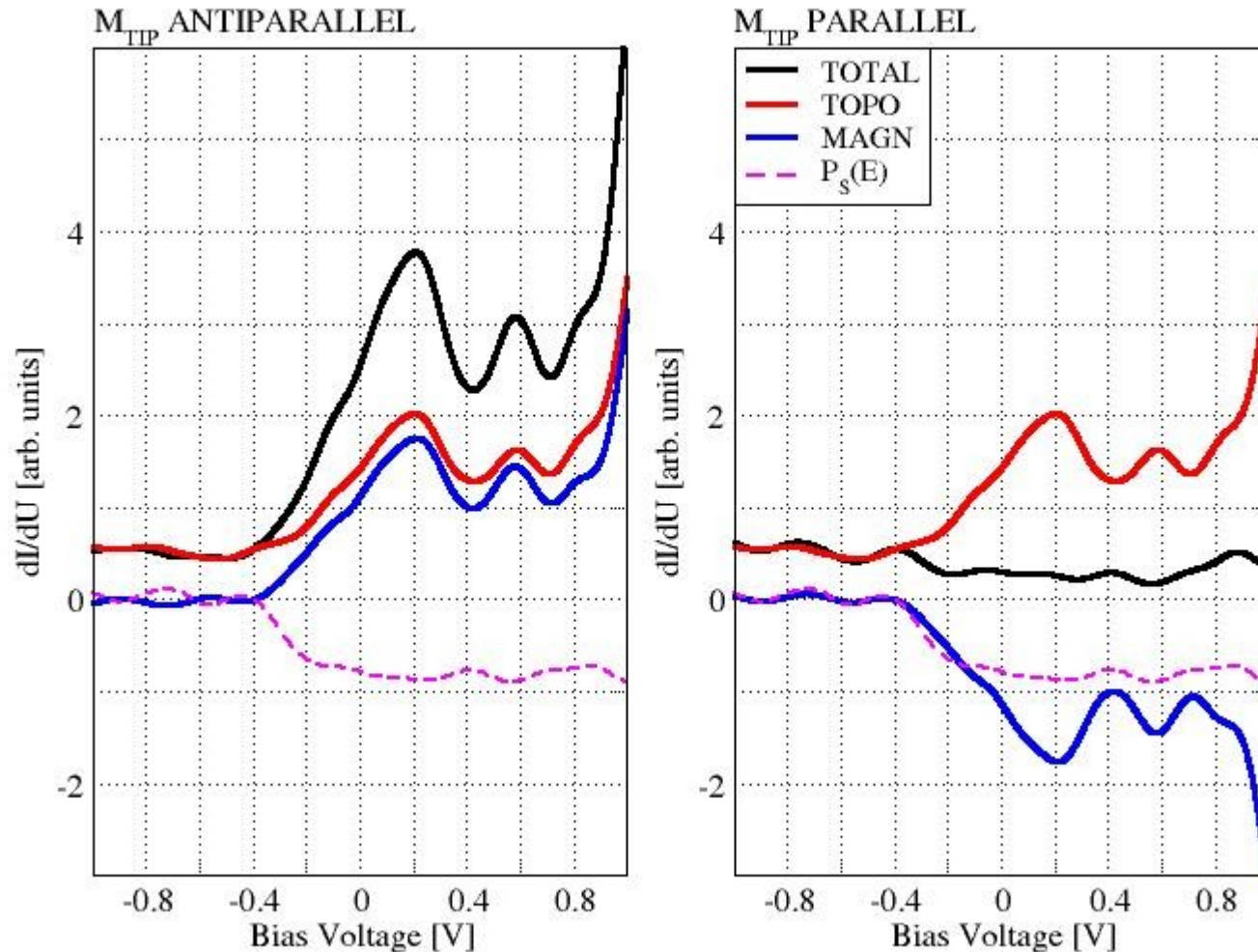




# Differential tunnelling spectrum of Fe(001)

**Ideal tip:**  $dI/dU(U)$

Palotás et al., PRB 83, 214410 (2011)



Sensitivity of STS can be tuned by changing **tip magnetization direction!**  
Enhanced sensitivity is possible!



# Imaging noncollinear surface magnetic structures

## Cr monolayer on Ag(111) surface

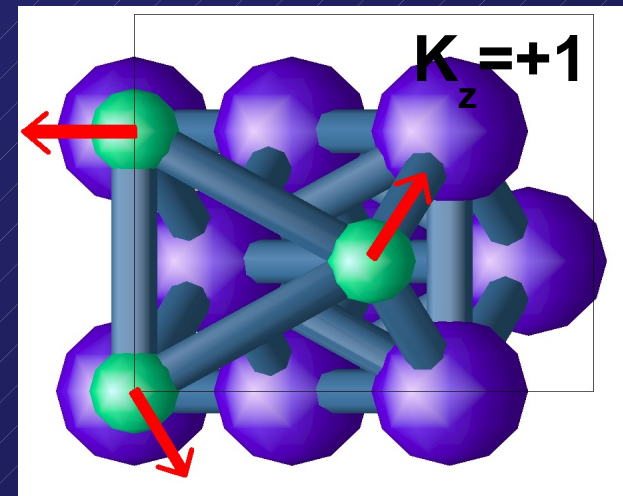
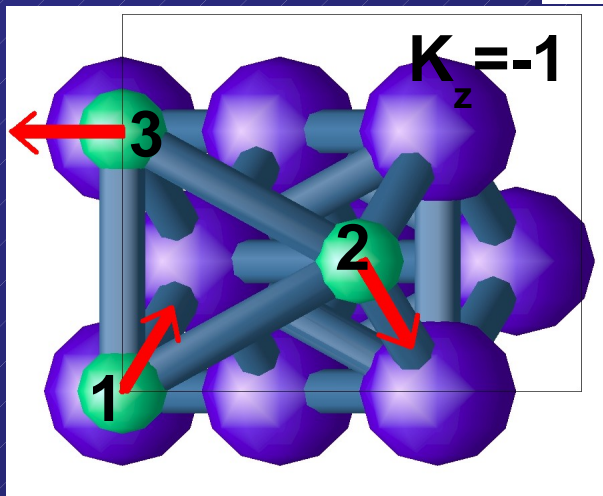
Simulation details: VASP+PAW+SOC, GGA-PW91

Symmetric 5 layers Ag slab+Cr layers, 121 BZ k-points

Two different magnetic chiralities characterized by

$$\underline{K} = \frac{2}{3\sqrt{3}} (\underline{e}_S^1 \times \underline{e}_S^2 + \underline{e}_S^2 \times \underline{e}_S^3 + \underline{e}_S^3 \times \underline{e}_S^1) \text{ chirality vector}$$

Magnetic unit cell:  $(\sqrt{3} \times \sqrt{3})R30^\circ$  Palotás et al., PRB 84, 174428

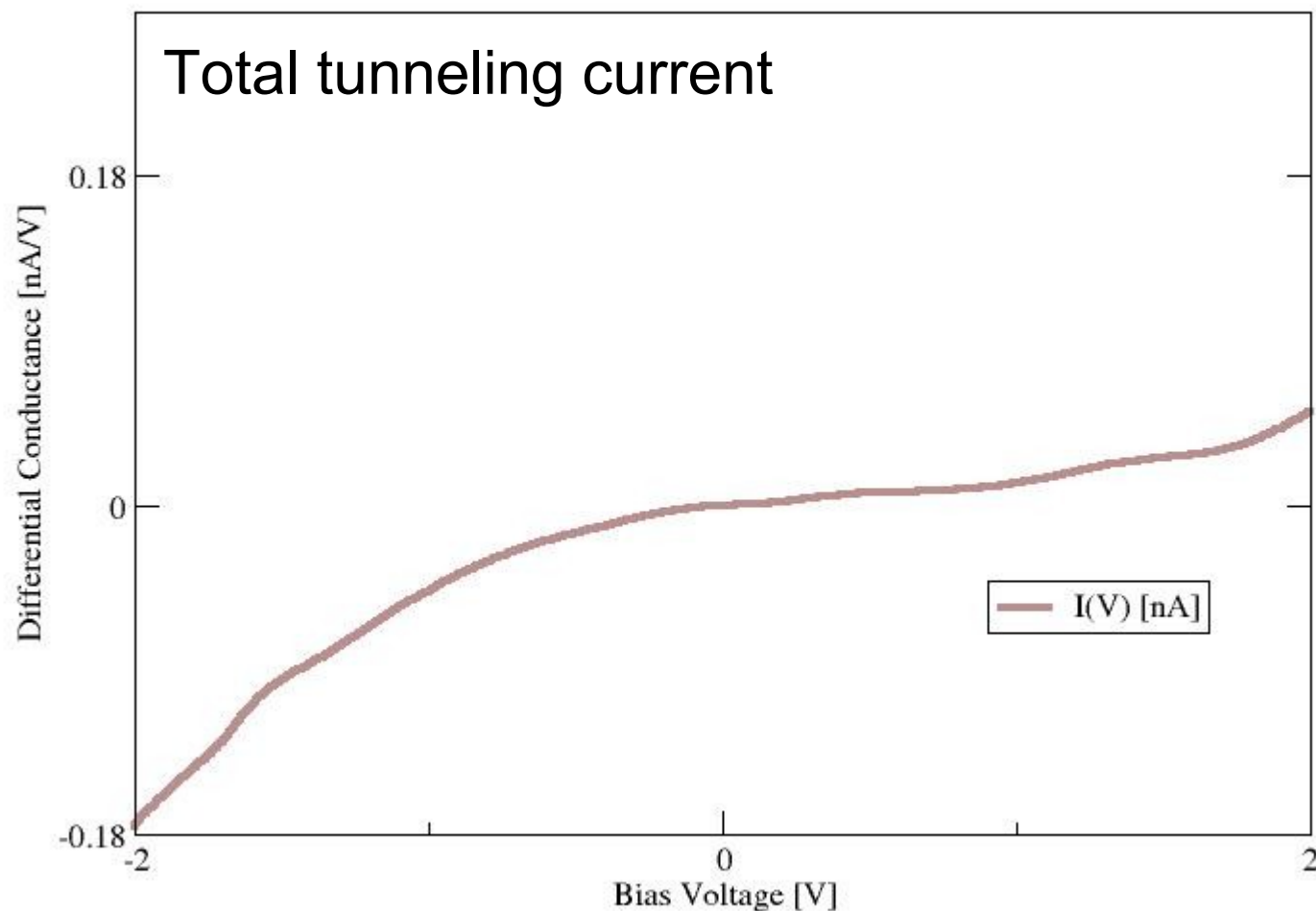


$K_z = -1$  energetically favored by 1.1 meV (FM state 1.04 eV higher)

Cr: AFM coupling  $\rightarrow$  noncollinear  $120^\circ$  Néel state,  $|M_{Cr}| = 3.73 \mu_B$

# Cr monolayer on Ag(111) surface

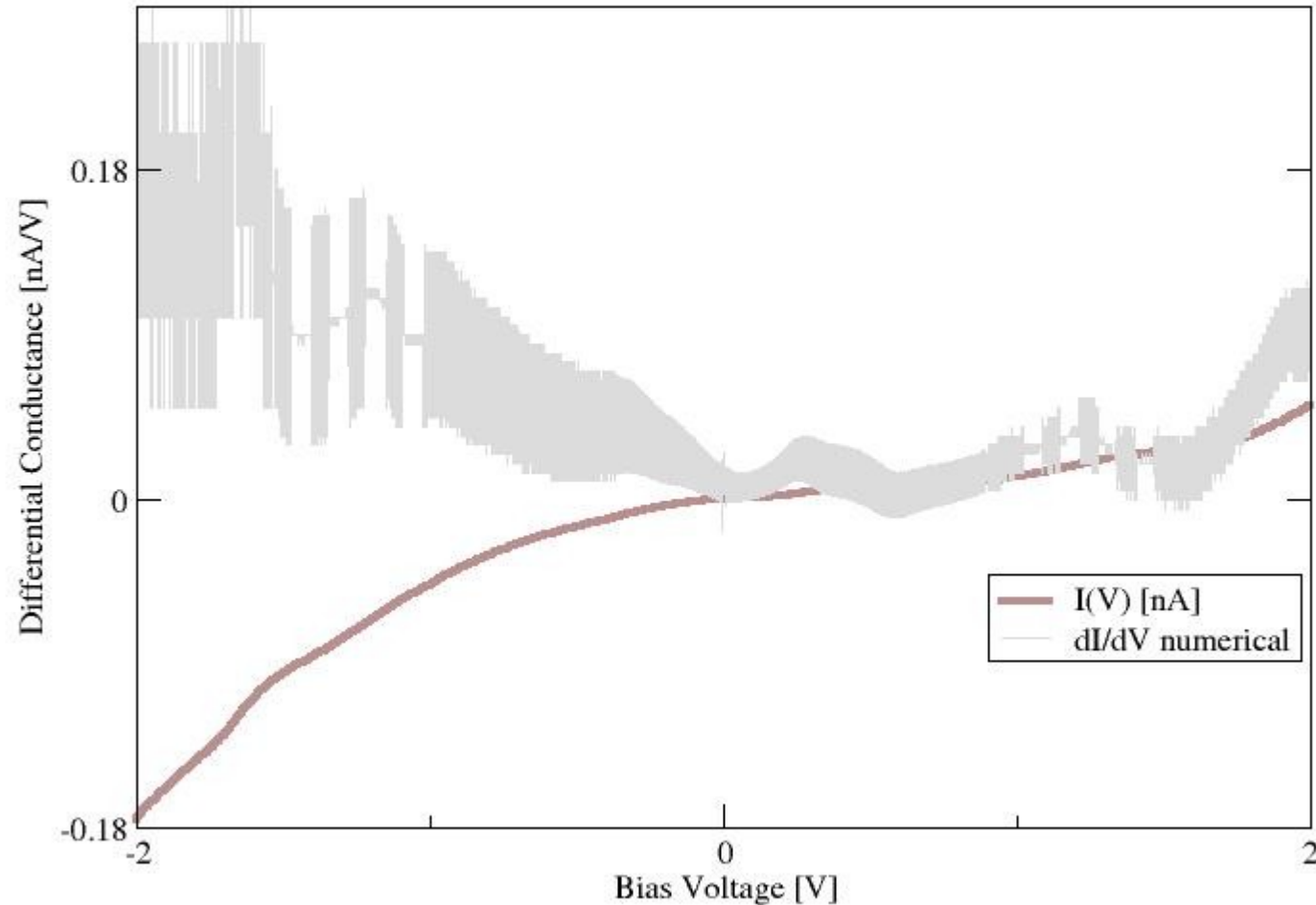
Tip: Cr adatom on Fe(001) [Ferriani et al. PRB 82, 054411 (2010)]  
@  $z=3.5$  Angstroms above surface Cr atom



Palotás et al., Phys. Rev. B 85, 205427 (2012)

# Cr monolayer on Ag(111) surface

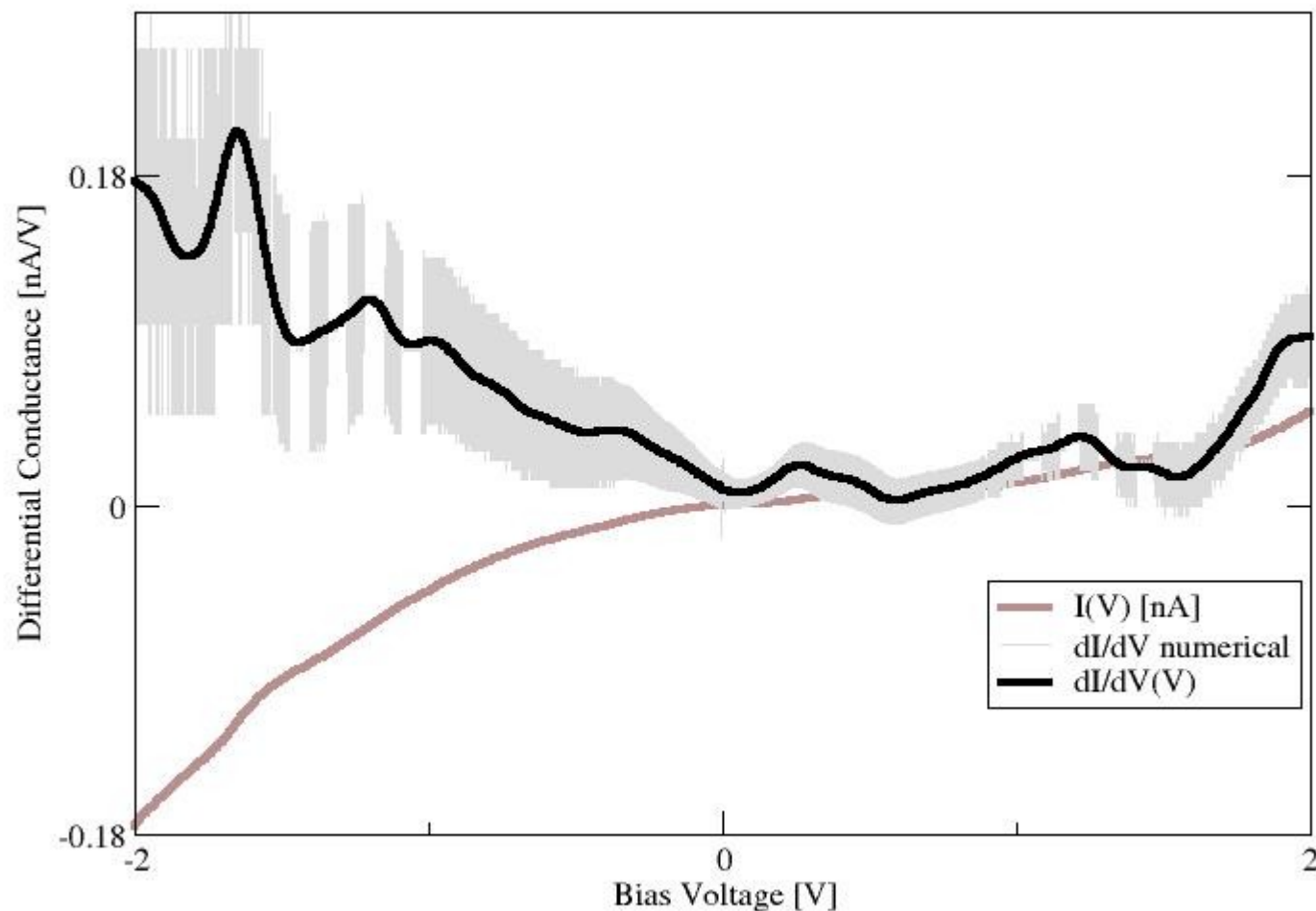
Differential conductance  $dI/dV$



Palotás et al., Phys. Rev. B 85, 205427 (2012)

# Cr monolayer on Ag(111) surface

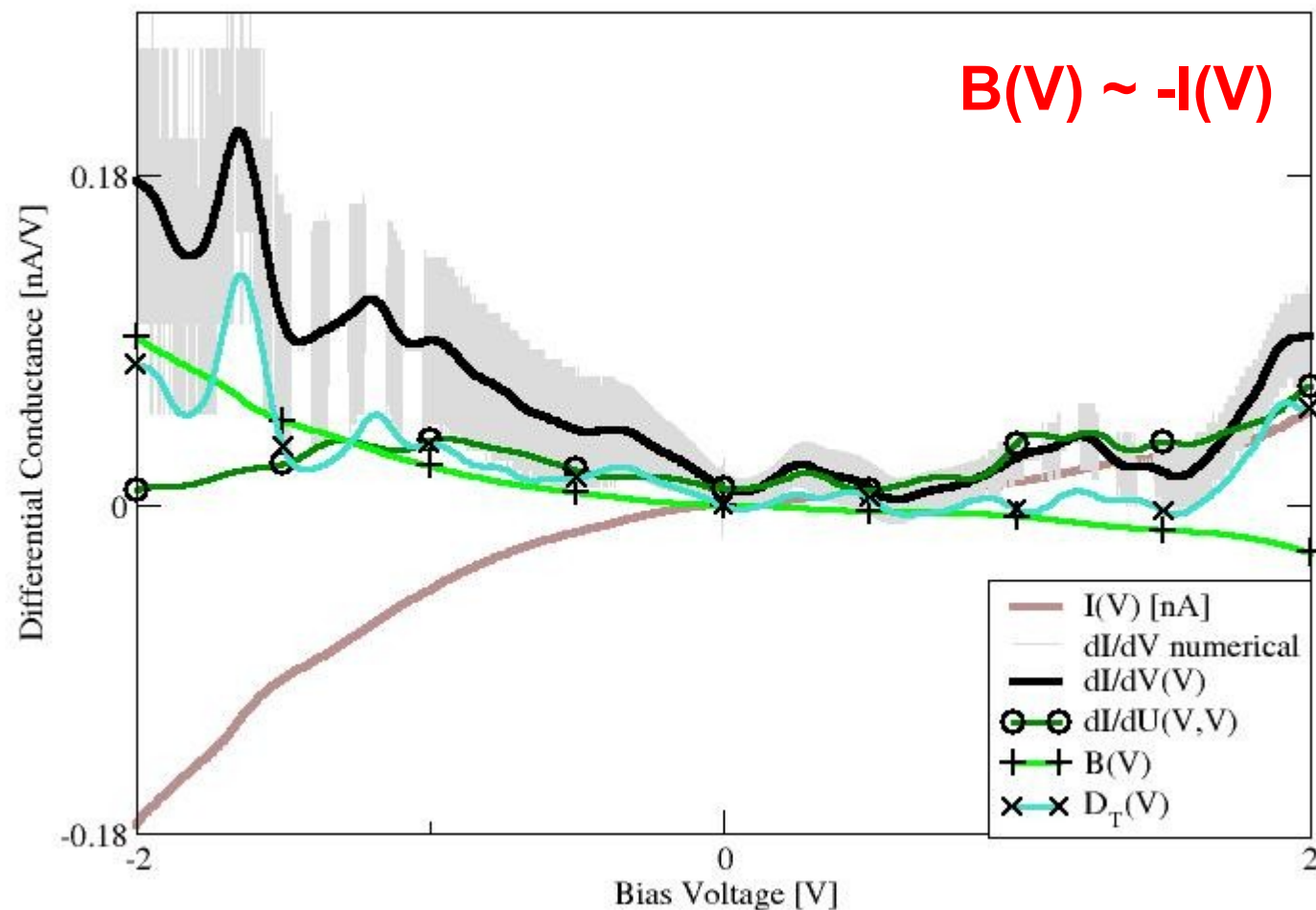
Differential conductance  $dI/dV$



Palotás et al., Phys. Rev. B 85, 205427 (2012)

# Cr monolayer on Ag(111) surface

$$\frac{dI_{TOTAL}}{dV}(x, y, z, V) = \frac{dI}{dU}(x, y, z, V, V) + B(x, y, z, V) + D_T(x, y, z, V)$$





Magnetic asymmetry:  $A_{MAGN}(x, y, z, V) = \frac{dI^P/dV(x, y, z, V) - dI^{AP}/dV(x, y, z, V)}{dI^P/dV(x, y, z, V) + dI^{AP}/dV(x, y, z, V)}$

Relation to the effective spin polarization

Differential conductance:

$$\frac{dI_{TOTAL}}{dV}(x, y, z, V) = \frac{dI}{dU}(x, y, z, V, V) + B(x, y, z, V) + D_T(x, y, z, V)$$

~LDOS

background  
( $\partial T/\partial V$ )

tip-derivative  
( $\partial n_T/\partial V$ )

Magnetic asymmetry:

$$A^{dI/dV}(x, y, z, V) = \frac{dI_{MAGN}^P/dV(x, y, z, V)}{dI_{TOPO}/dV(x, y, z, V)} \neq ESP$$

$$= \frac{dI_{MAGN}^P/dU(x, y, z, V, V) + B_{MAGN}^P(x, y, z, V) + D_T^{MAGN,P}(x, y, z, V)}{dI_{TOPO}/dU(x, y, z, V, V) + B_{TOPO}(x, y, z, V) + D_T^{TOPO}(x, y, z, V)}$$

Effective spin polarization:

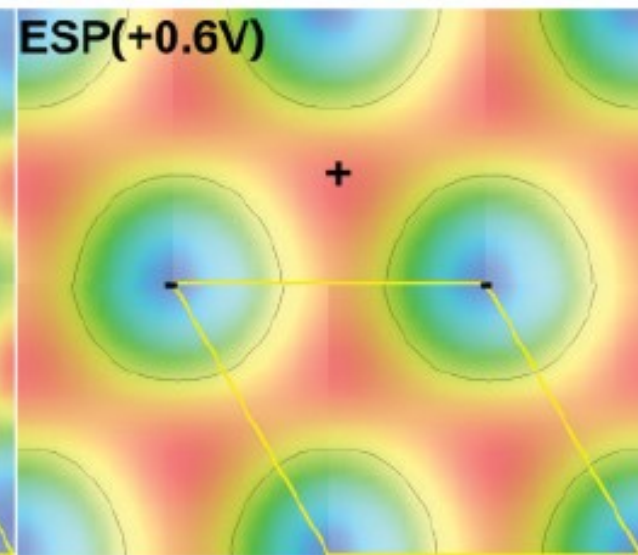
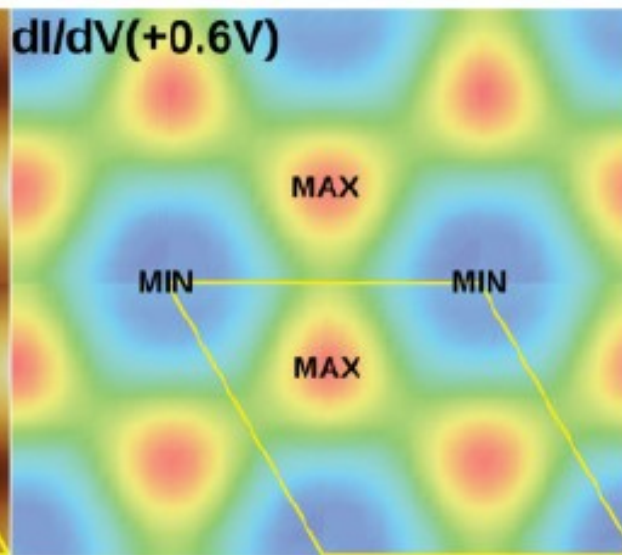
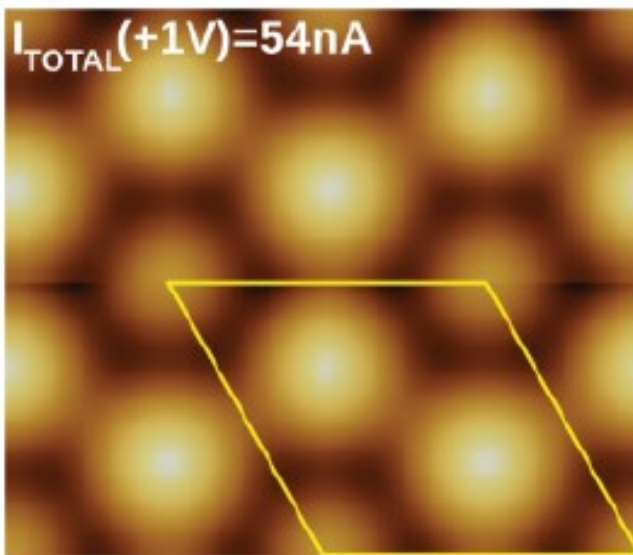
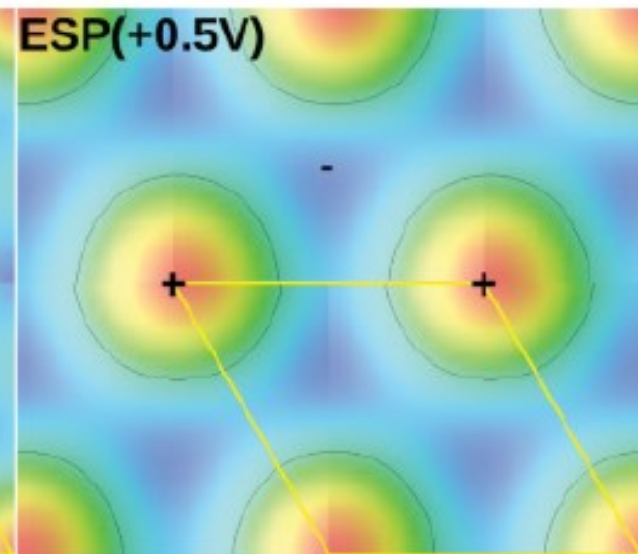
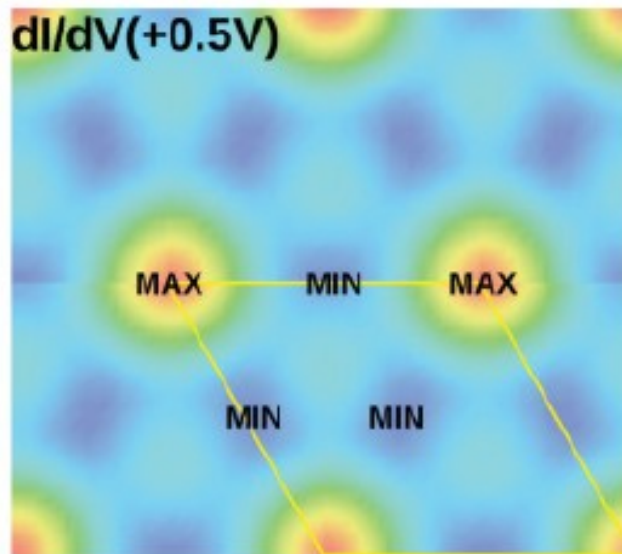
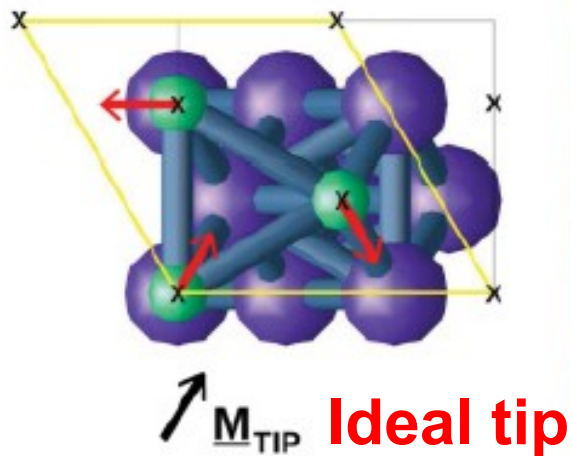
$$A^{dI/dU}(x, y, z, V) = \frac{dI_{MAGN}^P/dU(x, y, z, V, V)}{dI_{TOPO}/dU(x, y, z, V, V)}$$

$$= \underline{P}_T(E_F^T) \underline{P}_S(x, y, z, E_F^S + eV)$$

Palotás et al.,  
PRB 85, 205427 (2012)

# Cr monolayer on Ag(111) surface

## 2D $dI/dV$ & ESP maps on constant current contour



# Cr monolayer on Ag(111) surface

## Dependence of magnetic contrast on tip magnetization orientation

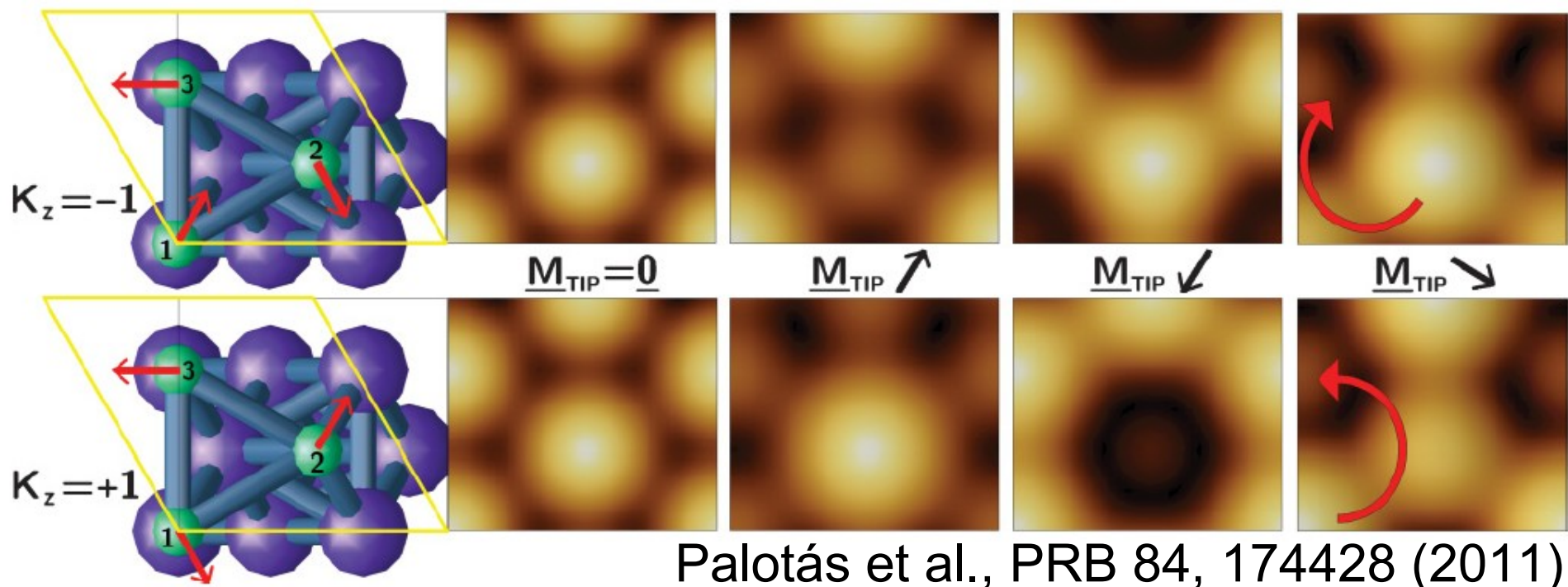
**Ideal magnetic tip, 0 V bias**,  $\phi_s = 4.47$  eV

Qualitatively similar images obtained in SP-STM exp./sim. for Néel states:

Cr/Ag(111) [Heinze, Appl. Phys. A 85, 407 \(2006\)](#) (sim.),

Mn/Ag(111) [Gao and Wulfhekel, Phys. Rev. Lett. 101, 267205 \(2008\)](#) (exp.),

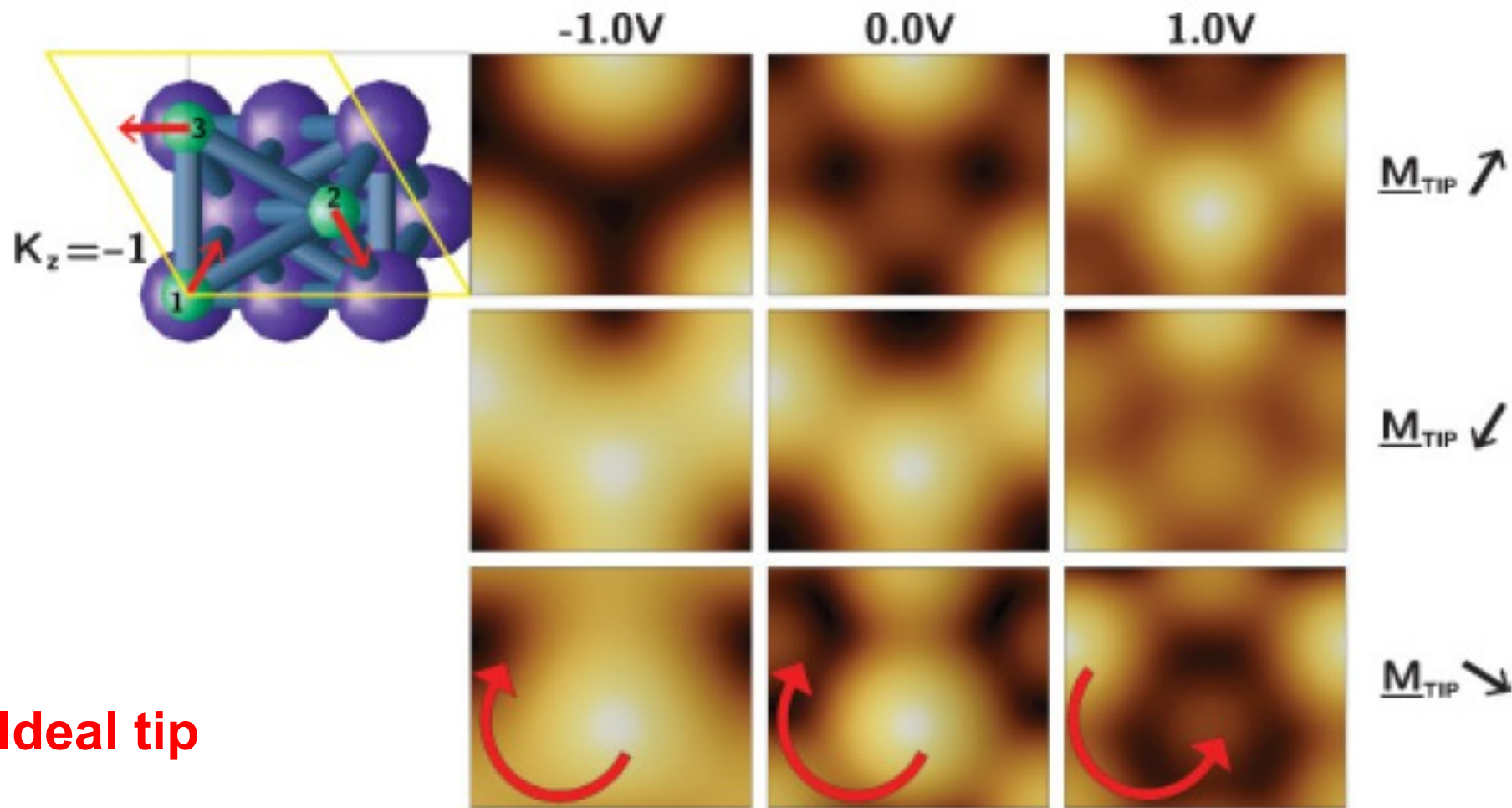
Cr/Pd(111) [Waśniowska et al., Phys. Rev. B 82, 012402 \(2010\)](#) (exp.+sim.)





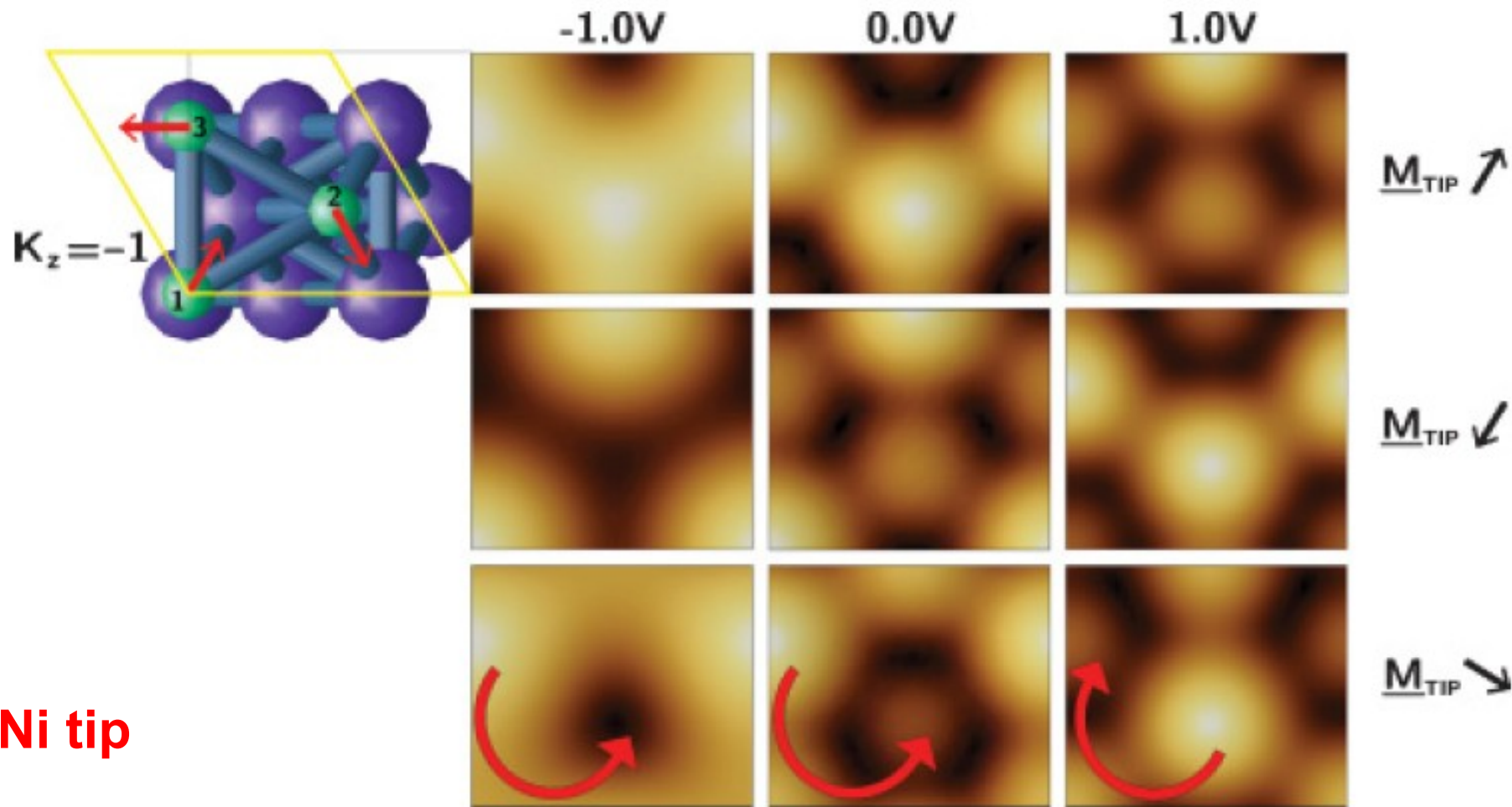
# Cr monolayer on Ag(111) surface

## Bias dependent magnetic contrast



# Cr monolayer on Ag(111) surface

## Bias dependent magnetic contrast



Ni tip

Be careful when interpreting SP-STM images!  
Palotás et al., PRB 84, 174428 (2011)



# Relation between constant current and constant height STM images

Height contrast between A and B lateral surface points in nonmagnetic STM: (Chen: Introduction to STM, 1993)

$$\Delta z_{\text{nonmagn}}^{AB}(z_1, V) = -\frac{\Delta I^{AB}(z_1, V)}{\partial I^{\text{av}}/\partial z(z_1, V)}$$

Total contrast in spin-polarized STM:

$$\begin{aligned}\Delta z^{AB}(z_1, V) &= \Delta z_{\text{TOPO}}^{AB}(z_1, V) + \Delta z_{\text{MAGN}}^{AB}(z_1, V) \\ &= -\frac{\Delta I_{\text{TOPO}}^{AB}(z_1, V)}{\partial I_{\text{TOT}}^{\text{av}}/\partial z(z_1, V)} - \frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOT}}^{\text{av}}/\partial z(z_1, V)}\end{aligned}$$

Averaged current over the scan area:

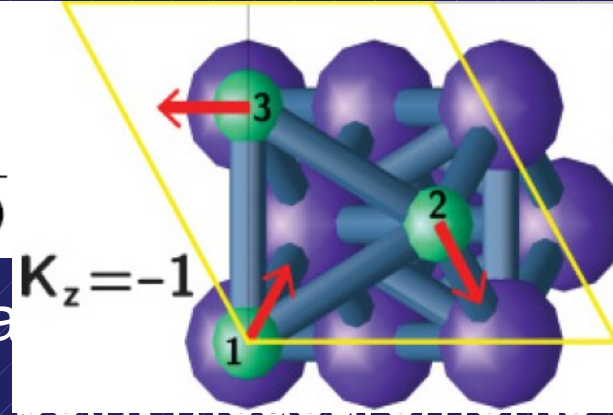
$$I_{\text{TOT}}^{\text{av}}(z, V) = \frac{1}{N_x N_y} \sum_{i=1}^{N_x} \sum_{j=1}^{N_y} I_{\text{TOT}}(x_i, y_j, z, V)$$

Palotás, Phys. Rev. B 87, 024417 (2013)

# Magnetic contrast estimation

Assumptions: Atomically flat surface consisting of chemically equivalent & magnetically inequivalent atoms

$$\begin{aligned} \Delta z^{AB}(z_1, V) &= \cancel{\Delta z_{\text{TOPO}}^{AB}(z_1, V)} + \Delta z_{\text{MAGN}}^{AB}(z_1, V) \\ &= -\cancel{\frac{\Delta I_{\text{TOPO}}^{AB}(z_1, V)}{\partial I_{\text{TOT}}^{\text{av}}/\partial z(z_1, V)}} - \frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOT}}^{\text{av}}/\partial z(z_1, V)} \end{aligned}$$



We want to avoid scanning the full scan and predict the magnetic contrast from single

→ 2 propositions: (measurements over points A and B needed)

$$\begin{aligned} \Delta z_I^{AB}(z_1, V) &= -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOPO}}^A/\partial z(z_1, V)} \\ &= \frac{I_{\text{MAGN}}^A(z_1, V) - I_{\text{MAGN}}^B(z_1, V)}{2\kappa_{\text{TOPO}}^A(V)I_{\text{TOPO}}^A(z_1, V)} \end{aligned}$$

$$\begin{aligned} \Delta z_{II}^{AB}(z_1, V) &= -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOT}}^{\text{av.}AB}/\partial z(z_1, V)} \\ &= \frac{I_{\text{MAGN}}^A(z_1, V) - I_{\text{MAGN}}^B(z_1, V)}{2\kappa_{\text{TOT}}^{\text{av.}AB}(V)I_{\text{TOT}}^{\text{av.}AB}(z_1, V)} \end{aligned}$$

# Magnetic contrast estimation

$$\begin{aligned}\Delta z_I^{AB}(z_1, V) &= -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOPO}}^A / \partial z(z_1, V)} \\ &= \frac{I_{\text{MAGN}}^A(z_1, V) - I_{\text{MAGN}}^B(z_1, V)}{2\kappa_{\text{TOPO}}^A(V) I_{\text{TOPO}}^A(z_1, V)}\end{aligned}$$

$$\begin{aligned}\Delta z_{II}^{AB}(z_1, V) &= -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOT}}^{\text{av.}AB} / \partial z(z_1, V)} \\ &= \frac{I_{\text{MAGN}}^A(z_1, V) - I_{\text{MAGN}}^B(z_1, V)}{2\kappa_{\text{TOT}}^{\text{av.}AB}(V) I_{\text{TOT}}^{\text{av.}AB}(z_1, V)}\end{aligned}$$

## Motivation:

Magnetic modulation  
superimposed on  
topographic image

$$\Delta z_{\text{nonmagn}}^{AB}(z_1, V) = -\frac{\Delta I^{AB}(z_1, V)}{\partial I^{\text{av}} / \partial z(z_1, V)}$$



$$\begin{aligned}\Delta I^{AB} &\rightarrow \Delta I_{\text{MAGN}}^{AB} \\ I^{\text{av}} &\rightarrow I_{\text{TOPO}}\end{aligned}$$

$$I_{\text{TOPO}}^A(z, V) = I_{\text{TOPO}}^{A0}(V) e^{-2\kappa_{\text{TOPO}}^A(V)z}$$

$$I_{\text{TOT}}^{\text{av}}(z, V) = \frac{1}{N_x N_y} \sum_{i=1}^{N_x} \sum_{j=1}^{N_y} I_{\text{TOT}}(x_i, y_j, z, V)$$

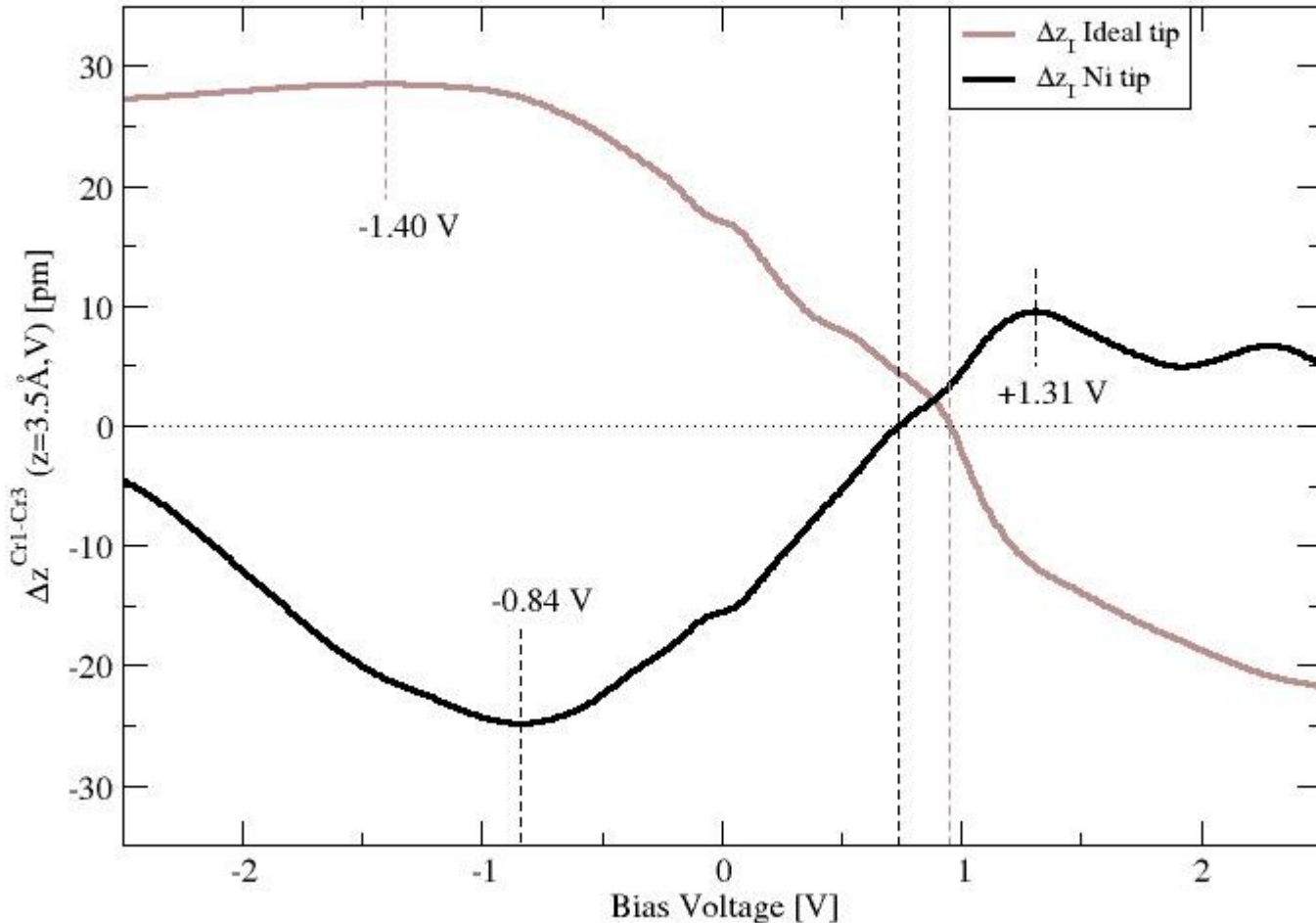


Average over scan area  
→ average over A & B

$$\begin{aligned}I_{\text{TOT}}^{\text{av.}AB}(z, V) &= \frac{I_{\text{TOT}}^A(z, V) + I_{\text{TOT}}^B(z, V)}{2} \\ &= I_{\text{TOT}}^{\text{av.}AB0}(V) e^{-2\kappa_{\text{TOT}}^{\text{av.}AB}(V)z}.\end{aligned}$$

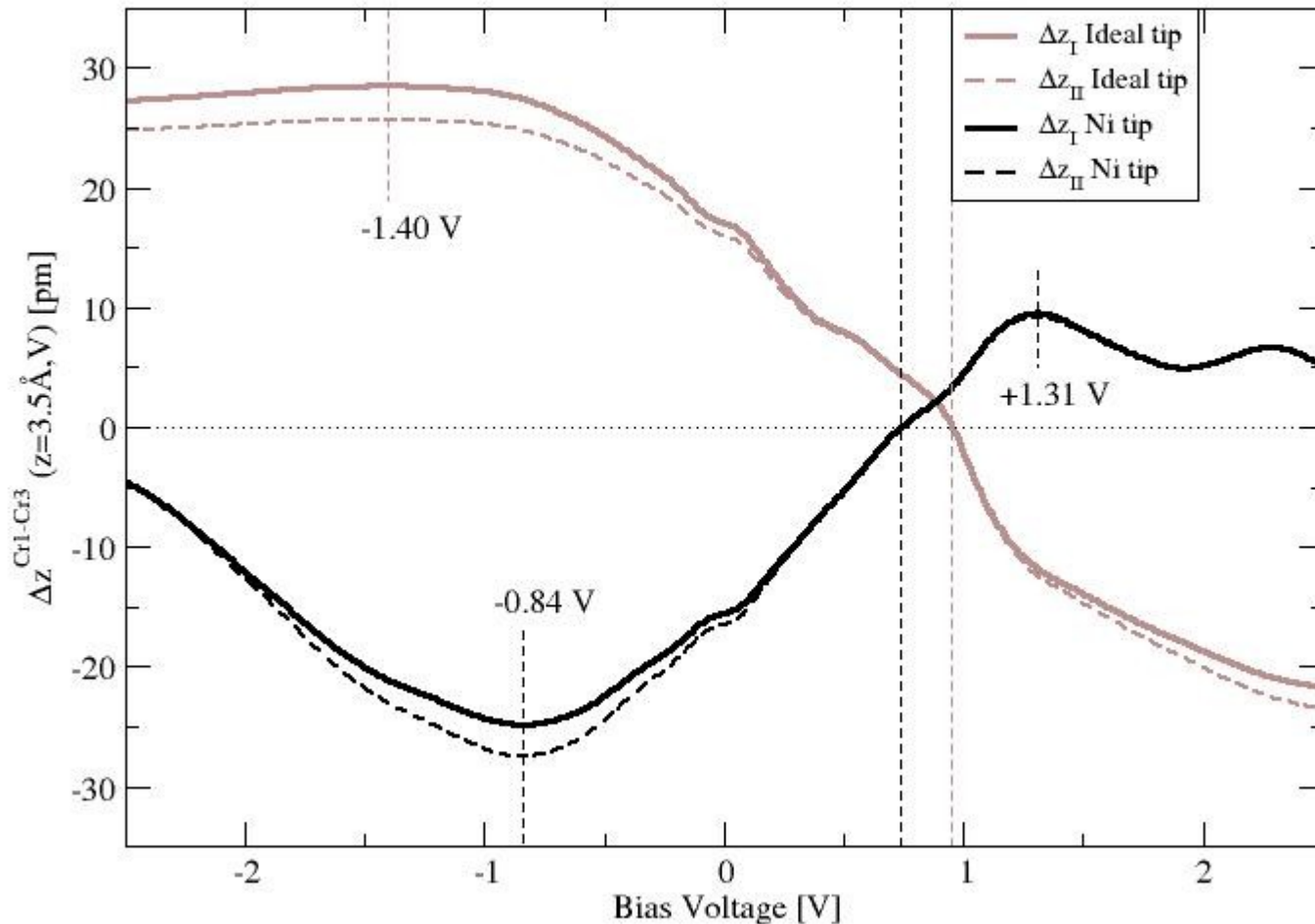
# Prediction of bias dependent magnetic contrast

$$\Delta z_I^{AB}(z_1, V) = -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOPO}}^A / \partial z(z_1, V)}$$



# Prediction of bias dependent magnetic contrast

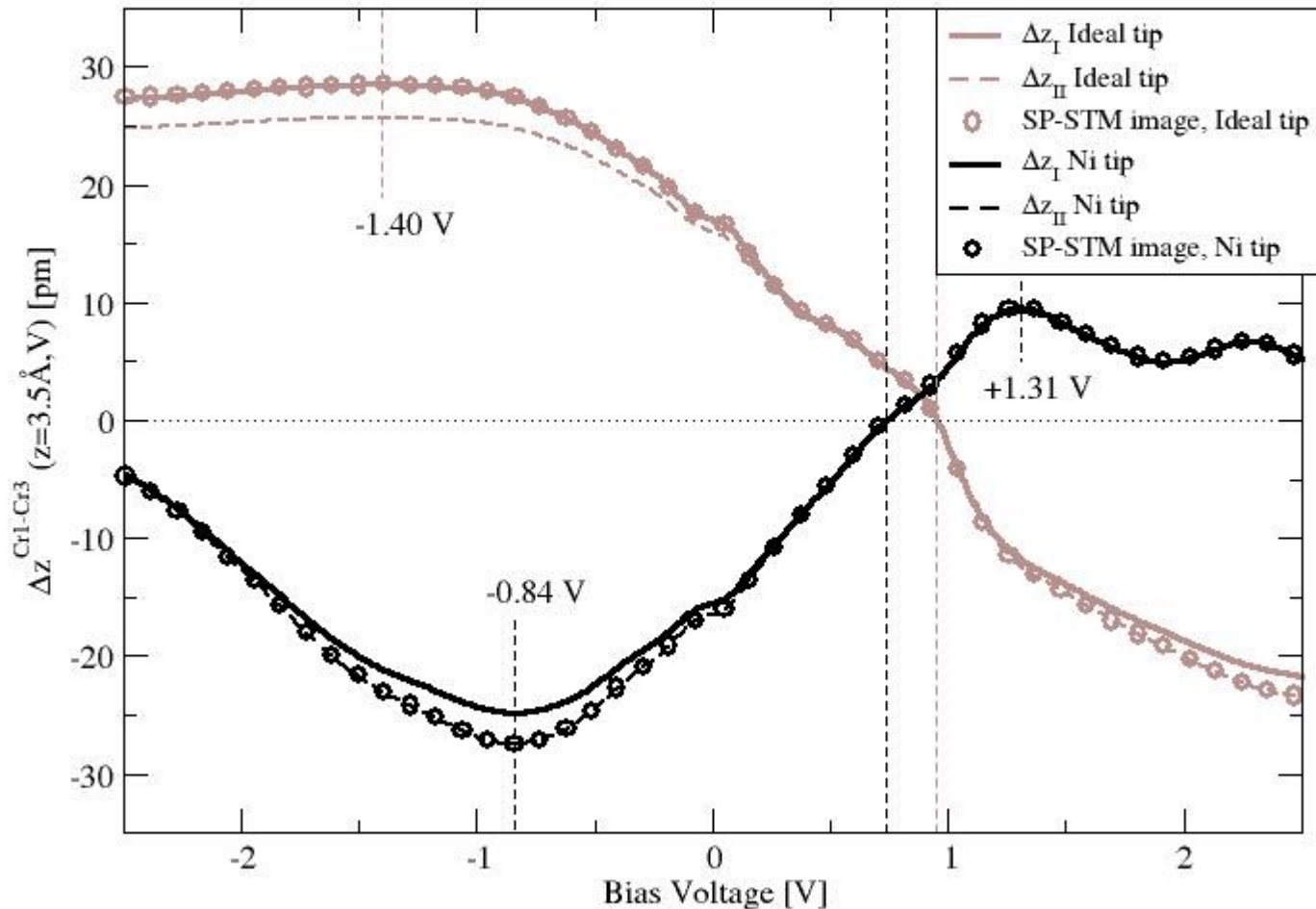
$$\Delta z_I^{AB}(z_1, V) = -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOPO}}^A / \partial z(z_1, V)} \quad \Delta z_{II}^{AB}(z_1, V) = -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOT}}^{\text{av.}AB} / \partial z(z_1, V)}$$





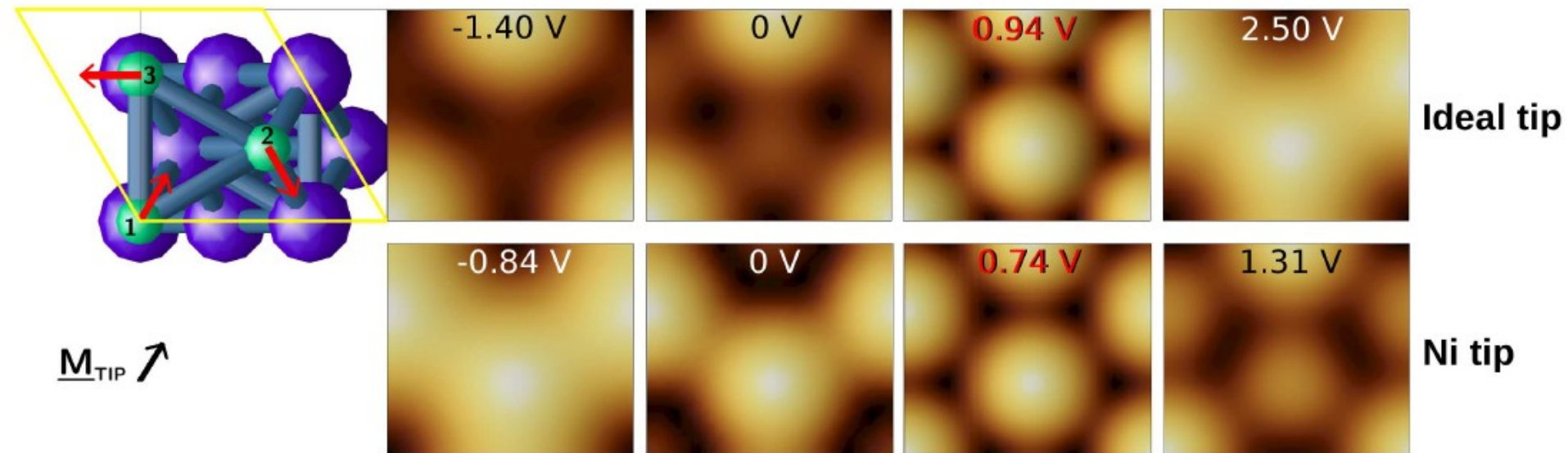
# Prediction of bias dependent magnetic contrast

$$\Delta z_I^{AB}(z_1, V) = -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOPO}}^A / \partial z(z_1, V)} \quad \Delta z_{II}^{AB}(z_1, V) = -\frac{\Delta I_{\text{MAGN}}^{AB}(z_1, V)}{\partial I_{\text{TOT}}^{\text{av.}AB} / \partial z(z_1, V)}$$



# Cr monolayer on Ag(111) surface

## Bias dependent magnetic contrast



Contrast reversal observed using ideal tip  
→ effect of surface electronic structure

**Tip electronic structure plays a role as well!**

Experimental verification is needed!

Palotás, Phys. Rev. B 87, 024417 (2013)

Palotás et al., Phys. Rev. B 84, 174428 (2011)

# Orbital independent tunneling

## Theoretical description

$$I(x, y, z, V) = \int_0^V \frac{dI}{dU}(x, y, z, U, V) dU$$

$$\frac{dI}{dU}(x, y, z, U, V) = \varepsilon^2 \frac{e^2}{h}$$

$$\times \sum_{\alpha} T(E_F^S + eU, V, d_{\alpha}(x, y, z)) n_T(E_F^T + eU - eV) n_S^{\alpha}(E_F^S + eU)$$

$$T(E_F^S + eU, V, d_{\alpha}) = e^{-2\kappa(U, V)d_{\alpha}}$$

Independent orbital approximation

$$\kappa(U, V) = \frac{1}{\hbar} \sqrt{2m \left( \frac{\phi_S + \phi_T + eV}{2} - eU \right)}$$

# Orbital dependent tunneling

## Theoretical description

$$n_S^\alpha(E) = \sum_{\beta} n_{S\beta}^\alpha(E)$$

$$n_T(E) = \sum_{\gamma} n_{T\gamma}(E)$$

Orbital decomposition of PDOS

$\beta, \gamma \in$

$\{s, p_y, p_z, p_x, d_{xy}, d_{yz}, d_{3z^2-r^2}, d_{xz}, d_{x^2-y^2}\}$

$$\frac{dI}{dU}(x, y, z, U, V) = \varepsilon^2 \frac{e^2}{h}$$

Generalization

(10)

$$\times \sum_{\alpha} \sum_{\beta, \gamma} T_{\beta\gamma}(E_F^S + eU, V, d_{\alpha}(x, y, z)) n_{T\gamma}(E_F^T + eU - eV) n_{S\beta}^{\alpha}(E_F^S + eU),$$

$$I(x, y, z, V) = \sum_{\beta, \gamma} I_{\beta\gamma}(x, y, z, V)$$

$$I_{\beta\gamma}(x, y, z, V) = \varepsilon^2 \frac{e^2}{h}$$

$$\times \sum_{\alpha} \int_0^V T_{\beta\gamma}(E_F^S + eU, V, d_{\alpha}(x, y, z)) n_{T\gamma}(E_F^T + eU - eV) n_{S\beta}^{\alpha}(E_F^S + eU) dU$$



# Orbital dependent tunneling

## Theoretical description

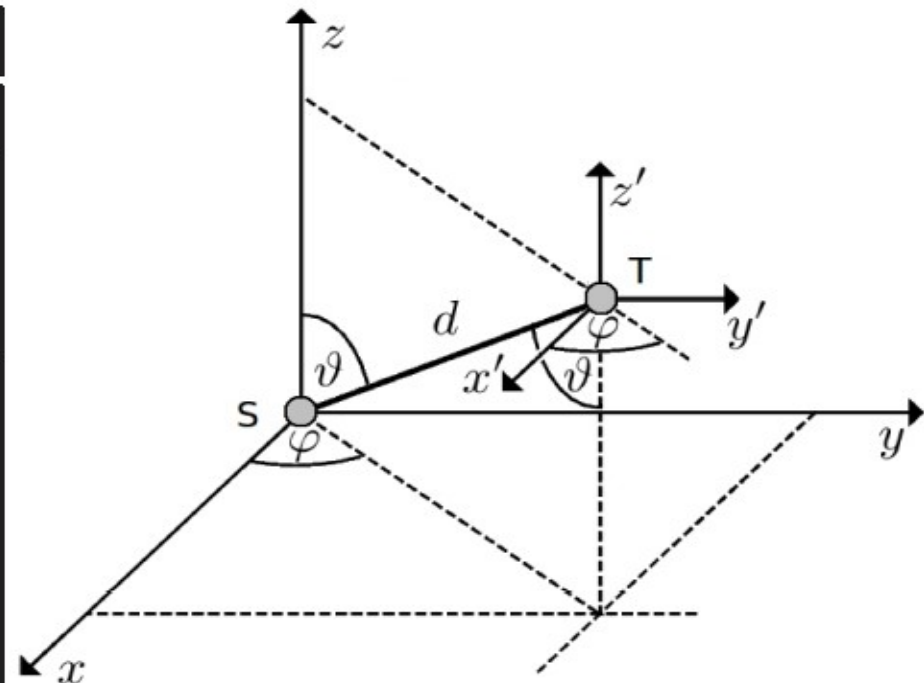
Generalized transmission function:  $\leftarrow$  orbital-independent

$$T_{\beta\gamma}(E_F^S + eU, V, d_\alpha) = e^{-2\kappa(U,V)d_\alpha} t_{\beta\gamma}(\vartheta_\alpha, \varphi_\alpha)$$

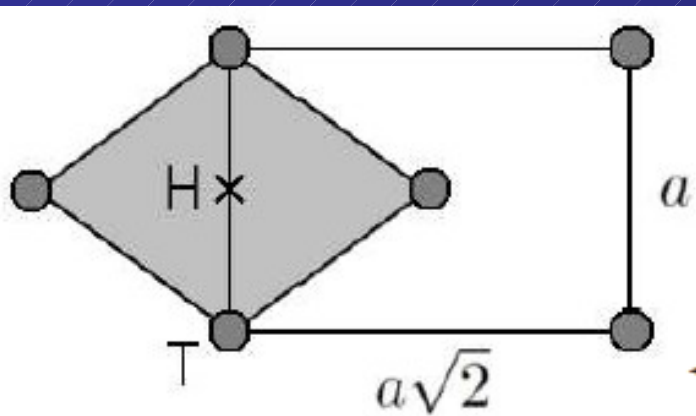
$\leftarrow$  orbital dependent

$$t_{\beta\gamma}(\vartheta_\alpha, \varphi_\alpha) = [\chi_\beta(\vartheta_\alpha, \varphi_\alpha)]^2 \times [\chi_\gamma(\vartheta_\alpha + \pi, \varphi_\alpha + \pi)]^2$$

orbital	index	definition	$\chi(\vartheta, \varphi)$
$s$	1	$Y_0^0$	1
$p_y$	2	$Y_1^1 - Y_1^{-1}$	$\sin(\vartheta)\sin(\varphi)$
$p_z$	3	$Y_1^0$	$\cos(\vartheta)$
$p_x$	4	$Y_1^1 + Y_1^{-1}$	$\sin(\vartheta)\cos(\varphi)$
$d_{xy}$	5	$Y_2^2 - Y_2^{-2}$	$\sin^2(\vartheta)\sin(2\varphi)$
$d_{yz}$	6	$Y_2^1 - Y_2^{-1}$	$\sin(2\vartheta)\sin(\varphi)$
$d_{3z^2-r^2}$	7	$Y_2^0$	$\frac{1}{2}(3\cos^2(\vartheta) - 1)$
$d_{xz}$	8	$Y_2^1 + Y_2^{-1}$	$\sin(2\vartheta)\cos(\varphi)$
$d_{x^2-y^2}$	9	$Y_2^2 + Y_2^{-2}$	$\sin^2(\vartheta)\cos(2\varphi)$



## Orbital contributions to the current on W(110)

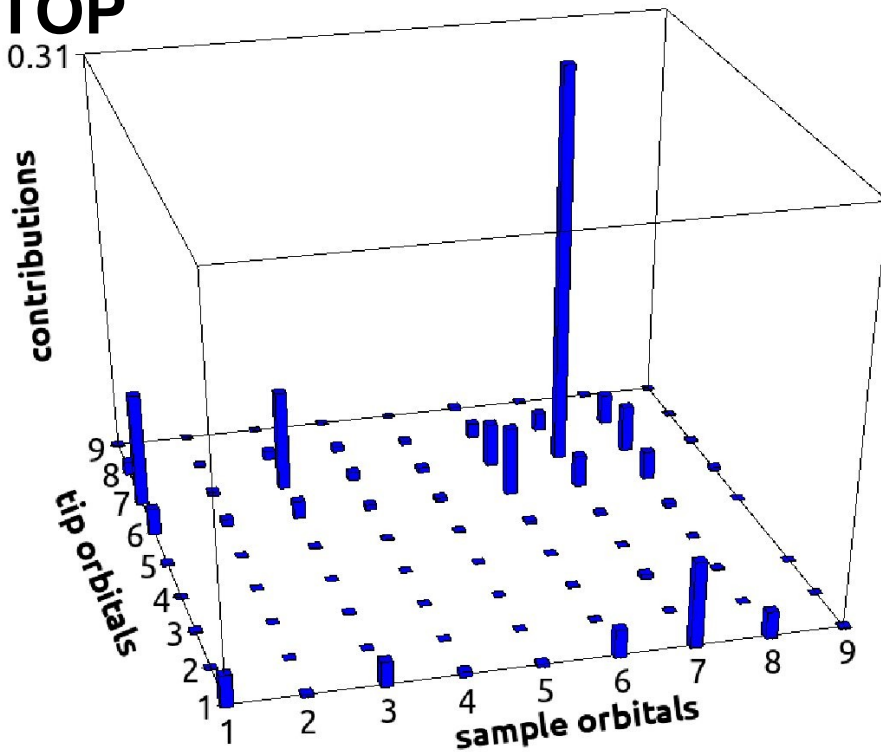


$$V = -0.1 \text{ V}, z = 4.5 \text{ Angströms}$$

$$\{s, p_y, p_z, p_x, d_{xy}, d_{yz}, d_{3z^2-r^2}, d_{xz}, d_{x^2-y^2}\}$$

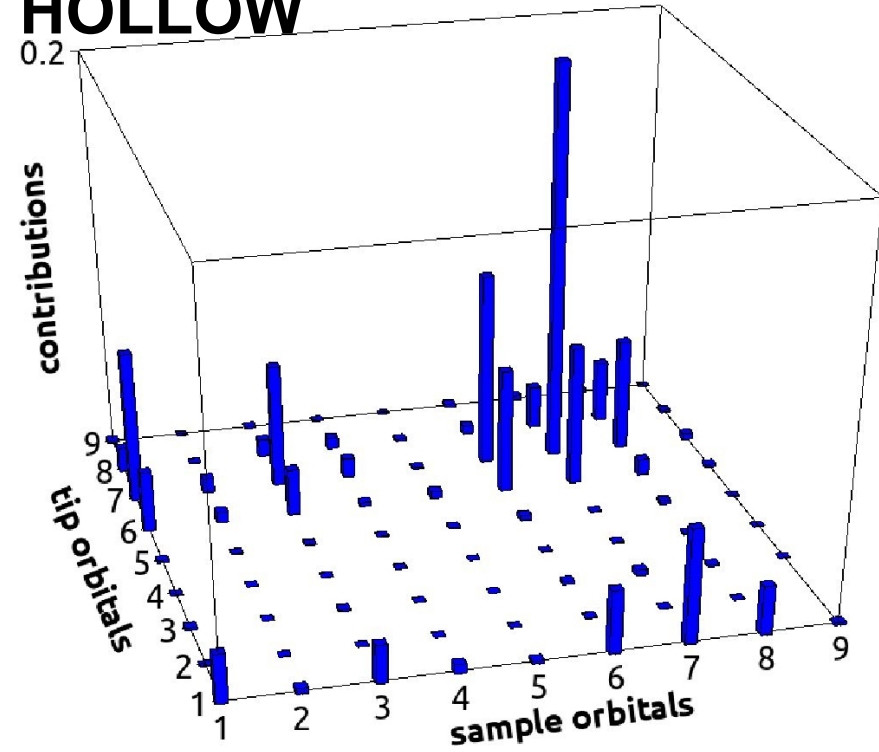
TOP

0.31



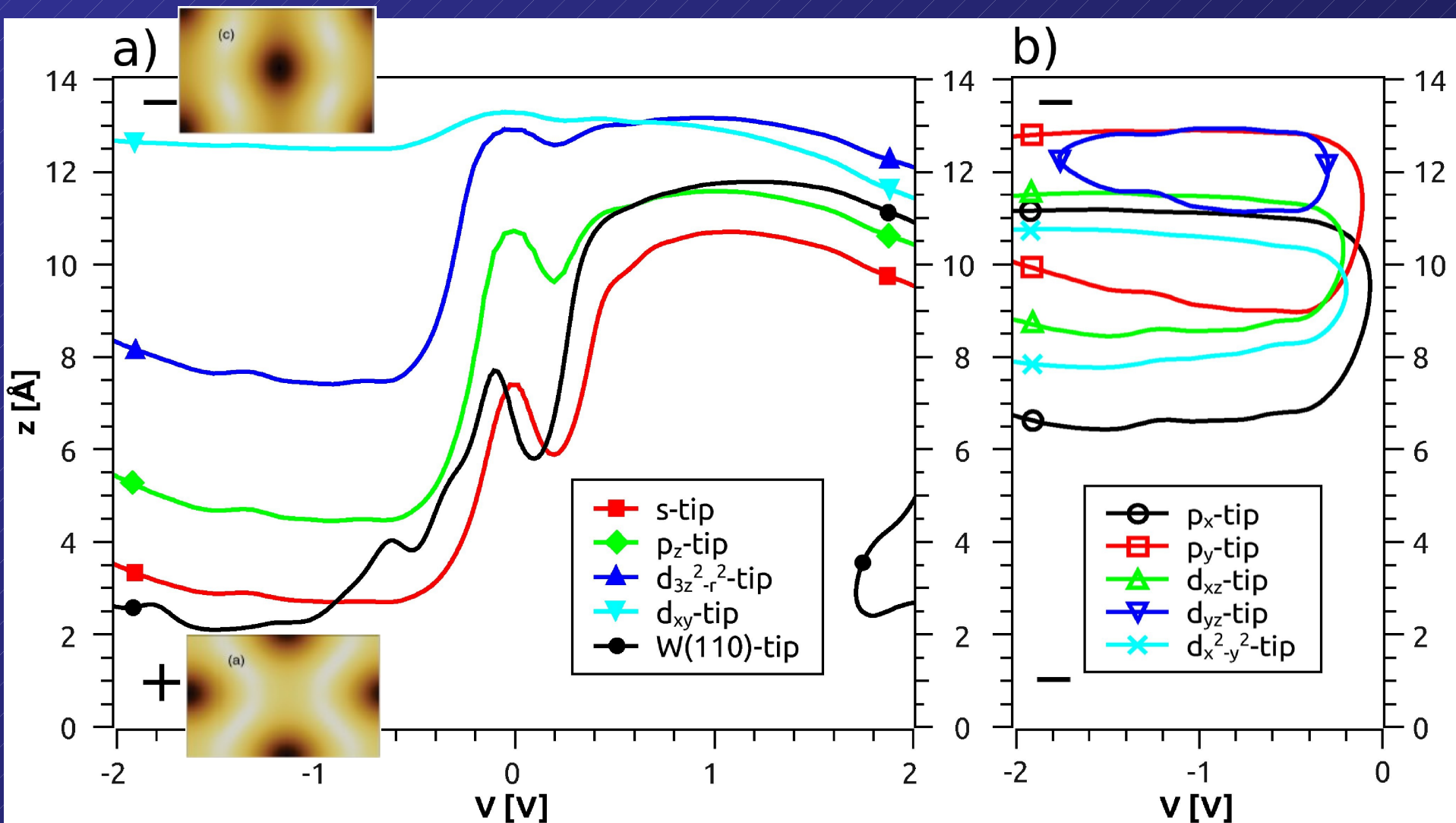
HOLLOW

0.2



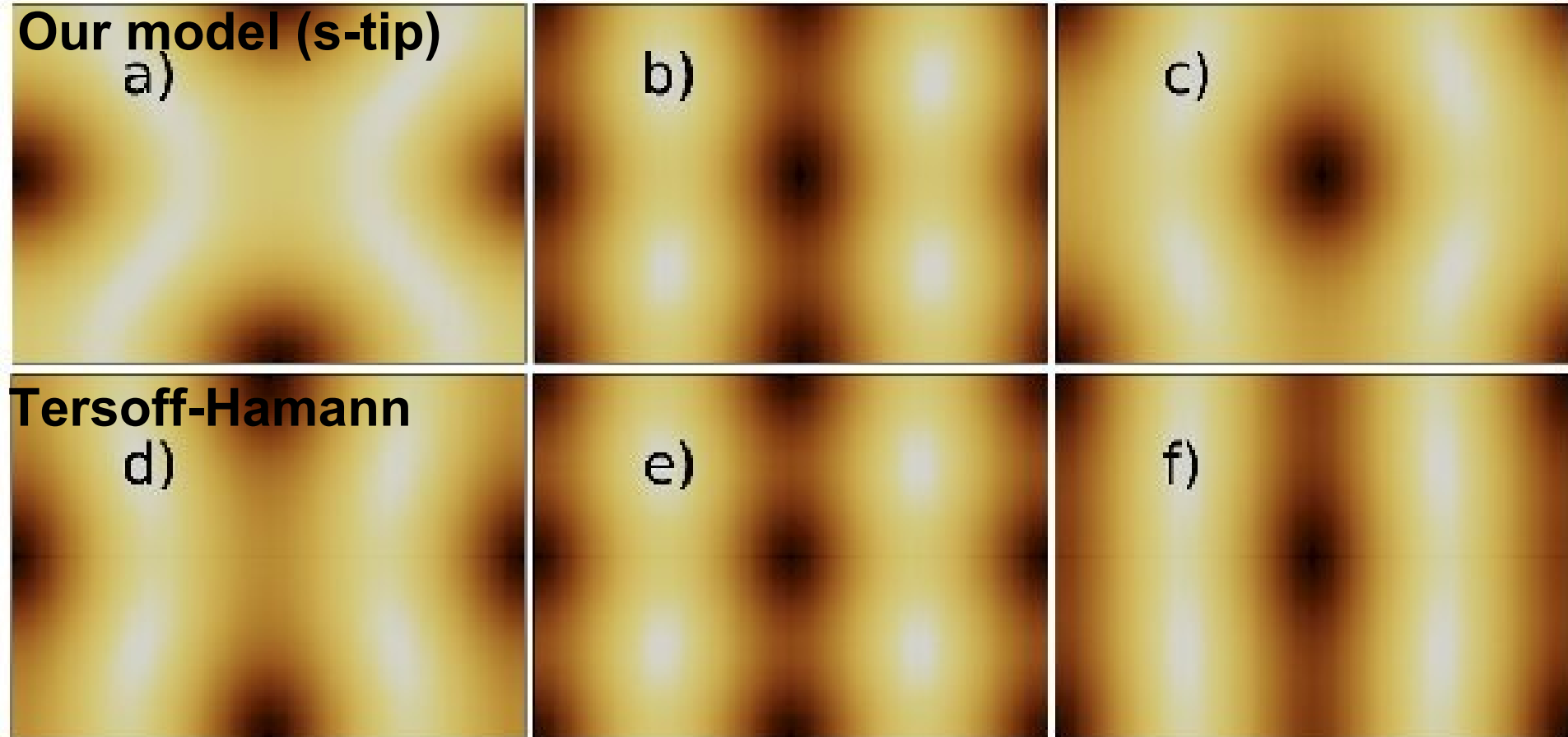
# Corrugation inversion on W(110)

Dependence on tip-symmetry, bias, and tip-sample distance



# Corrugation inversion on W(110)

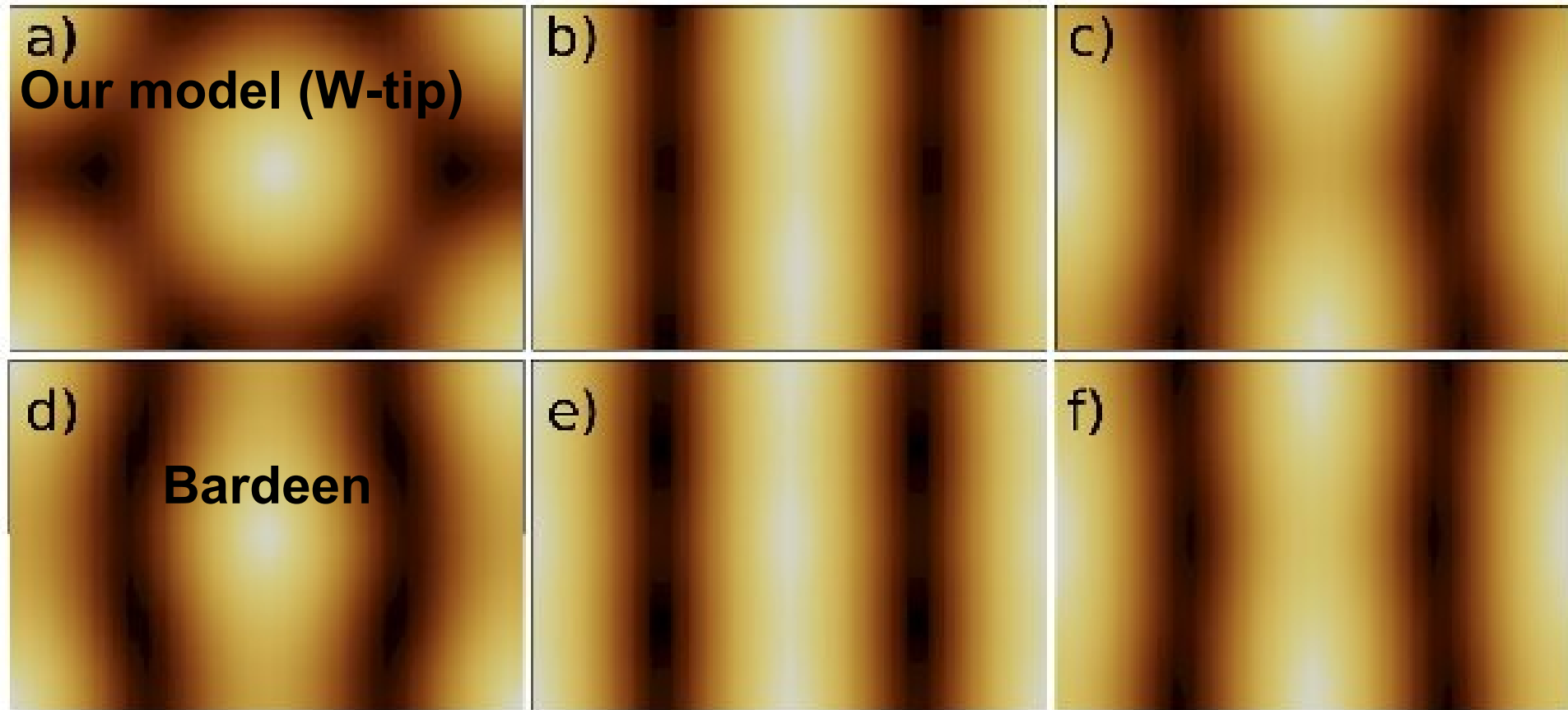
Simulated STM images,  $V=-0.25$  V



Good agreement of contrast reversal height: 4.15 vs 4.21 Å  
Good agreement with Heinze et al., PRB 58, 16432 (1998)



## Corrugation inversion on W(110)

Simulated STM images,  $V=-0.25$  V

Good agreement of contrast reversal height: 5.80 vs 5.55 Å

Computational time of our model does not depend on k-point sampling of BZ!  
Example: Sample 41x41x5, Tip 11x15x5 k-set: Our model **8500** times faster!

# Summary

- **New SP-STM/STS simulation package** developed based on first principles electronic structure data and the work of Heinze, Appl. Phys. A 85, 407 (2006).
- Main features:
  1. Imaging noncollinear surface magnetic structures
  2. Tip electronic structure considered
  3. Bias voltage included
  4. Energy dependence of local spin quantization axes included
  5. Orbital dependent tunneling transmission
- Main advantages:
  1. **Easy combination with any electronic structure code**
  2. **Possible combination of different levels of electronic structure methods for tip and surface**
  3. **Computationally cheap**
  4. **Easy to parallelize → fast**

# Work in progress - Outlook

- Going beyond the independent orbital approximation considering tunneling between **directional orbitals**
  - **arbitrary tip orientations** (comparison to experiments, at the moment graphite(0001) surface)
  - **extension to study magnetic systems**  
reveal contrast mechanisms  
**PhD work** in Budapest: **Gábor Mándi**
- Local electronic properties of **surfaces** with **Moiré** structure  
**TDK work** in Budapest: **Mátyás Seress**
- Improve tunneling theory for complex magnetic surfaces  
(**BSKAN code - Werner Hofer, Liverpool**  
**interface to noncollinear VASP code**)
- Study of **magnetic atomic contacts**  
(at the moment Ir contacts, domain walls in Co contacts)

# Conclusions

- Reproduced Fe(001) surface state peak at +0.20V in the SP-STs spectrum
- Sensitivity of SP-STs on magnetic samples can be enhanced by using proper magnetic tips. Role of effective spin polarization!  
**PRB 83, 214410 (2011)**
- $dI/dV$ : background and tip-derivative terms considered
- 2D  $dI/dV$  map, Magn. Asymm. map  $\rightarrow$  2D Eff. Spin-Pol. map  
**PRB 85, 205427 (2012)**
- Cr/Ag(111): Evidence for tip and bias dependent magnetic contrast  
**PRB 84, 174428 (2011); PRB 87, 024417 (2013)**
- Orbital dependent tunneling: W(110), **PRB 86, 235415 (2012)**

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**Thank YOU  
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